## Imaging of Charged-Particle Beams with OTR and ODR

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#### I. Introduction

## **II.** Optical Transition Radiation (OTR)

- OTR results with electrons
- OTR point-spread function (PSF) aspects
- OTR results with protons, hadrons
- III. Optical Diffraction Radiation (ODR) as a nonintercepting (NI) beam-size monitor.
  - ODR near-field experimental results (APS, CEBAF)
  - ODR model results for Gamma=1000, 46000
- IV. Summary



 The charged-particle beam transverse size and profiles are part of the basic characterizations needed in accelerators to determine beam quality.

**Intro to Beam-Size Imaging** 

- A basic beam imaging system includes:
  - conversion mechanism (scintillator, optical or x-ray synchrotron radiation (OSR or XSR), Cherenkov radiation (CR), optical transition radiation (OTR), undulator radiation (UR), and optical diffraction radiation (ODR).
  - optical transport (lenses, mirrors, filters, polarizers).
  - imaging sensor such as CCD,CID, CMOS camera, with or without intensifier and/or cooling.
  - video digitizer.

image processing software.



## **OTR Basics**



 OTR can be used for beam size/profile, position, divergence, energy, relative intensity, bunch length info.



**Coherent Spectral-Angular Distribution from a Macropulse**,

Number of Photons per Unit Frequency and Solid Angle

$$\frac{d^2 N}{d\omega d\Omega} = \left| r_{\perp, //} \right|^2 \frac{d^2 N_1}{d\omega d\Omega} I(\mathbf{k}) \mathfrak{I}(\mathbf{k})$$

$$E = 220 \text{ MeV} \quad \sigma_{x', y'} = 0.2 \text{ mrad}$$

1.0

0.4

0.2

0.0

-0.010

-0.005

0.000

Angle (radians)



$$\frac{d^2 N_1}{d\omega d\Omega} = \frac{e^2}{\hbar c} \frac{1}{\pi^2 \omega} \frac{\left(\theta_x^2 + \theta_y^2\right)}{\left(\gamma^{-2} + \theta_x^2 + \theta_y^2\right)^2}$$

From D. Rule and A. Lumpkin, PAC'01

0.010

0.005



1.0

0.8

0.6

0.4

0.2

0.0 -0.010

Relative Intensity (arb. units)

#### **Wartski Interferometer Phase Term** $E = 220 \text{ MeV}, \sigma_{x', y'} = 0.2 \text{ mrad}$

$$I(\mathbf{k}) = 4\sin^2 \left[ \frac{kL}{4} \left( \gamma^{-2} + \theta_x^2 + \theta_y^2 \right) \right]$$

L = foil separation distance

 $k_{x} = k \sin \theta \cos \phi = k \sin \theta_{x} \approx k \theta_{x}$  $k_{y} = k \sin \theta \sin \phi = k \sin \theta_{y} \approx k \theta_{y}$  $k_{z} = k \cos \theta \approx k = \omega / c$ 

 $\theta^2 = \theta_x^2 + \theta_y^2 << 1$ 

(relativistic case)

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se) From D. Rule and A. Lumpkin, PAC'01

-0.005

L= 6.3 cm,  $\lambda$ =537 nm

0.000

Angle (radians)

0.005

0.010







#### **Coherence Function**

$$\mathfrak{I}(\mathbf{k}) = N + N_B (N_B - 1) |H(\mathbf{k})|^2$$

Fourier Transform of Charge Form Factors

$$H(\mathbf{k}) = \frac{\rho(\mathbf{k})}{Q} = g_x(k_x)g_y(k_y)F_z(k_z)$$

Q = total charge of macropulse

Bunching fraction =  $f_B = N_B / N$ 

Note: The coherence function reduces to just the number of particles, N, when the number of microbunched particles,  $N_B$  is zero.

From D. Rule and A. Lumpkin, PAC'01

## Schematic Layout for APS Accelerators





# ii: 7-GeV Test with OTR at APS



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- Lebedev evaluated OTR resolution in 1996 and Castellano et al. paper in 1998 points out an OTR PSF that has polarization feature. But they calc. about 12λ (FWHM) for total width and 0.1 rad collection angle.
- Polarization effects on beam image size observed in ODR and OTR in 2007 in collaboration with JLAB.
- Dao Xiang et al. in PRST-AB (2007) calc. PSF for OTR and ODR.
- OTR polarization effects reported for A0PI beam sizes at BIW10.
- KEK OTR experiment in 2005 did not use polarizer.
- KEK OTR experiment in IPAC10 does use polarizer and PSF structure.





- Fermilab
- Perpendicular OTR component has smaller image than total OTR image by about 20 µm at 150-350 µm sizes.



A. Lumpkin et al., BIW10



#### **Resolution of near field imaging**





Because of diffraction, the image of point source is not a point but ring pattern which is determined by the OTR point spread function. For a simple model like below, the PSF would be proportional to:

$$f^{2}(\theta_{m},\gamma,\varsigma) = \left[\int_{0}^{\theta_{m}} \frac{\theta^{2}}{\theta^{2}+\gamma^{-2}} J_{1}(\varsigma\theta) d\theta\right]^{2}$$



 $\theta_m$  is the maximum acceptance angle of the lens, R<sub>I</sub> is the radius of the lens,  $\theta = R_I/a$ ,  $\varsigma = kR_i/M$ , M = b/a is the magnification factor



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## **Properties of PSF**

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- 14.3 MeV, M=1,  $\lambda$ =500 nm,  $\theta_{max}$ =0.010, sigma =25  $\mu$ m
- This version with convolutions implemented at FNAL.





## **PSF Convolved**



#### 14.3 MeV, M=1, λ=500nm, θ<sub>max</sub>=0.010, sigma =25 μm



Original Sigma = 25 Total PSF Sigma = 33.1772 HorPol-HorProj PSF Sigma = 38.0076 HorPol-VerProj PSF Sigma = 29.3867



## **PSF Convolved**



#### 14.3 MeV, M=1, λ=500 nm, θ<sub>max</sub>=.010, sigma = 10 μm



Original Sigma = 10 Total PSF Sigma = 22.5904 HorPol-HorProj PSF Sigma = NA HorPol-VerProj PSF Sigma = 16.627





 KEK staff used vertical polarizer and small beam to observe PSF and suggested potential use of structure.







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Figure 4: Horizontal RMS beam size as a function of the QF19X strength (a) and the dependence of the smoothing parameter  $\sigma$  (Eq. 1) versus QD18X quadrupole magnet strength. SAD predictions of the vertical beam size for the same magnet strengths are also shown in the picture.

$$f(x) = a + \frac{b}{1 + [c(x - \Delta x)]^4} \left[ 1 - e^{-2c^2\sigma^2} \cos[c(x - \Delta x)] \right] \quad (1)$$

where a, b, c,  $\sigma$ , and  $\Delta x$  are free parameters of the fit function, namely: a is the vertical offset of the distribution with respect to zero which included a constant background; b is the amplitude of the distribution; c is the distribution width;  $\sigma$  is the smoothing parameter dominantly defined by the beam size; and  $\Delta x$  is the horizontal offset of the distribution with respect to zero

A. Aryshev et al., IPAC10





- It seems the OTR PSF polarization effect is a symmetric difference in image size around the total PSF size in the model, while the JLAB data are strongly asymmetric in effect magnitude.
- Postulate this anomalous aspect is due to the induced current distribution as revealed through polarized OTR.
- Such strong asymmetry also seen in the ODR data and simulations. Perpendicular component is better.
- The broken A.D. symmetry at low gamma should be in the PSF calc. model.





# • Five OTR stations in beamlines at Fermilab after feasibility evaluated by Lumpkin and Scarpine (PAC03).





## **OTR Station at Fermilab**









#### V.E. Scarpine and A. H. Lumpkin





#### Intense beams imaged before the NUMI target.





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#### Initial success on imaging 120 GeV protons @10<sup>13</sup> ppp.



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#### Both single-foil and two-foil effects considered.





A. Lumpkin et al., PAC07

### First 120-GeV Pbar Beam OTR Images Obtained 5-15-07 at FNAL



#### Antiprotons (Pbars) were less intense than proton beams, but still can be imaged in a transport line.



V.E Scarpine, A.H. Lumpkin

### OTR Works for Intense Relativistic Hadrons, What About Heavy Ions (HI)?



- Is there sufficient charge crossing the interface so OTR could be detectable? Use Q<sup>2</sup> and β<sup>2</sup> dependencies.
- Can the thin foil survive the areal charge density levels? (Beamline exit windows and stripper foils do).
- 120-GeV protons, up to 10<sup>13</sup> in a 10-μs batch in 1mm x 1mm spot on aluminized Kapton (6 μm). Screen survived 6 months in beam at Fermilab.
- Look at lobe angle like 80-keV electrons? Or other.
- Use ICCD, cooled CCD, or CMOS cameras to boost sensitivity to low signals.
- Use Forward OTR; with annular mirror? Out of stripper foil?
- What beam intensity levels used at GSI (and LHC)?



- Fermilab
- Consider applying technologies and concepts for ions.
- Take advantage of charge state for OTR generation.





Table I. Comparison of various particle beam cases and estimated OTR photons generated for ions (Preliminary).

Part.	E(MeV)	<u>Q</u>	<u>β</u>	<u> </u>	<u>Y(ph/e)</u>	<u>N</u>	<u>Mult.</u>	Photon #	<u>CCD</u>
e⁻	.080	1	0.63	1.15	2x10 <sup>-6</sup>	4x10 <sup>1</sup>	<sup>1</sup> 1	7x10 <sup>5</sup>	*Int.
e⁻	150	1	0.99	300	2x10 <sup>-3</sup>	6x10 <sup>g</sup>	) _	1x10 <sup>7</sup>	yes
p+	120x10 <sup>3</sup>	<sup>5</sup> 1	0.99	129	10 <sup>-3</sup>	<b>10</b> <sup>11</sup>	-	10 <sup>8</sup>	CID
	MeV/u								
Ar+	11.4	10	0.15	1.01	10 <sup>-6</sup>	<b>10</b> <sup>10</sup>	5.3	5x10 <sup>4</sup>	∗Int.
U+	11.4	28	0.15	1.01	10 <sup>-6</sup>	<b>1</b> 0 <sup>11</sup>	42	4x10 <sup>6</sup>	∗Int.
U+	300	73	0.65	$1.2^{\circ}$	1 10 <sup>-6</sup>	10 <sup>9</sup>	5329	$9 5 \times 10^6$	*Int

\*Use intensifier for gain and the gating feature. More discussions later today. Also the ion intensity increases projected for FAIR look even better for photon numbers. The Multiplier (Mult.) column is the estimated scaling with  $Q^2\beta^2$ .





- Diffraction radiation is produced when a charge moving at constant velocity passes nearby a boundary between media with different dielectric constants.
  - DR is produced by the interaction between the EM fields of the traveling charge and the conducting screen

    \*the image charge currents radiate, ODR is radially polarized.
    The extension of the electromagnetic field of a relativistic particle is a flat circle of diameter  $\gamma \lambda / 2\pi$ ,
    The radiation intensity is  $I \propto e^{-\frac{2\pi a}{\gamma \lambda}}$ No radiation

    DR impact parameter is  $\frac{\gamma \lambda}{2\pi} \Rightarrow$  if a  $\frac{\gamma \lambda}{2\pi}$  DR  $< <\frac{\gamma \lambda}{2\pi}$  TR

Enrica Chiadroni LNF - INFN





#### **Diffraction Radiation Observables**

- Near field (at or near target) intensity
- Far field angular distribution
- Polarization
- Frequency spectrum
- Interference between radiation from 2 sources

These can be combined to measure potentially

- Beam size
- Beam position
- Beam divergence
- Energy

Recent measurements at KEK, APS, FLASH, CEBAF Interest at other labs: BNL



• Path to test near-field imaging on 10-µm size at 23 GeV.



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## **ODR Demonstrations**



Tech- nique, Near or Far field	Beam Energy (GeV	Beam size (µm)	Charge	Detector	Div. (µrad)	Lab
Slit in plane,F	1.2	10-14	1 nC	PMT, scan	1.5	KEK
Slit in plane,F	0.68, 0.90	85**	30 nC	Cooled CCD	80	INFN/ FLASH
Single plane,N	7	1300	3 nC	CCD	70	APS/ ANL
Single plane,N	4.5	120	80 µC	CCD		FNAL/ CEBAF
Slit in plane,N	0.90	200	30 nC	Cooled CCD	80**	FNAL/ INFN
Two planes,F	0.90	89	30 nC**	Cooled CCD	150	INFN/ FLASH
Two-1/2 Planes	1.2, 0.9	10, 90		Cooled CCD		KEK, INFN

# CODR is a Potential Nonintercepting Diagnostic for GeV Lepton Beams and TeV. Hadron Beams

- At left, schematic of ODR generated from two vertical planes (based on Fig.1 of Fiorito and Rule, NIM B173, 67 (2001). We started with a single plane.
- At right, calculation of the ODR light generated by a 7-GeV electron beam for d =1.25 mm in the optical near field based on a new model (Rule and Lumpkin).





• We convolved the electron beam's Gaussian distribution of sizes  $\sigma_x$  and  $\sigma_y$  with the field expected from a single electron at point *P* in the metal plane (J.D. Jackson)

$$\frac{dI}{d\omega}(\boldsymbol{u},\omega) = \frac{1}{\pi^2} \frac{q^2}{c} \left(\frac{c}{v}\right)^2 \alpha^2 N \frac{1}{\sqrt{2\pi\sigma_x^2}} \frac{1}{\sqrt{2\pi\sigma_y^2}} \times \int dx dy K_1^2(\alpha b) e^{-\frac{x^2}{2\sigma_x^2}} e^{-\frac{y^2}{2\sigma_y^2}},$$

where  $\omega$  = radiation frequency, v = electron velocity  $\approx$  c = speed of light, q = electron charge, N is the particle number, K<sub>1</sub>( $\alpha$ b) is a modified Bessel function with  $\alpha$ = 2 $\pi$ / $\gamma$  $\lambda$  and b is the impact parameter.

Lumpkin et al., Phys. Rev. ST-AB, Feb. 2007





- Electron beam energy = 7GeV,  $\gamma$ = 13,699
- Bunch intensity ~ 1.9x10<sup>10</sup> (3 nC)
- Beam sizes:  $\sigma_x = 1375 \ \mu m$ ,  $\sigma_y = 200 \ \mu m$
- Typical impact parameter ~ 5 σ<sub>y</sub>
- Wavelength  $\lambda \sim 0.4-0.8 \ \mu m$
- Sensitive to horizontal offsets of 50-100 µm
- Sensitive to beam size changes of 20%

## 7-GeV Test at APS

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Lumpkin et al., PRST-AB (Feb. 2007)



• Quadrupole current scan provides beam-size scan.



- ODR size tracks OTR or bunch real size
- ODR/OTR ratio function of ODR PSF

Lumpkin et al., Phys. Rev. ST-AB, Feb. 2007

#### **IC** ODR Also Has Good NI Beam-Position Sensitivity Using Orthogonal Polarization Component

OTR and ODR Image Centroid versus Horizontal rf BPM values are linear.



ODR also BPM

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 CEBAF beam size is 10 times smaller and the charge is 1000 times greater than APS case. What are background sources?

<u>Parameter</u>	<u>APS</u>	<u>CEBAF</u>	<u>ILC</u>
Energy (GeV)	7	1- 5	5, 250
X Beam size (μm)	1300	100-150	300, 30
Y Beam size (μm)	200	100-150	15, 2
Current (nA)	6	100,000	50,000
Charge/ 33 ms (nC)	3	3,000	10,000

A. Lumpkin et al., PAC07



#### Polarization Component effects are very clear in ODR.











• Effects of vertical polarizer and 550x10 nm Bandpass filter on ODR profile size are shown.



 ODR size tracks OTR and flying wire (FW) size, better V-pol. and 550nm filter



• Path to test near-field imaging on 10-µm size at 23 GeV.





• New parameter space for ODR tests provided at FACET.

Parameter	<u>APS</u>	<u>CEBAF</u>	ILC	<u>FACET</u>
Energy (GeV)	7	1-5	5,15,250	23
X Beam size (μm) Y Beam size (μm)	1300 200	80-100 80-100	300,150,3 15,8,2	30 10 10
Current (nA)	6	100,000	50,000	30
Charge/ 33 ms (nC)	3	3,000	10,000	3

FACET parameters more similar to ILC parameter.





#### • Scaling from APS test at 7 GeV indicates signals OK.

<u>Parameter</u>	<u>APS</u>	FACET
Charge (nC)	3	3
Rep, rate (Hz)	2	10
Energy (GeV)	7	23
Beam size (um)	1300 x 200	10 x 10
γλ/2π (mm)	1.4	4.6
5 sigma-y (mm)	1.0	0.05
CCD	8 bit	12 bit









#### Vertical polarization component, lambda= 800 nm, IP= 100, 50 μm. Curves for 10, 20, 35, 50,100 μm.







 Parallel polarization component shows beam-size effect at 10-µm regime. Curves for 10, 20, 35, 50,100 µm.



- H-Pol "valley" also sensitive to bunch size
- More sensitive with IP=50 $\mu$ m (small  $\sigma_x$ )





- New OTR converter using aluminized Kapton for the 20mm aperture was prepared at Fermilab Thin Films lab by Eileen Hahn. About 1500 Angstroms of Al deposited by evaporation method on a stretched 6-µm thick Kapton film for CEBAF experiments. (possibly for GSI).
- New ODR converter was prepared by sputtering a 600 Angstrom AI coating on a 300-µm thick Si wafer cut for <100> plane. (Possibly use same type at FACET.)









 ODR Point spread function (PSF) may be defined for optical system so can deconvolve from observed image.



 Beam profile and not only size and position can (potentially) be measured with NI ODR!!



• NML examples for beam-size monitor for  $\sigma_x=200 \ \mu m$  (L) and 400  $\mu m \pm 20\%$  (R) with  $\sigma_y=200 \ \mu m$ ,  $d = 5 \ \sigma_y$ , and  $\gamma=1000$ .



Courtesy of C.-Y. Yao, ANL



• Examples for beam-size monitor for  $\sigma_x$ =400 ±20% µm with  $\sigma_y$ =400 µm,  $d = 12 \sigma_y$ , and  $\gamma$ =1000.  $\lambda$ =0.8 µm (left) and 10 µm (right).



**Perpendicular Polarization** 

Courtesy of C.-Y. Yao , ANL

## ic ODR Model Shows Beam-size Effects



• LHC examples for beam-size monitor for  $\sigma_x$ =800 µm and varying *d* from 4.8-8 mm (L), and with  $\sigma_x$ =800 µm ± 20%,  $\sigma_y$ =800 µm, *d* = 6  $\sigma_y$ ,  $\lambda$ =1.0 µm, and  $\gamma$ =7500 (R).



**Perpendicular Polarization** 

Courtesy of C.-Y. Yao, ANL





- Extensive experience with OTR imaging of relativistic leptons and some with hadrons provides base for diagnostic applications.
- OTR polarization effects need to be elucidated, and the microbunching instability COTR discussed Monday is a challenge for imaging bright beams. (Mitigation options).
- OTR imaging seems to have potential for intense, non-relativistic heavy ion beams in many GSI-FAIR cases. Follow-up needed.
- Demonstrations of ODR imaging for leptons done in several labs and parameter sets. Further tests at FACET and NML proposed.
- Modeling done for ODR imaging of hadrons in principle, but not very practical in rings, possibly in transport lines.
- The future still remains bright for imaging techniques for chargedparticle beam diagnostics.



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