



Beam Position Monitor:

Detector Principle, Hardware and Electronics

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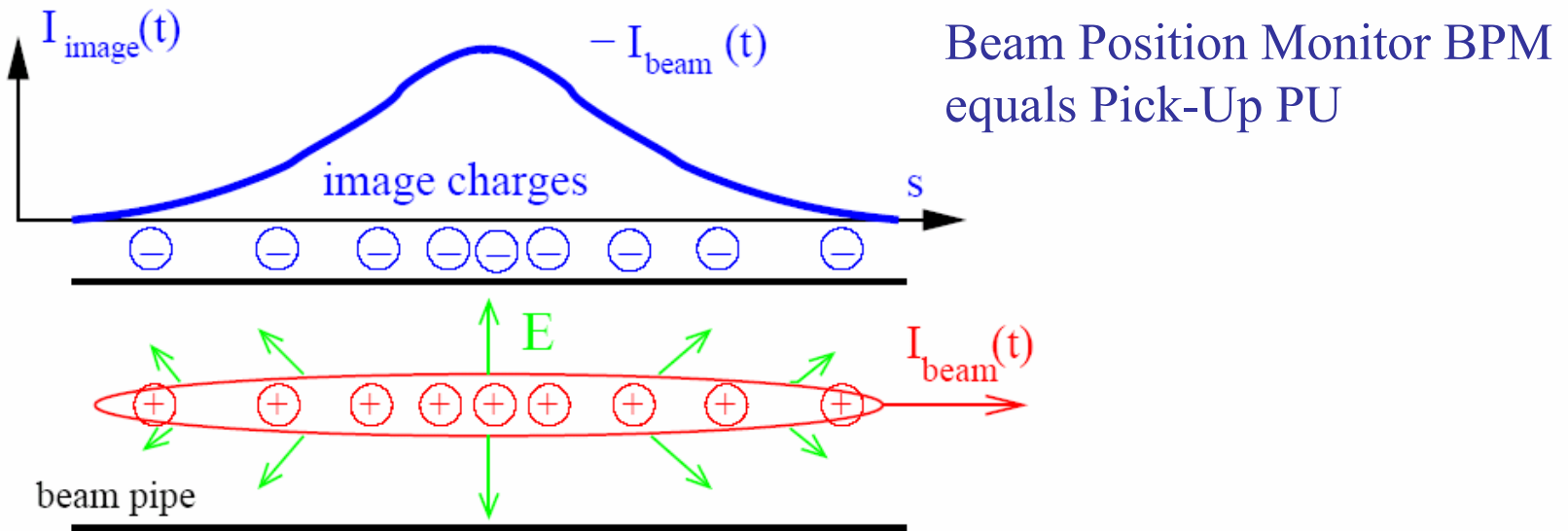
Outline:

- *Signal generation → transfer impedance*
- *Consideration for capacitive shoe box BPM*
- *Consideration for capacitive button BPM*
- *Other BPM principles: stripline → traveling wave*
 - inductive → wall current*
 - cavity → resonator for dipole mode*
- *Electronics for position evaluation*
- *Some examples for position evaluation and other applications*
- *Summary*

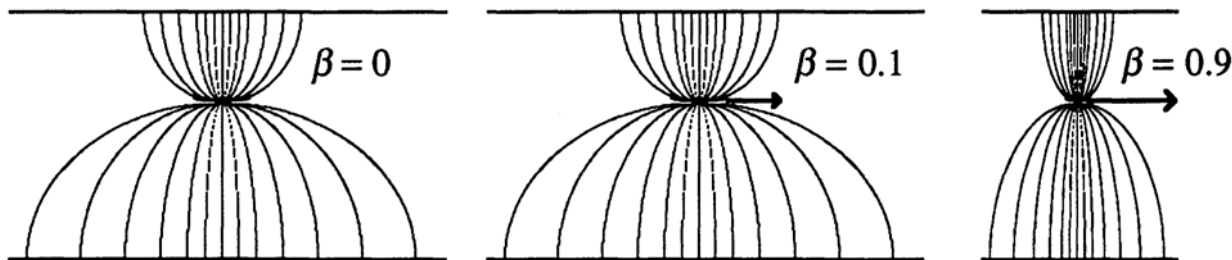
General Idea: Detection of Wall Charges



The image current at the vacuum wall is monitored on a high frequency basis i.e. the ac-part given by the bunched beam.



For relativistic velocities, the electric field is mainly transversal: $E_{\perp,lab}(t) = \gamma \cdot E_{\perp,rest}(t)$



Usage of BPMs



A BPM is an non-destructive device

It has a low cut-off frequency i.e. dc-beam behavior can not be monitored
(exception: Schottky spectra, here the physics is due to finite number of particles)

⇒ Usage with bunched beams!

It delivers information about:

1. The center of the beam

- Closed orbit
i.e. central orbit averaged over a period much longer than a betatron oscillation
- Bunch position on a large time scale: bunch-by-bunch → turn-by-turn → averaged position
- Single bunch position → determination of parameters like tune, chromaticity, β -function
- Time evolution of a single bunch can be compared to ‘macro-particle tracking’ calculations
- Feedback: fast bunch-by-bunch damping → precise (and slow) closed orbit correction

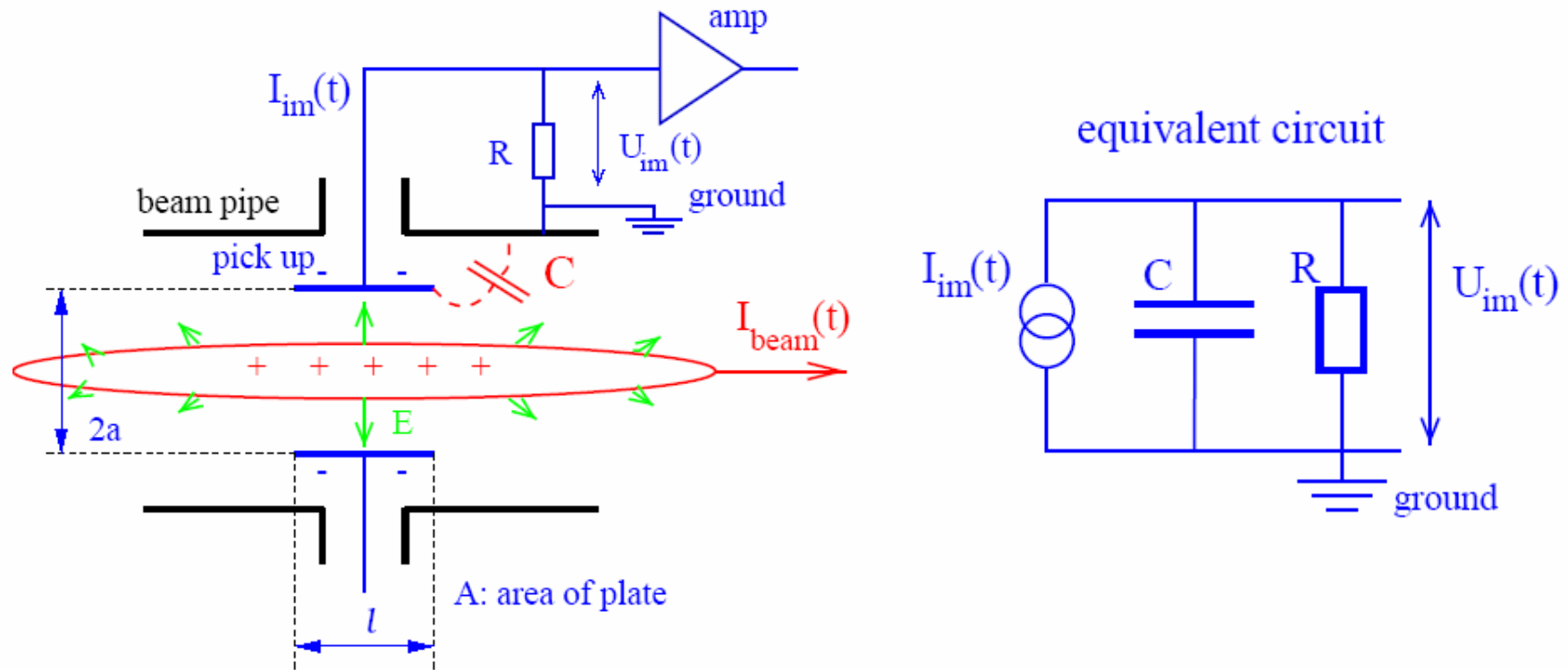
2. Longitudinal bunch shapes

- Bunch behavior during storage and acceleration
- For proton LINACs: the beam velocity can be determined by two BPMs
- *Relative* low current measurement down to 10 nA.

Model for Signal Treatment of capacitive BPMs



The wall current is monitored by a plate or ring inserted in the beam pipe:



The image current I_{im} at the plate is given by the beam current and geometry:

$$I_{im}(t) \equiv dQ_{im}/dt = A/2\pi a l \cdot dQ_{beam}(t)/dt = A/2\pi a l \cdot l/\beta c \cdot dI_{beam}/dt$$

$$= A/2\pi a \cdot l/\beta c \cdot i\omega I_{beam}(\omega)$$

Using a relation for Fourier transformation: $I_{beam} = I_0 e^{i\omega t} \Rightarrow dI_{beam}/dt = i\omega I_{beam}$.

Transfer Impedance for capacitive BPM



At a resistor R the voltage U_{im} from the image current is measured.

The transfer impedance Z_t is the ratio between voltage U_{im} and beam current I_{beam} in *frequency domain*: $U_{im}(\omega) = R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega)$.

Capacitive BPM:

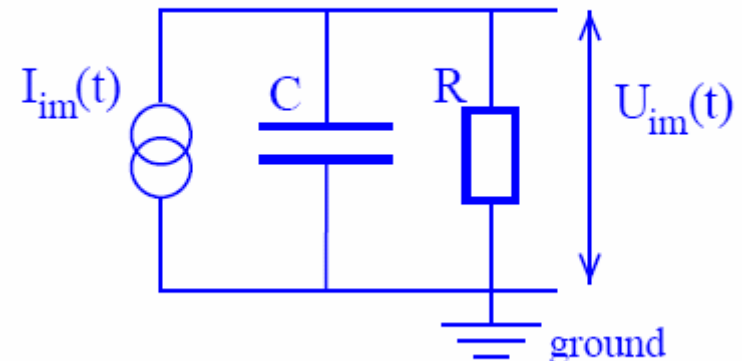
- The pick-up capacitance C :
plate \leftrightarrow vacuum-pipe and cable.
- The amplifier with input resistor R .
- The beam is a high-impedance current source:

$$\begin{aligned} U_{im} &= \frac{R}{1+i\omega RC} \cdot I_{im} \\ &= \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{i\omega RC}{1+i\omega RC} \cdot I_{beam} \\ &\equiv Z_t(\omega, \beta) \cdot I_{beam} \end{aligned}$$

This is a high-pass characteristic with $\omega_{cut} = 1/RC$:

$$\text{Amplitude: } |Z_t(\omega)| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}} \quad \text{Phase: } \varphi(\omega) = \arctan(\omega_{cut} / \omega)$$

equivalent circuit



$$\frac{1}{Z} = \frac{1}{R} + i\omega C \Leftrightarrow Z = \frac{R}{1+i\omega RC}$$

Example of Transfer Impedance for Proton Synchrotron



The high-pass characteristic for typical synchrotron BPM:

$$U_{im}(\omega) = Z_t(\omega) \cdot I_{beam}(\omega)$$

$$|Z_t| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$$

$$\varphi = \arctan(\omega_{cut} / \omega)$$

Parameter for shoe-box BPM:

$C=100\text{pF}$, $l=10\text{cm}$, $\beta=50\%$

$$f_{cut} = \omega / 2\pi = (2\pi RC)^{-1}$$

for $R=50\ \Omega \Rightarrow f_{cut} = 32\ \text{MHz}$

for $R=1\ \text{M}\Omega \Rightarrow f_{cut} = 1.6\ \text{kHz}$

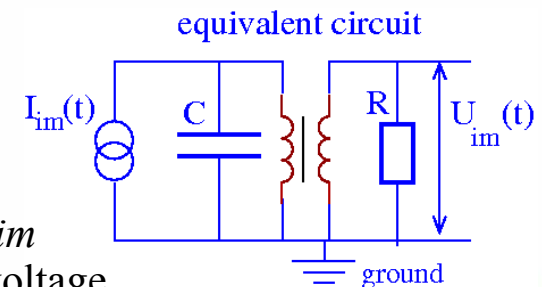
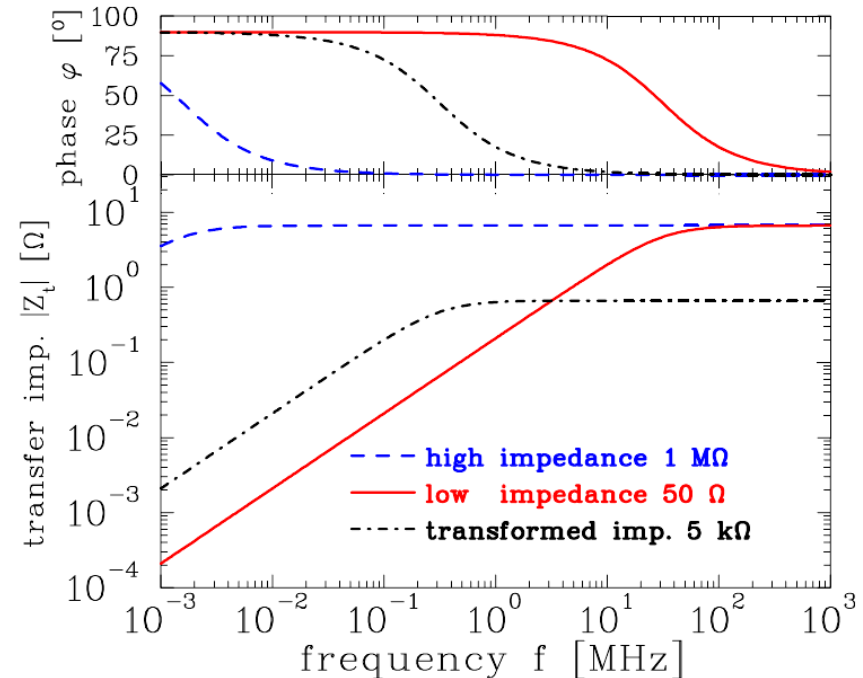
Large signal strength \rightarrow **high impedance**

Smooth signal transmission \rightarrow **50 Ω**

Compromise $\rightarrow \approx 5\ \text{k}\Omega$ by transformer e.g. $N_{prim}/N_{sec}=3:30$

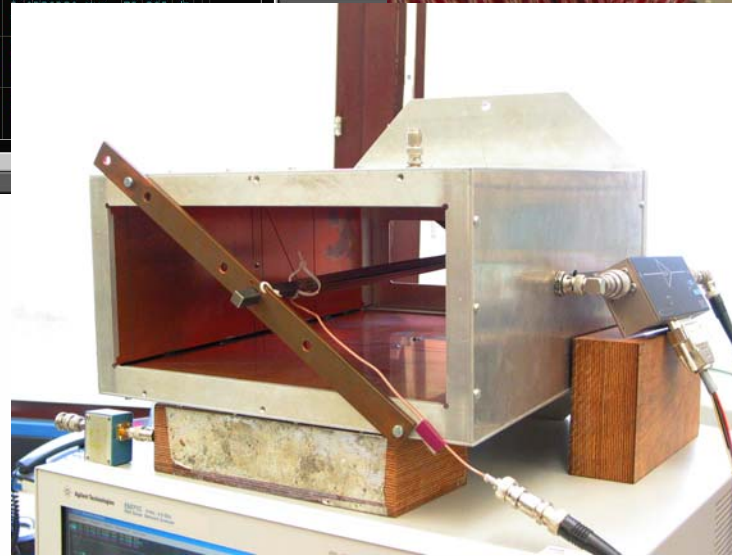
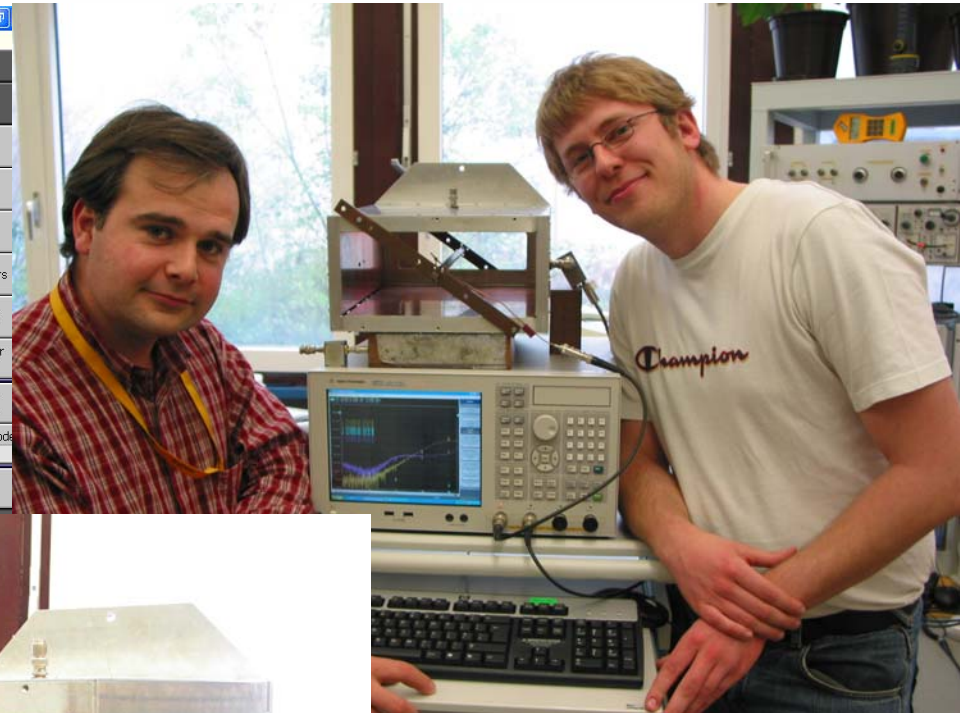
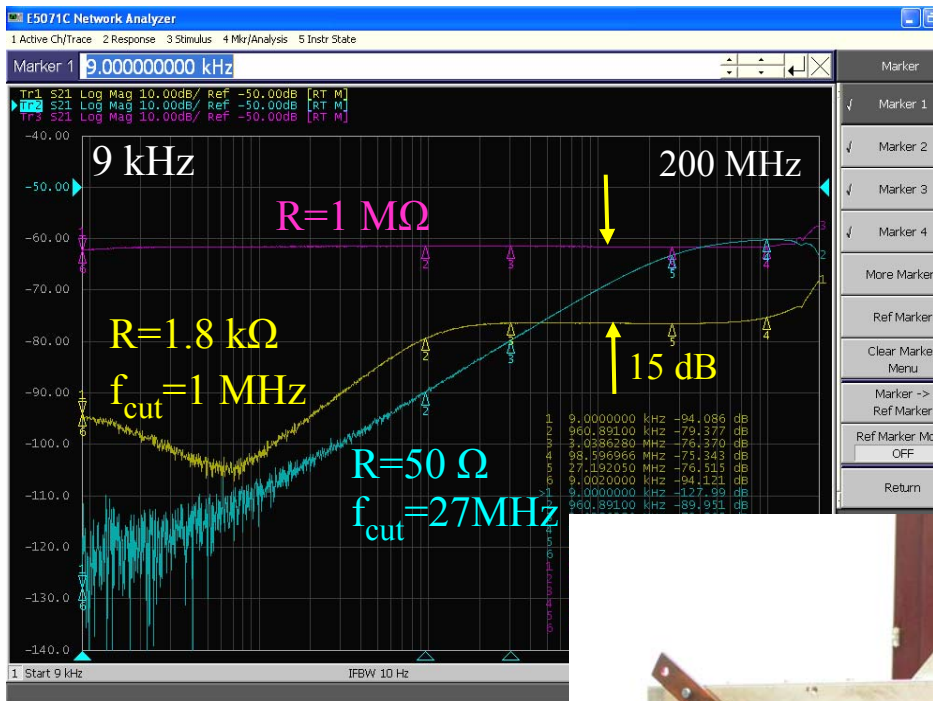
Impedance $Z_{prim} = (N_{prim}/N_{sec})^2 \cdot Z_{sec}$ voltage $U_{im} = N_{sec}/N_{prim} \cdot U_{prim}$

\rightarrow Smooth signal chain, medium cut-off frequency, but lower usable voltage



Transfer Impedance Measurement

With a network analyzer and an antenna the BPM properties can be determined.



Test BPM of $250 \times 80 \text{ mm}^2$
using a stripline antenna
of 300 MHz bandwidth

Signal Shape for capacitive BPMs: differentiated ↔ proportional



Depending on the frequency range *and* termination the signal looks different:

➤ *High frequency range* $\omega \gg \omega_{cut}$:

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow 1 \Rightarrow U_{im}(t) = \frac{1}{C} \cdot \frac{1}{\beta c} \cdot \frac{A}{2\pi a} \cdot I_{beam}(t)$$

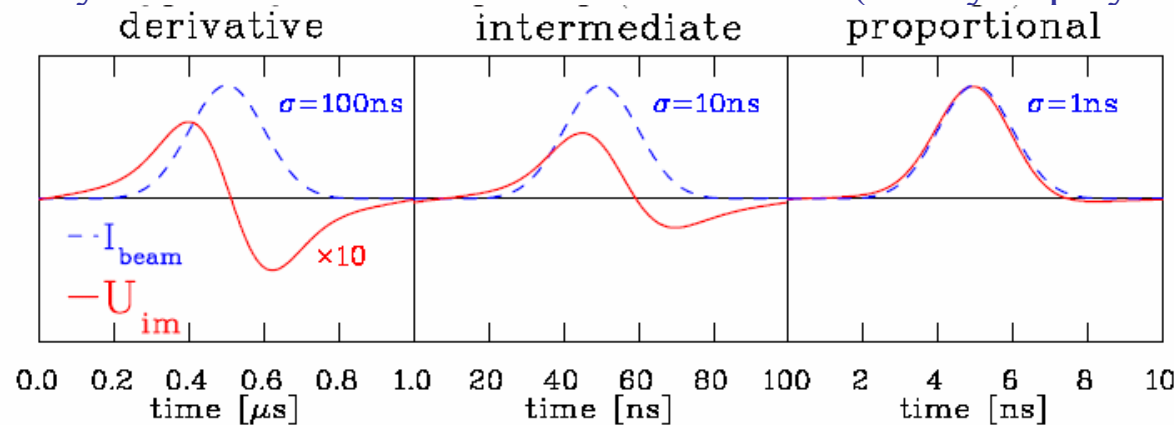
⇒ **direct image** of the bunch. Signal strength $Z_t \propto A/C$ i.e. nearly independent on length

➤ *Low frequency range* $\omega \ll \omega_{cut}$:

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow i \frac{\omega}{\omega_{cut}} \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot i\omega I_{beam}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$$

⇒ **derivative** of bunch, single strength $Z_t \propto A$, i.e. (nearly) independent on C

Example from synchrotron BPM with 50 Ω termination (reality at p-synchrotron : $\sigma \gg 1$ ns):



Examples for differentiated & proportional Shape



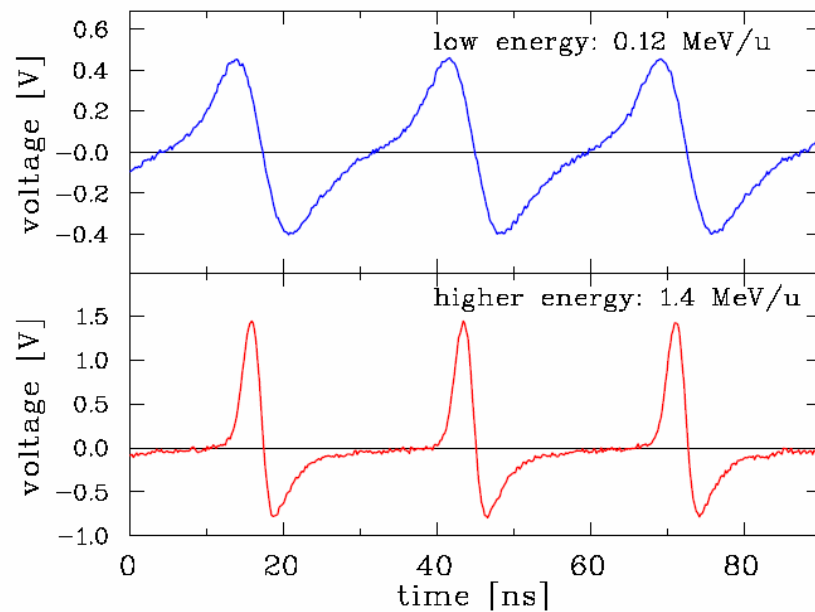
Proton LINAC, e⁻-LINAC & synchrotron:

$100 \text{ MHz} < f_{rf} < 1 \text{ GHz}$ typically

$R=50 \ \Omega$ processing to reach bandwidth

$C \approx 5 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 700 \text{ MHz}$

Example: 36 MHz GSI ion LINAC



Proton synchrotron:

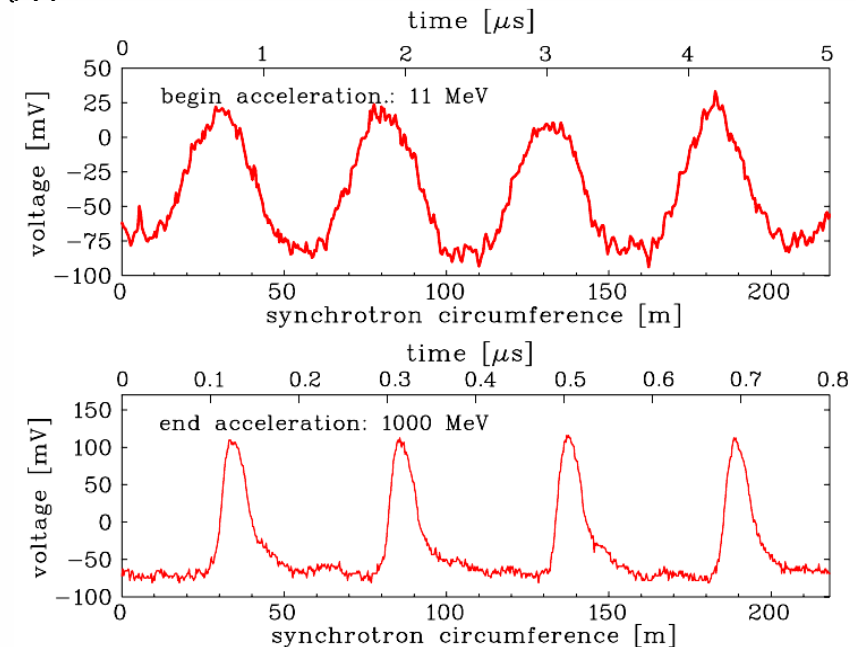
$1 \text{ MHz} < f_{rf} < 30 \text{ MHz}$ typically

$R=1 \text{ M}\Omega$ for large signal i.e. large Z_t

$C \approx 100 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 10 \text{ kHz}$

Example: non-relativistic GSI synchrotron

$f_{rf}: 0.8 \text{ MHz} \rightarrow 5 \text{ MHz}$



Remark: During acceleration the bunching-factor is increased: ‘adiabatic damping’.

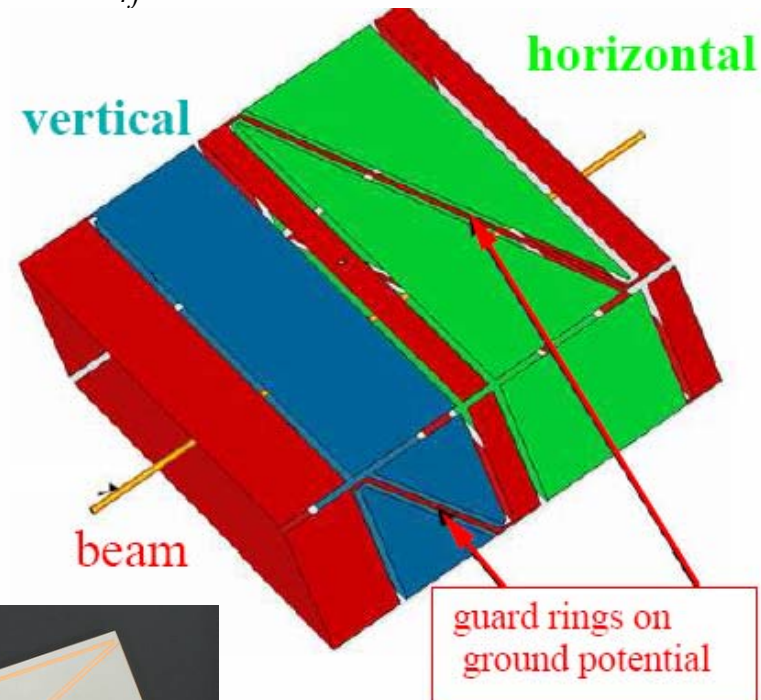
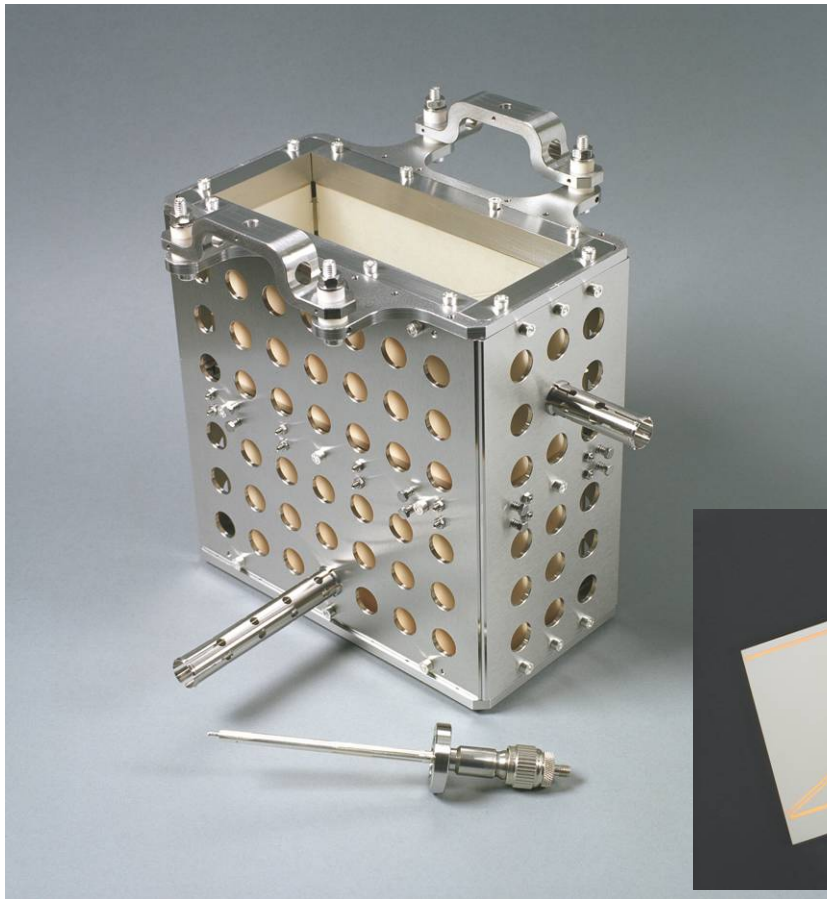


Example Shoe-box BPMs

Shoe-box BPMs used at low β proton & ion synchrotron for $1\text{MHz} < f_{rf} < 10\text{MHz}$.

Example: HIT cancer therapy synchrotron $0.8\text{MHz} < f_{rf} < 5\text{MHz}$

Aperture $180 \times 70\text{mm}^2$

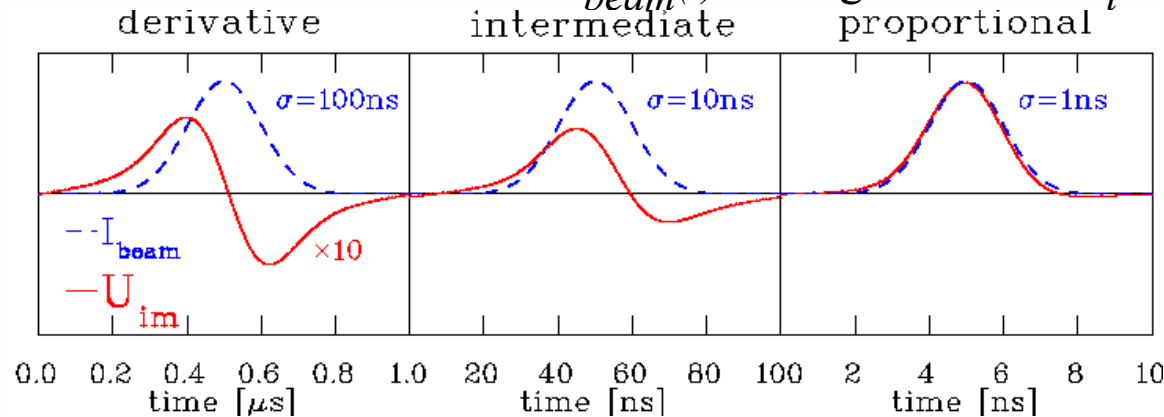


Calculation of Signal Shape: Single Bunch

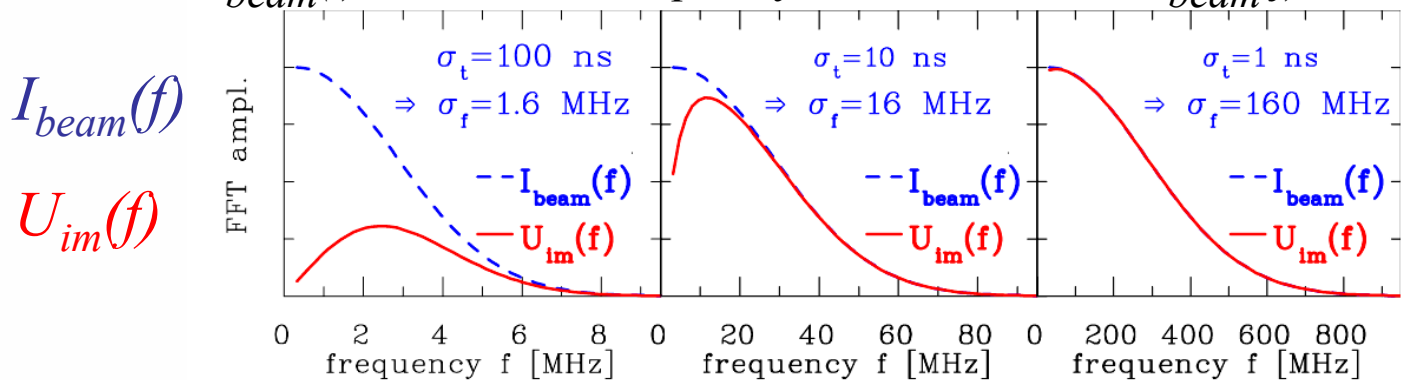


The transfer impedance is used in frequency domain! The following is performed:

- 1. Start:** Time domain Gaussian function $I_{beam}(t)$ having a width of σ_t



- 2. FFT** of $I_{beam}(t)$ leads to the frequency domain Gaussian $I_{beam}(f)$ with $\sigma_f=(2\pi\sigma_t)^{-1}$



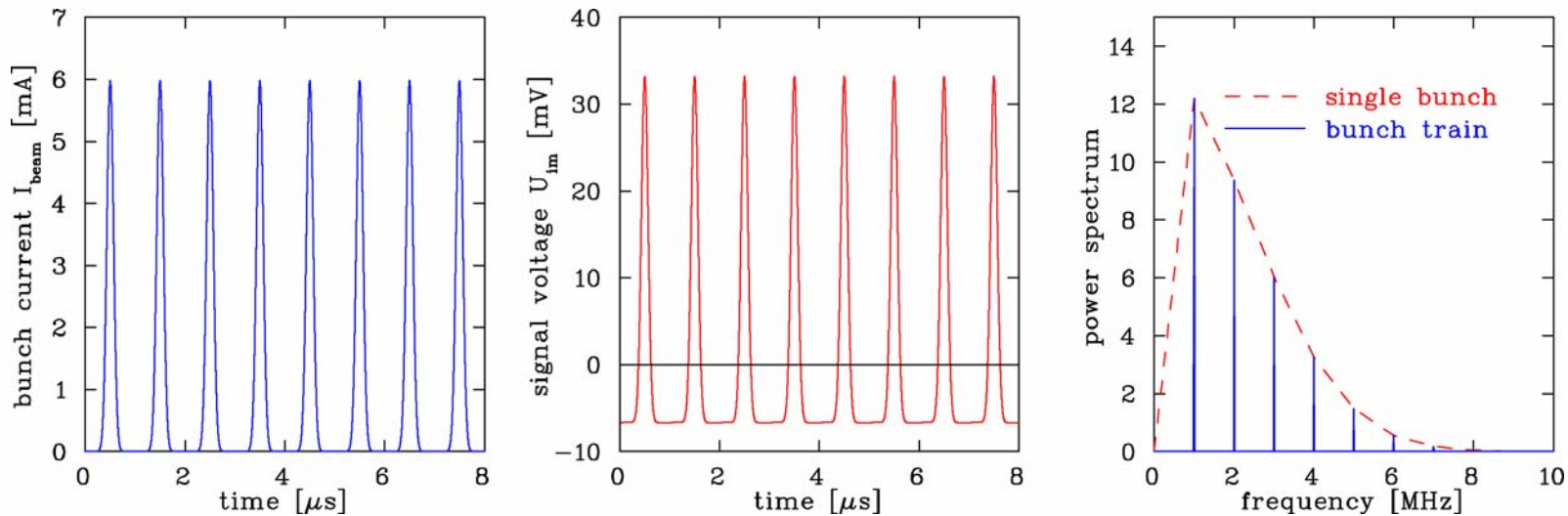
- 3. Multiplication** with $Z_t(f)$ with $f_{cut}=32\text{ MHz}$ leads to $U_{im}(f)=Z_t(f)\cdot I_{beam}(f)$

- 4. Inverse FFT** leads to $U_{im}(t)$



Calculation of Signal Shape: Bunch Train

Example for low energy proton synchrotron: Train of bunches with $R=1 \text{ M}\Omega$



$$\text{Calculation: } I_{beam}(t) \xrightarrow{\text{FFT}} I_{beam}(\omega) \rightarrow U_{im}(\omega) = Z_{tot}(\omega) \cdot I_{beam}(\omega) \xrightarrow{\text{invFFT}} U_{im}(t)$$

Parameter: $R=1 \text{ M}\Omega \Rightarrow f_{cut}=2\text{kHz}$, $Z_t=5\Omega$ all buckets filled, no amp

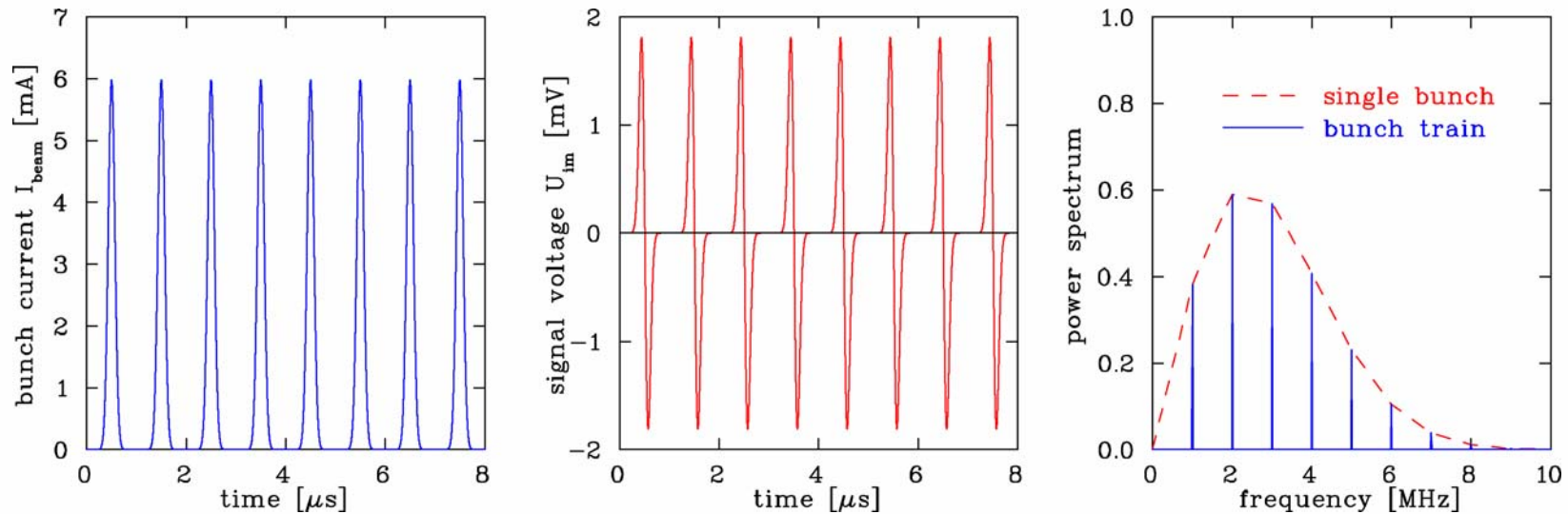
$$C=100\text{pF}, l=10\text{cm}, \beta=50\%, \sigma_t=100 \text{ ns} \Rightarrow \sigma_l=15\text{m}$$

- Fourier spectrum is composed of lines separated by acceleration f_{rf}
- Envelope given by single bunch Fourier transformation
- Baseline shift due to ac-coupling

Remark: $1 \text{ MHz} < f_{rf} < 10\text{MHz} \Rightarrow \text{Bandwidth} \approx 100\text{MHz} = 10 \cdot f_{rf}$ for broadband observation

Calculation of Signal Shape: Bunch Train

Train of bunches with $R=50 \Omega$ termination:



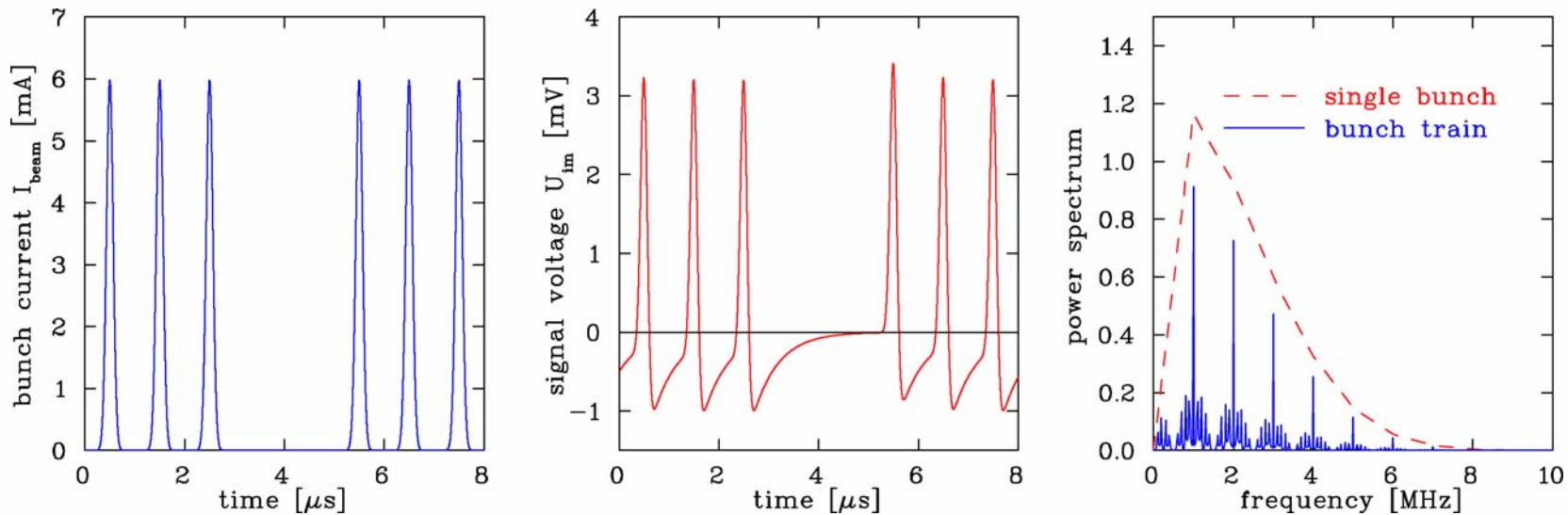
Parameter: $R=50 \Omega \Rightarrow f_{\text{cut}}=32 \text{ MHz}$, all buckets filled, no amp
 $C=100\text{pF}$, $l=10\text{cm}$, $\beta=50\%$, $\sigma_t=100 \text{ ns}$

- Low frequency cut-off due to $f_{\text{cut}}=32 \text{ MHz}$
- Differentiated bunches, 15 fold lower amplitude
- Modified Fourier spectrum with low amplitude value, maximum shift to higher frequencies

Calculation of Signal Shape: Bunch Train with empty Buckets



Synchrotron during filling: Empty buckets, $R=5 \text{ k}\Omega$ termination:



Parameter: $R=5 \text{ k}\Omega \Rightarrow f_{\text{cut}}=320 \text{ kHz}$, 2 empty buckets

$C=100\text{pF}$, $l=10\text{cm}$, $\beta=50\%$, $\sigma=100 \text{ ns}$

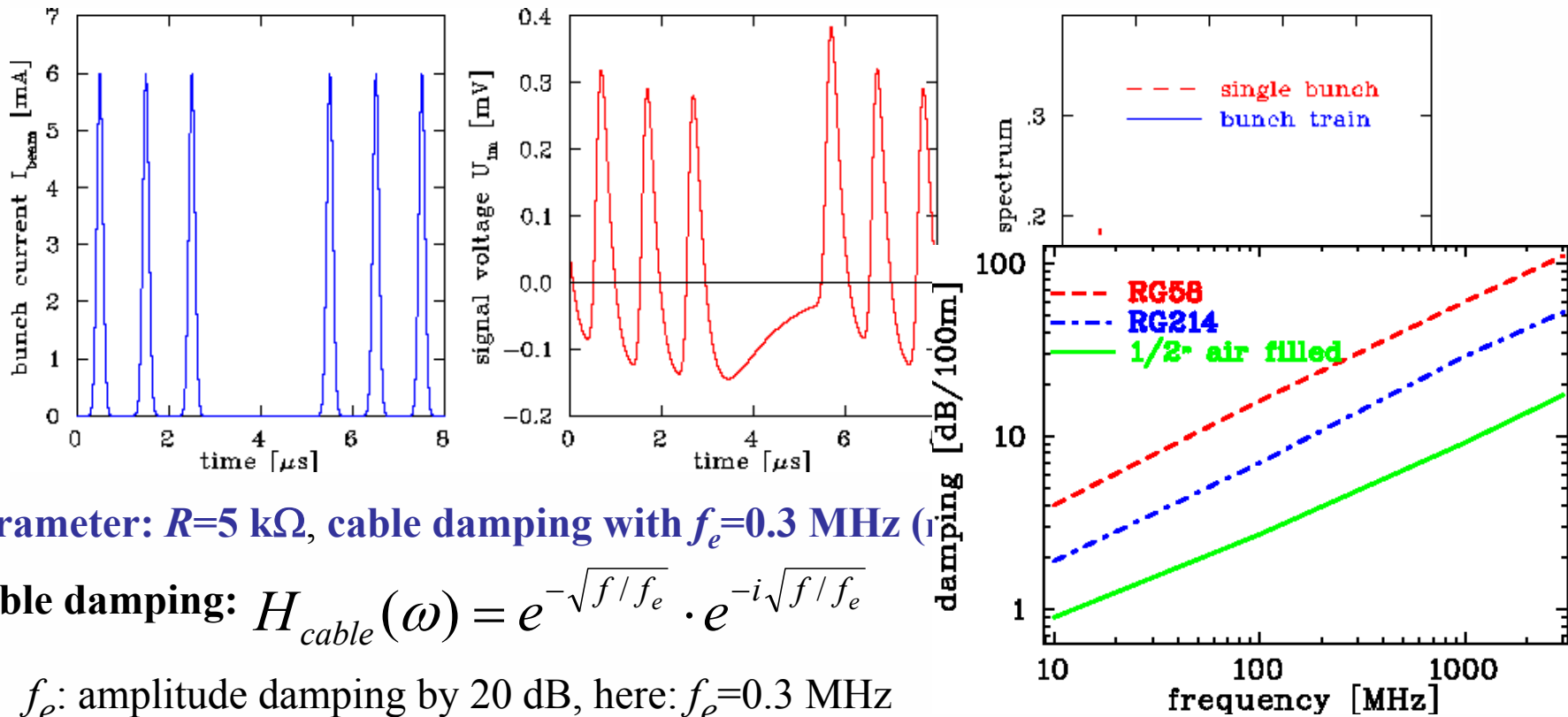
- Fourier spectrum is more complex, harmonics are broader
- Varying baseline with $\tau \approx (3f_{\text{cut}})^{-1} = 1 \mu\text{s}$
- Baseline shift calls for dedicated restoring algorithm for time domain processing.



Calculation of Signal Shape: Bunch Train with Cable Damping



Effect of cable or other electronics:



Parameter: $R=5 \text{ k}\Omega$, cable damping with $f_e=0.3 \text{ MHz}$ (i

Cable damping: $H_{cable}(\omega) = e^{-\sqrt{f/f_e}} \cdot e^{-i\sqrt{f/f_e}}$

f_e : amplitude damping by 20 dB, here: $f_e=0.3 \text{ MHz}$

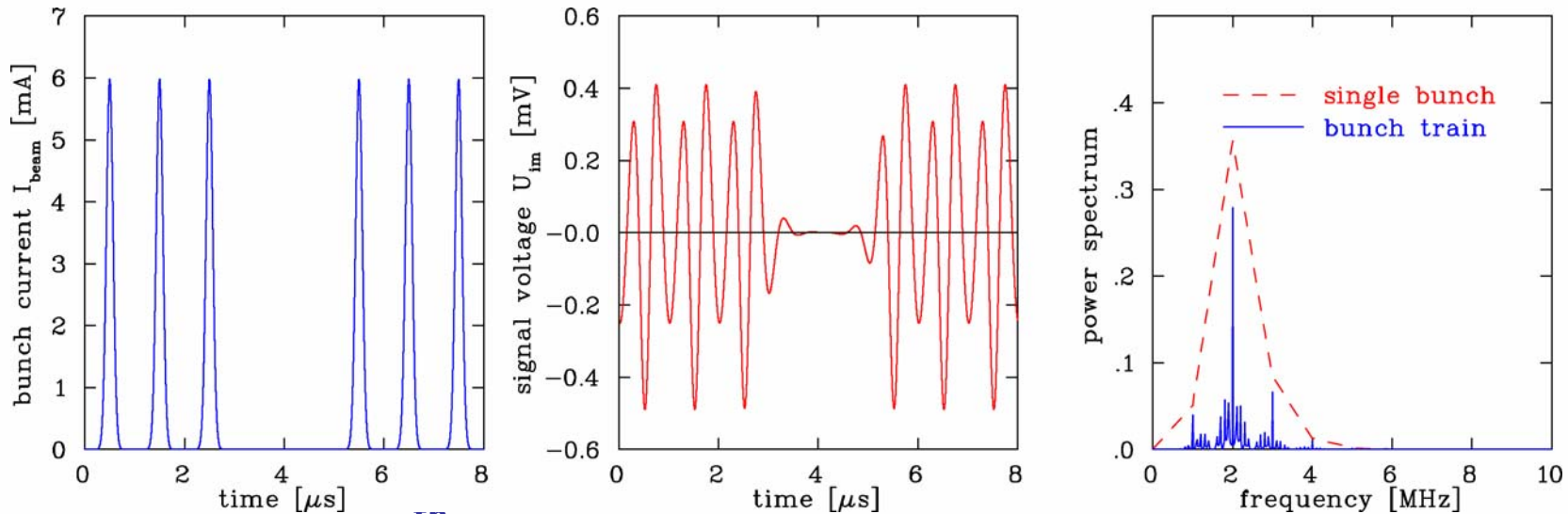
- Bunch signal is damped; 10 fold lower amplitude, higher frequencies are damped stronger
- Bunch signal gets asymmetric, baseline did not reach zero
- \Rightarrow ‘Good cables’ are a precaution for broadband signal transmission



Calculation of Signal Shape: Filtering of Harmonics



Effect of filters, here bandpass:



Parameter: $R=5 \text{ k}\Omega$, 4th order Butterworth filter at $f_{cut}=2 \text{ MHz}$

$C=100\text{pF}$, $l=10\text{cm}$, $\beta=50\%$, $\sigma=100 \text{ ns}$

- Ringing due to sharp cutoff
- Other filter types more appropriate

n^{th} order Butterworth filter, math. simple, but **not** well suited:

$$|H_{low}| = \frac{1}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}} \quad \text{and} \quad |H_{high}| = \frac{(\omega / \omega_{cut})^n}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}}$$

$$H_{filter} = H_{high} \cdot H_{low}$$

Generally: $Z_{tot}(\omega) = H_{cable}(\omega) \cdot H_{filter}(\omega) \cdot H_{amp}(\omega) \cdot \dots \cdot Z_t(\omega)$

Remark: For electronics calculation, time domain filters (FIR and IIR) are more appropriate



Principle of Position Determination with BPM

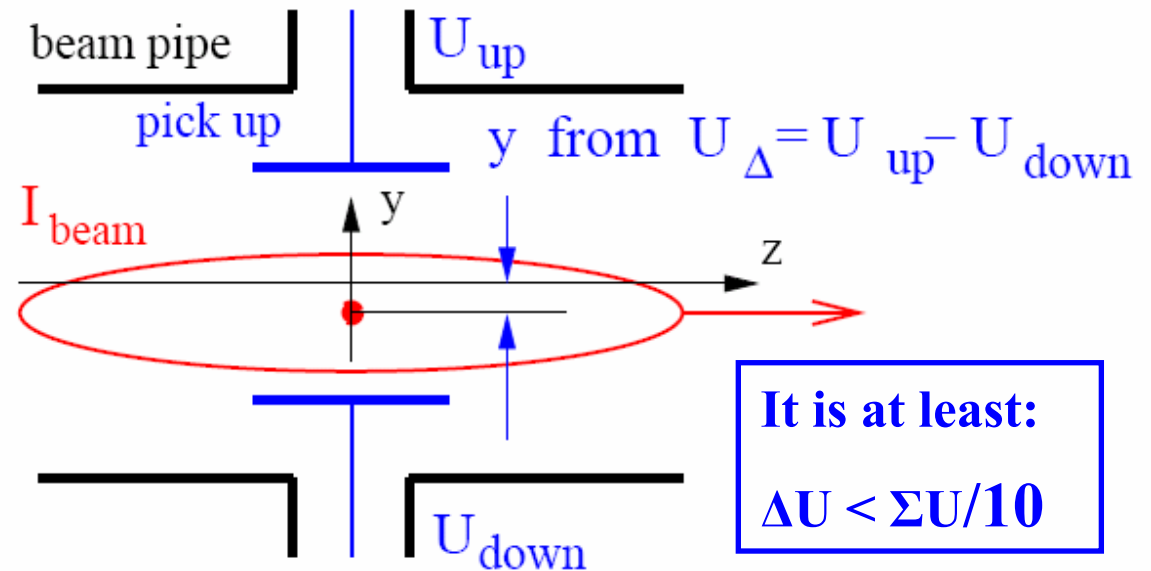
The difference between plates gives the beam's center-of-mass
 → **most frequent application**

'Proximity' effect leads to different voltages at the plates:

$$y = \frac{1}{S_y(\omega)} \cdot \frac{U_{up} - U_{down}}{U_{up} + U_{down}} + \delta_y(\omega)$$

$$\equiv \frac{1}{S_y} \cdot \frac{\Delta U_y}{\Sigma U_y} + \delta_y$$

$$x = \frac{1}{S_x(\omega)} \cdot \frac{U_{right} - U_{left}}{U_{right} + U_{left}} + \delta_x(\omega)$$



$S(\omega, \mathbf{x})$ is called **position sensitivity**, sometimes the inverse is used $k(\omega, \mathbf{x}) = 1/S(\omega, \mathbf{x})$

S is a geometry dependent, non-linear function, which have to be optimized.

Units: $S = [\%/mm]$ and sometimes $S = [dB/mm]$ or $k = [mm]$

Sometimes the transverse transfer impedance is defined via $U_{\Delta} = Z_{\perp}(\omega) \cdot x I_{beam}$

It can be assumed: $Z_{\perp}(\omega, \mathbf{x}) = Z_r(\omega) / S(\omega, \mathbf{x})$



Beam Position Monitor: Detector Principle, Hardware and Electronics

Outline:

- *Signal generation → transfer impedance*
- ***Consideration for capacitive ‘shoe box’ = ‘linear cut’ BPM***
 - position sensitivity calculation, crosstalk, realization***
- *Consideration for capacitive button BPM*
- *Other BPM principles: stripline → traveling wave*
 - inductive → wall current*
 - cavity → resonator for dipole mode*
- *Electronics for position evaluation*
- *Some examples for position evaluation and other applications*
- *Summary*

Shoe-box BPM for Proton or Ion Synchrotron

Frequency range: $1 \text{ MHz} < f_{\text{rf}} < 10 \text{ MHz} \Rightarrow \text{bunch-length} \gg \text{BPM length}$.

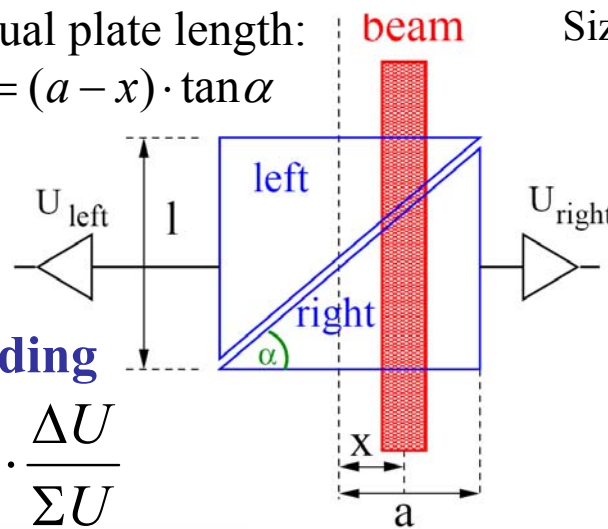
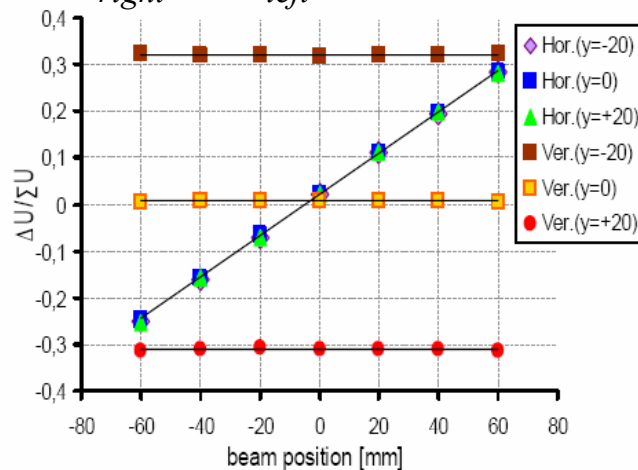
Signal is proportional to actual plate length:

$$l_{\text{right}} = (a + x) \cdot \tan \alpha, \quad l_{\text{left}} = (a - x) \cdot \tan \alpha$$

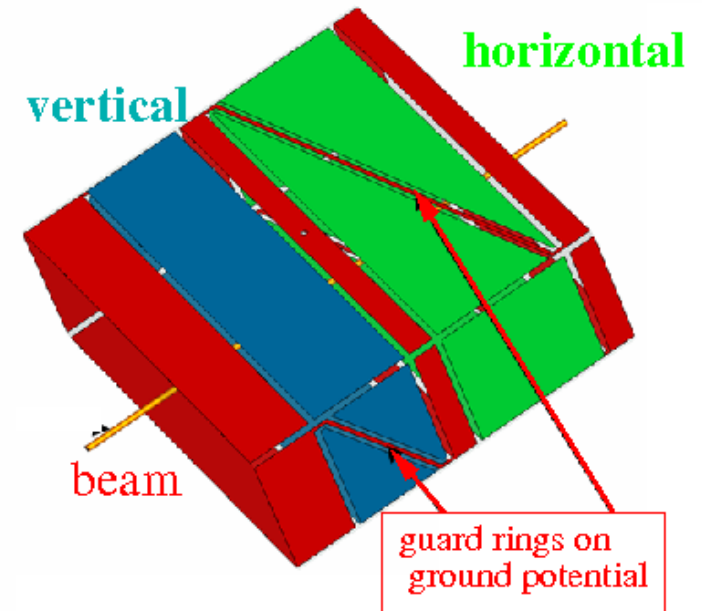
$$\Rightarrow x = a \cdot \frac{l_{\text{right}} - l_{\text{left}}}{l_{\text{right}} + l_{\text{left}}}$$

In ideal case: linear reading

$$x = a \cdot \frac{U_{\text{right}} - U_{\text{left}}}{U_{\text{right}} + U_{\text{left}}} \equiv a \cdot \frac{\Delta U}{\Sigma U}$$



Size: $200 \times 70 \text{ mm}^2$



Shoe-box BPM:

Advantage: Very linear, low frequency dependence
i.e. position sensitivity S is constant

Disadvantage: Large size, complex mechanics
high capacitance

Boundary Contribution \Rightarrow FEM Calculation required



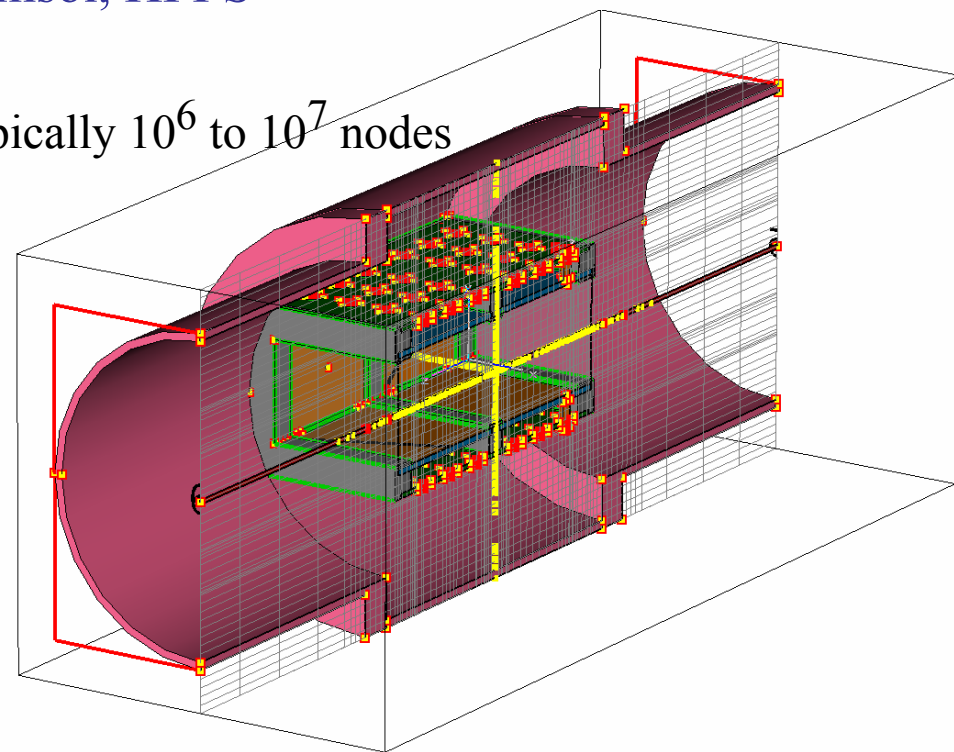
Boundary condition by the environment can significantly influence BPM properties

\Rightarrow real properties have to be calculated numerically by **Finite Element Method**:

Examples are: CST-Studio (MAFIA), Comsol, HFSS

General idea of FEM calculations:

- Volume is divided in 3-dim meshes with typically 10^6 to 10^7 nodes
- The beam is simulated by a traveling wave on a wire
- Goal: Field distribution within the meshes
- The Maxwell equations are solved by iterative matrix inversion
- Time domain: Propagation of source terms (here: Gaussian shaped pulse corresponding to 200 MHz bandwidth)
- Frequency domain: e.g. eigenmodes
- Output: time dependent signal, frequency dependences, S-parameters, field distribution etc.



Meshplane at x= 90 (Index=30)

Optimization of Position Sensitivity

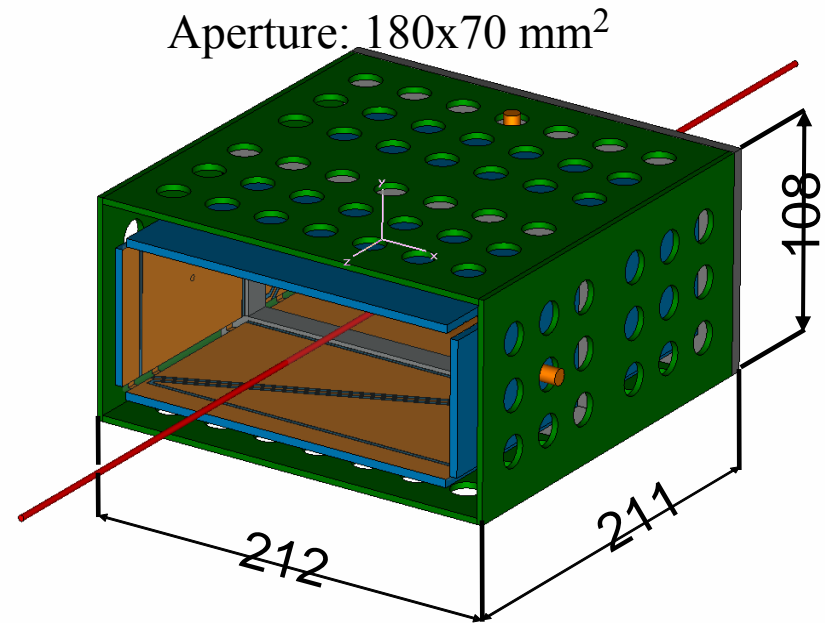
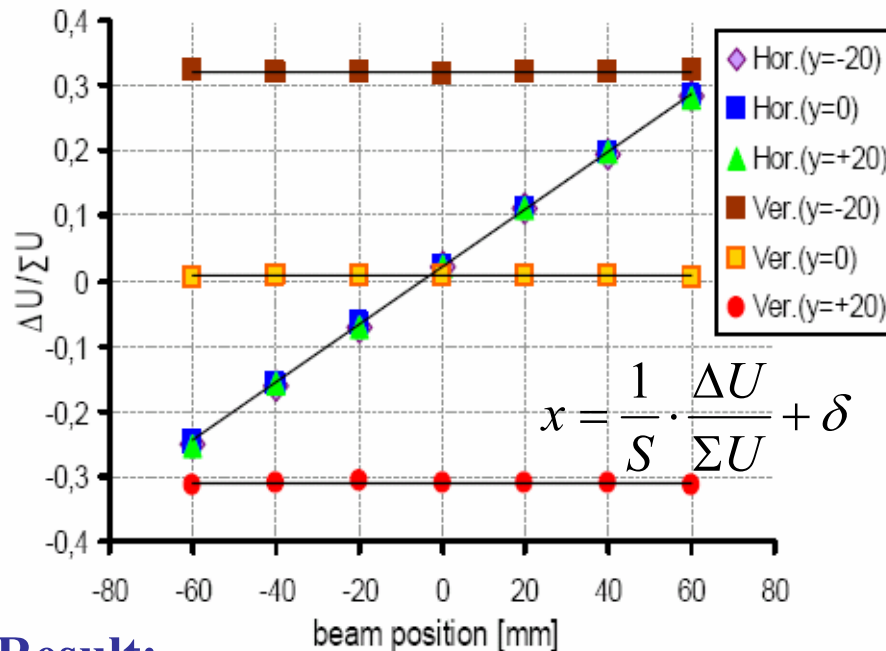


Simulation: Gaussian pulse travels on wire on different positions

→ induced voltage calculated on matched output ports

→ calculation of $\Delta U/\Sigma U$

Criteria of optimization: linearity, sensitivity, offset reduction, x-y plane independence



Result:

Nearly perfect: $S_x=0.96$ %/mm, $\delta_x=-0.4$ mm (ideal value $S_x=1.1$ %/mm, $\delta=0$)

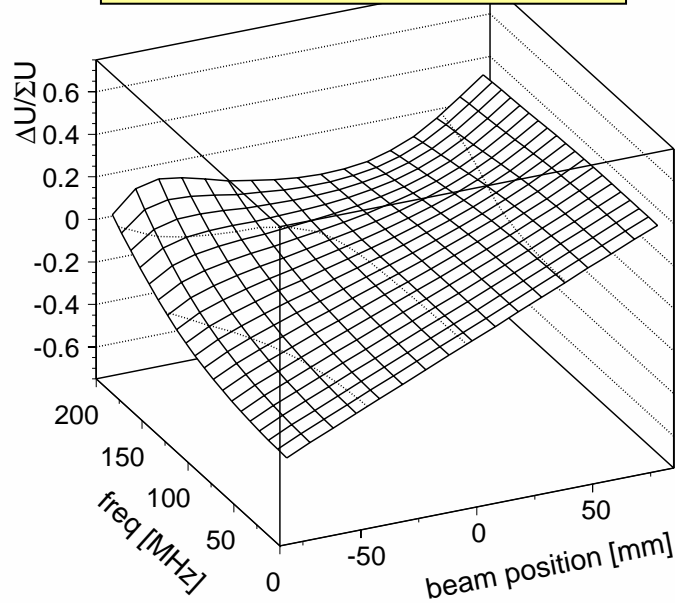
$S_y=2.6$ %/mm, $\delta_y=-0.04$ mm (ideal value $S_y=2.9$ %/mm, $\delta=0$) **at 1 MHz**



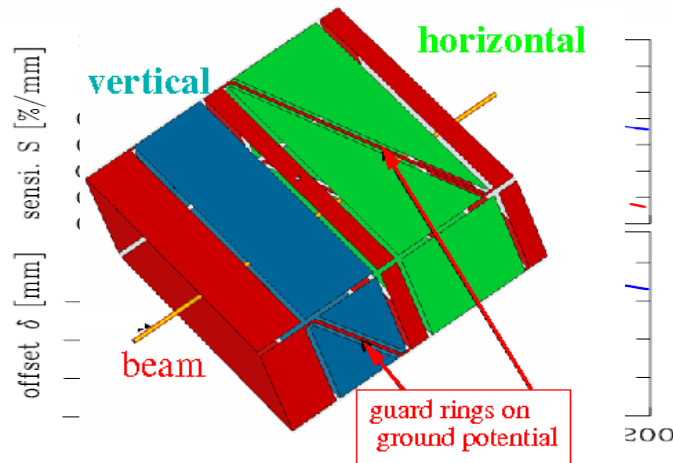
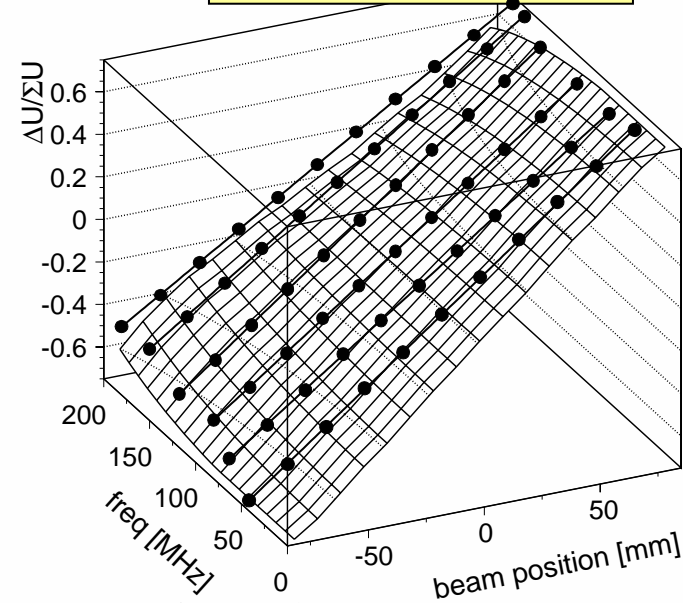
Frequency Dependence of Position Sensitivity



Without guard ring



With guard ring



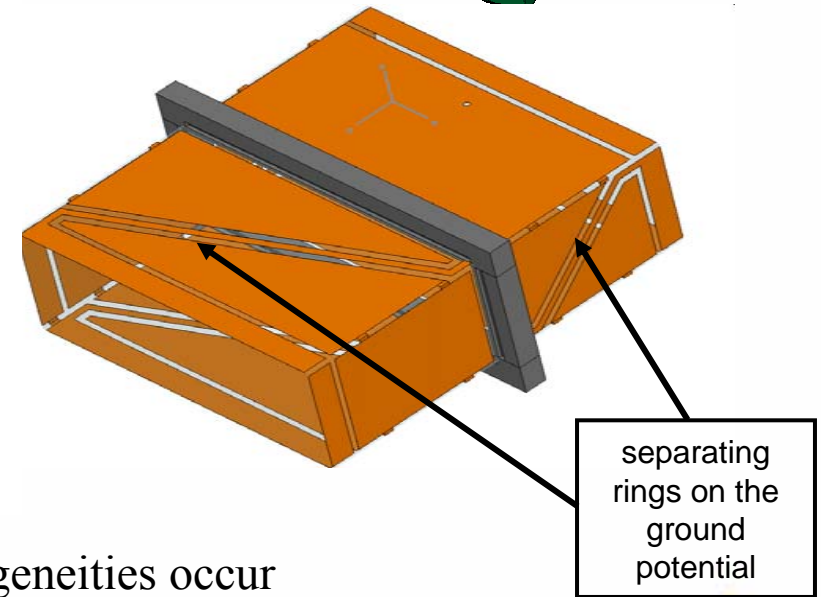
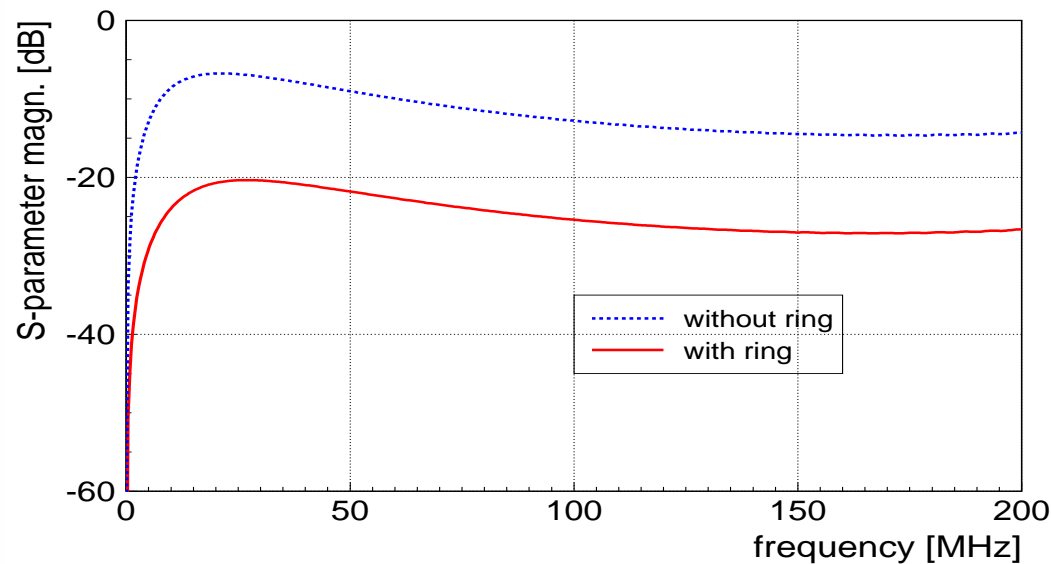
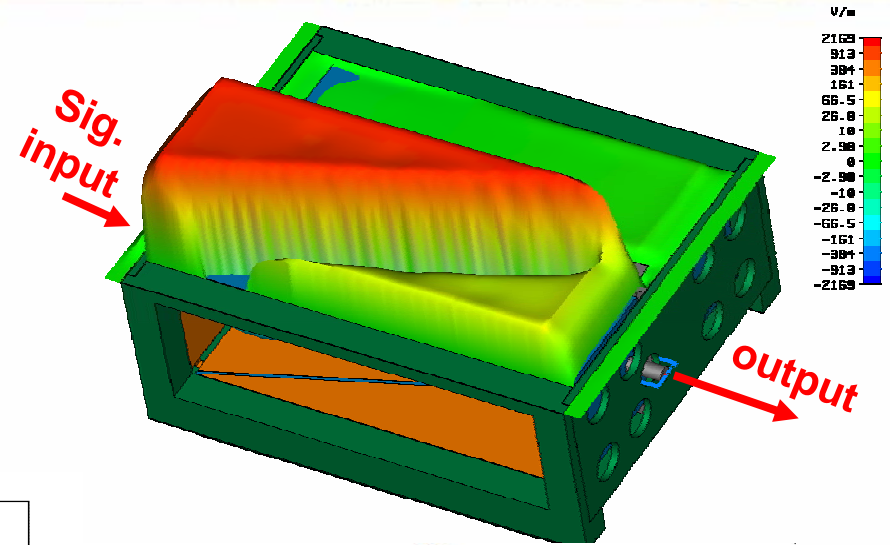
$$x = \frac{1}{S(\omega)} \cdot \frac{\Delta U}{\Sigma U} + \delta(\omega)$$

- Displacement sensitivity is nearly frequency independent only with separating guard rings
- Sensitivity with separating rings is a factor of two larger as without ring.
- Capacitive cross talk spoils the sensitivity

Plate-to-Plate Cross-Talk reduces Sensitivity



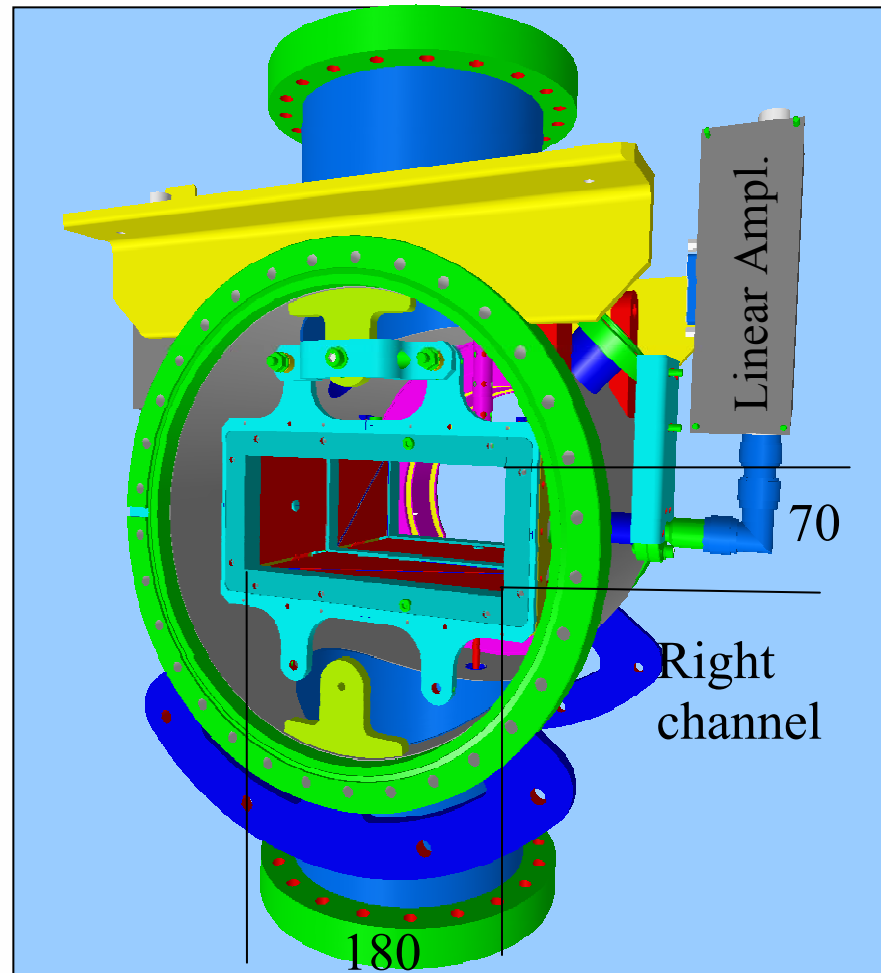
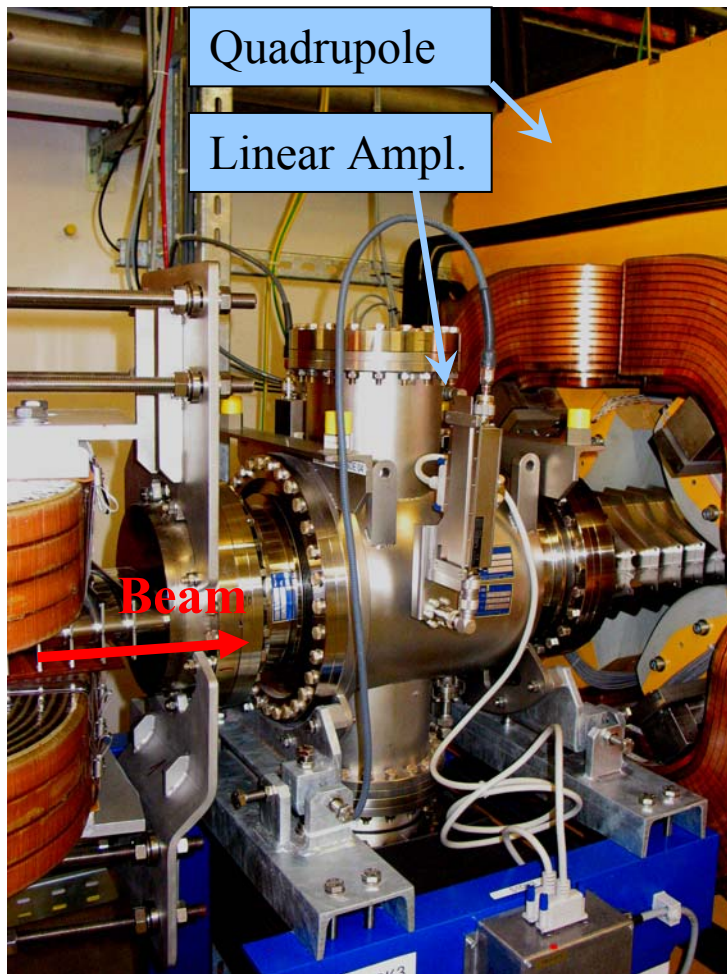
- Capacitive coupling determines position sensitivity
 - Plate-to-plate cross talk caused by ceramic permittivity $\epsilon=9.6$ resulting in high coupling capacitance between adjacent plates
- ⇒ Insertion of the guard-ring between plates reduces cross talks by more than 10dB



Remark: If guard rings are too large: E-field in-homogeneities occur

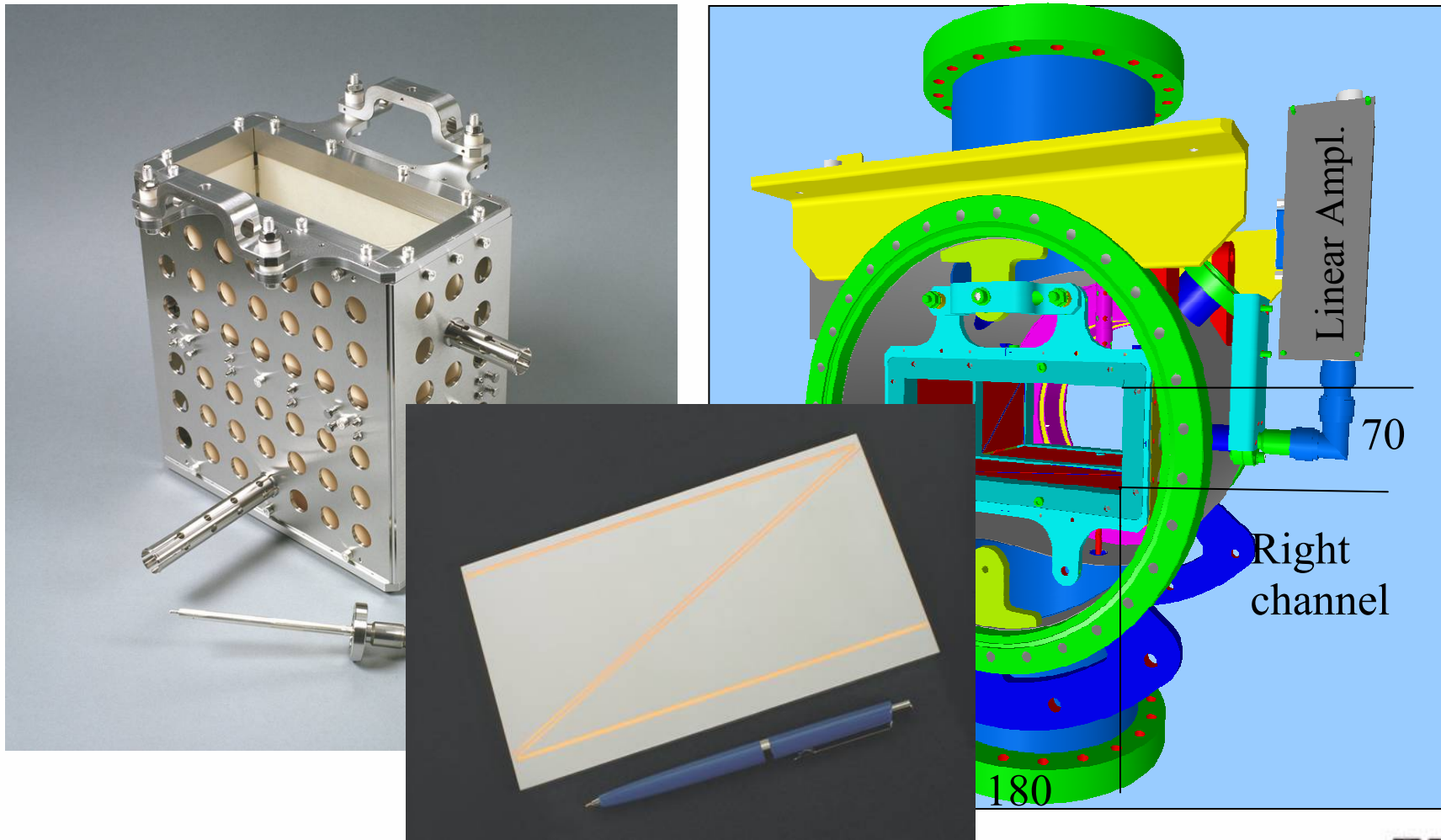
Technical Realization of Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u \rightarrow 440 MeV/u
BPM clearance: 180x70 mm², standard beam pipe diameter: 200 mm.



Technical Realization of Shoe-Box BPM

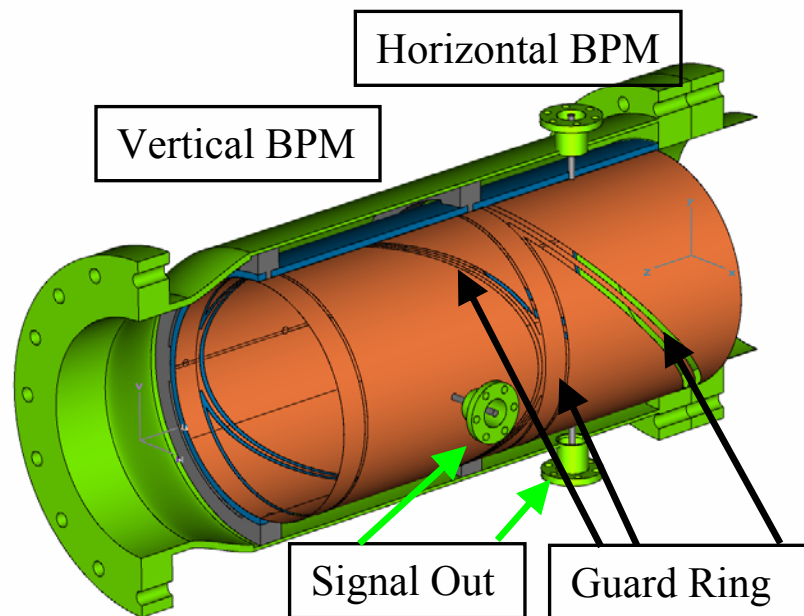
Technical realization at HIT synchrotron of 46 m length for 7 MeV/u \rightarrow 440 MeV/u
BPM clearance: 180x70 mm², standard beam pipe diameter: 200 mm.



Other Types of diagonal cut BPM

Round type: cut cylinder

Same properties as shoe-box:



Other realization: Full metal plates

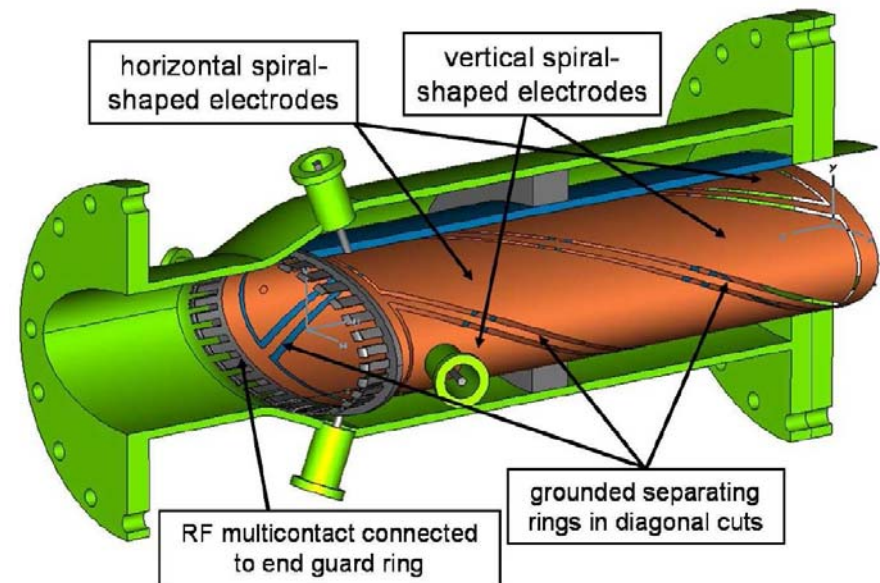
→ No guard rings required

→ but mechanical alignment more difficult

Wounded strips:

Same distance from beam and capacitance for all plates

But horizontal-vertical coupling.





Beam Position Monitor: Detector Principle, Hardware and Electronics

Outline:

- *Signal generation → transfer impedance*
- *Consideration for capacitive shoe box BPM*
- ***Consideration for capacitive button BPM***
 - simple electro-static model, low β effect, modification for synch. light source*
- Comparison shoe box button BPM***
- *Other BPM principles: stripline → traveling wave, inductive → wall current, cavity → resonator for dipole mode*
- *Electronics for position evaluation*
- *Some examples for position evaluation and other applications*
- *Summary*

Button BPM for short Bunches

LINACs, e-synchrotrons: $100 \text{ MHz} < f_{rf} < 3 \text{ GHz} \rightarrow$ bunch length \approx BPM length

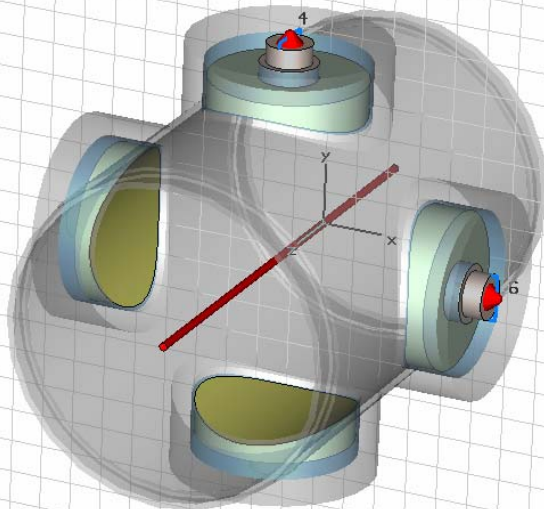
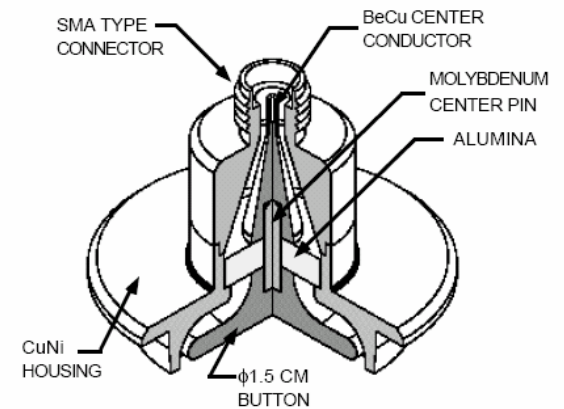
$\rightarrow 50 \Omega$ signal path to prevent reflections

Button BPM with $50 \Omega \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$

Example: LHC-type inside cryostat:

$\varnothing 24 \text{ mm}$, half aperture $a=25 \text{ mm}$, $C=8 \text{ pF}$

$\Rightarrow f_{cut}=400 \text{ MHz}$, $Z_t = 1.3 \Omega$ above f_{cut}



From C. Boccard (CERN)



2-dim Model for Button BPM

‘Proximity effect’: larger signal for closer plate

Ideal 2-dim case: Cylindrical pipe → image current density via ‘image charge method’ for ‘pensile’ beam:

$$j_{im}(\phi) = \frac{I_{beam}}{2\pi a} \cdot \left(\frac{a^2 - r^2}{a^2 + r^2 - 2ar \cdot \cos(\phi - \theta)} \right)$$

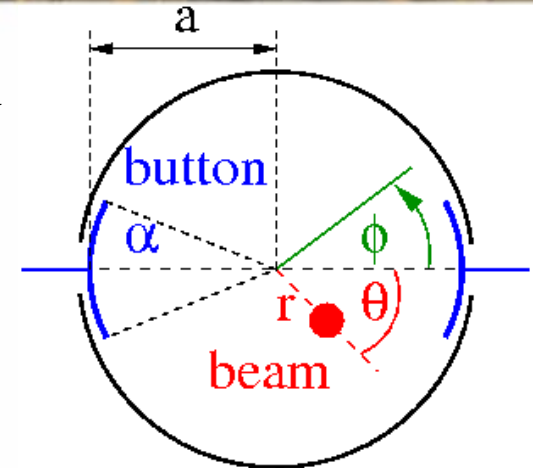
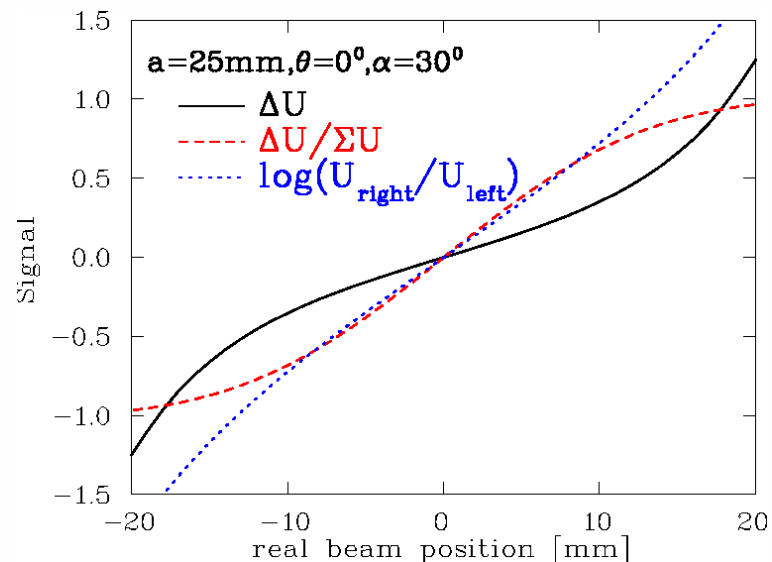
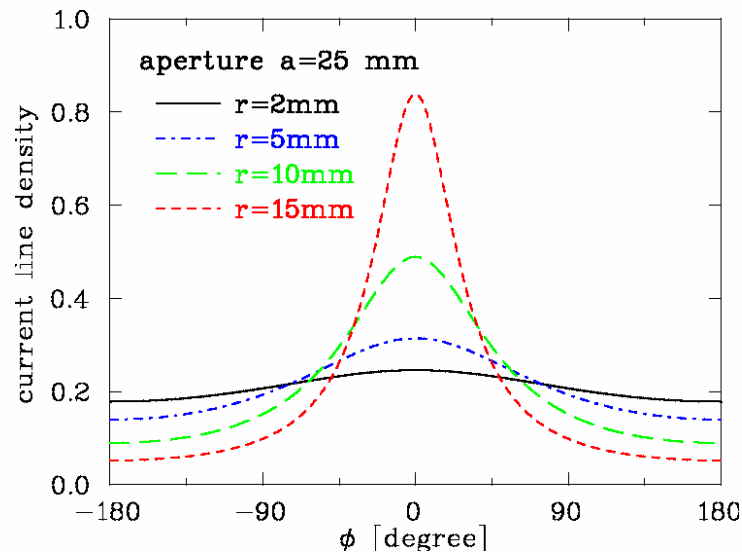


Image current: Integration of finite BPM size: $I_{im} = a \cdot \int_{-\alpha/2}^{\alpha/2} j_{im}(\phi) d\phi$

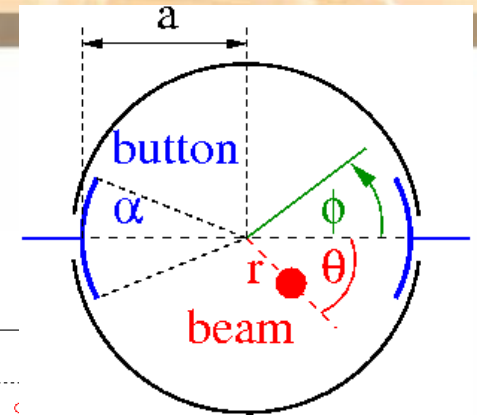
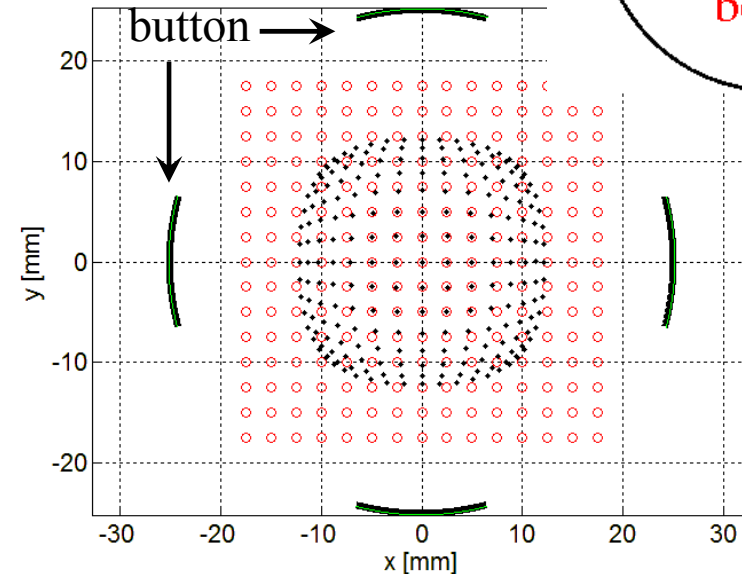
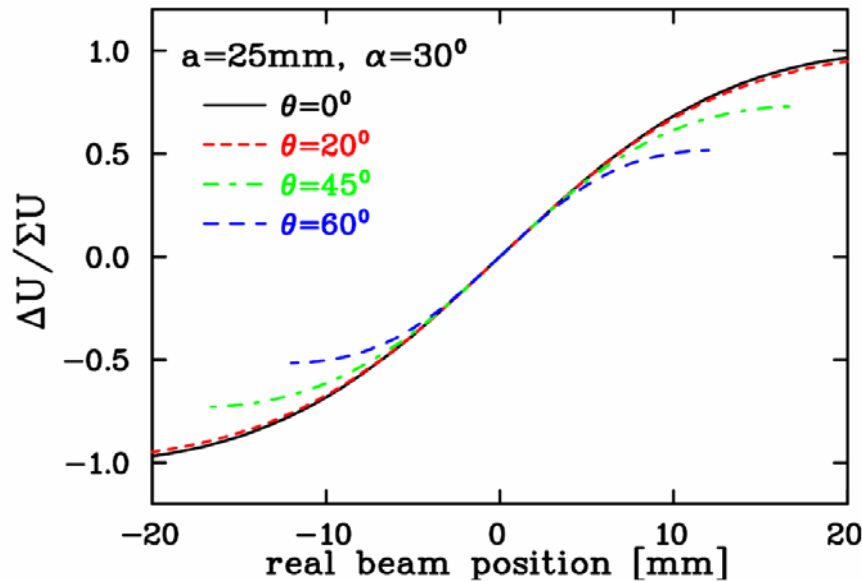


2-dim Model for Button BPM

Ideal 2-dim model: Non-linear behavior and hor-vert coupling:

Sensitivity: $x=1/S \cdot \Delta U / \Sigma U$ with S [%/mm] or [dB/mm]

For this example: center part $S=7.4\%/mm \Leftrightarrow k=1/S=14mm$



Current density can also be calculated by Laplace equation for Fourier components

$$I_{beam} = \langle I_{beam} \rangle + 2 \langle I_{beam} \rangle \cdot \sum_{n=1}^{\infty} A_n \cos(n\omega_0 t) \quad \text{for Gaussian bunches: } A_n = \exp(-n^2 \omega^2 \sigma_t^2 / 2)$$

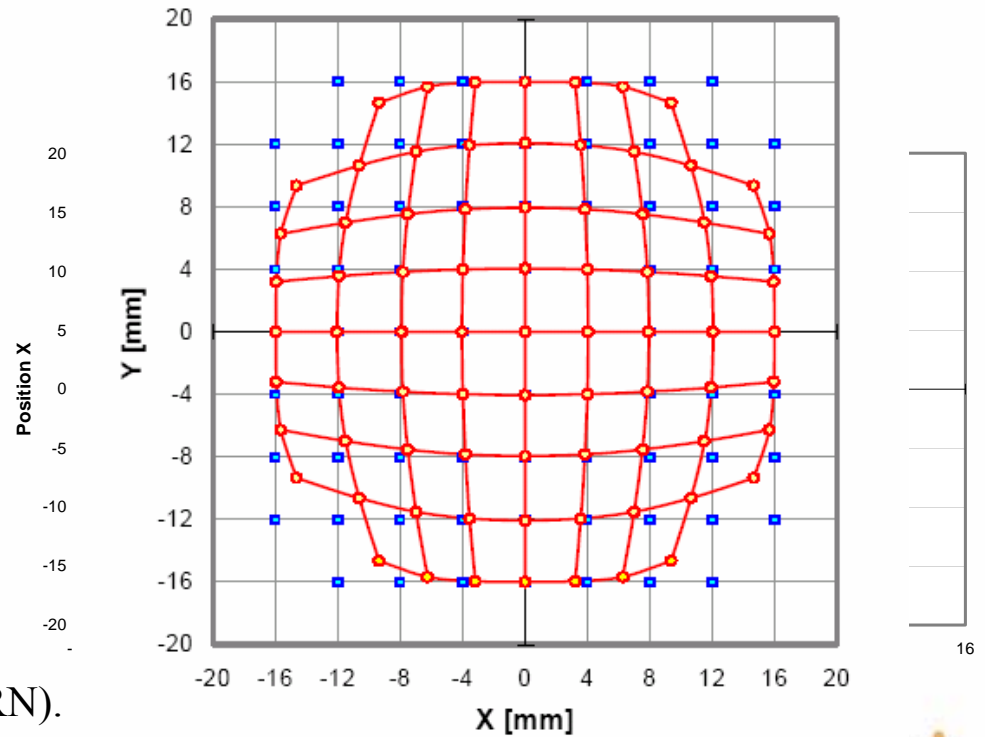
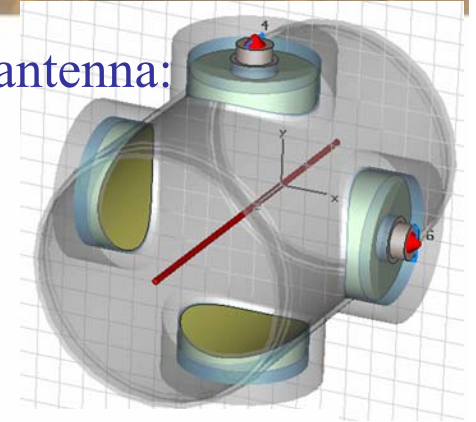
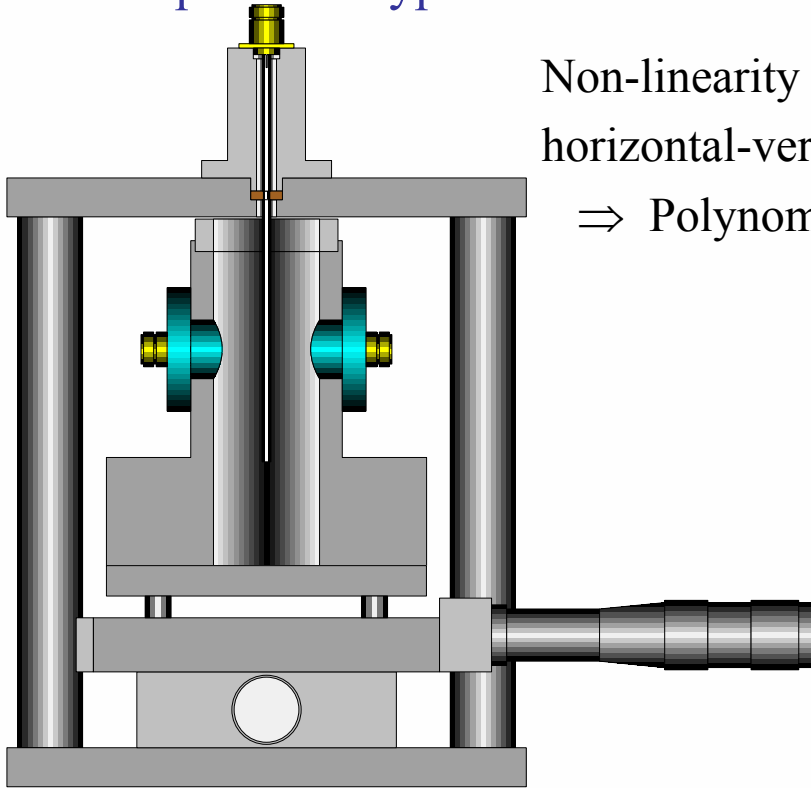
In addition, frequency dependence can be calculated by this method.

Position Measurement for Button BPM

Example LHC type: Measurement with movable $50\ \Omega$ matched antenna:

Non-linearity and
horizontal-vertical coupling

⇒ Polynomial fit with x and y dependence



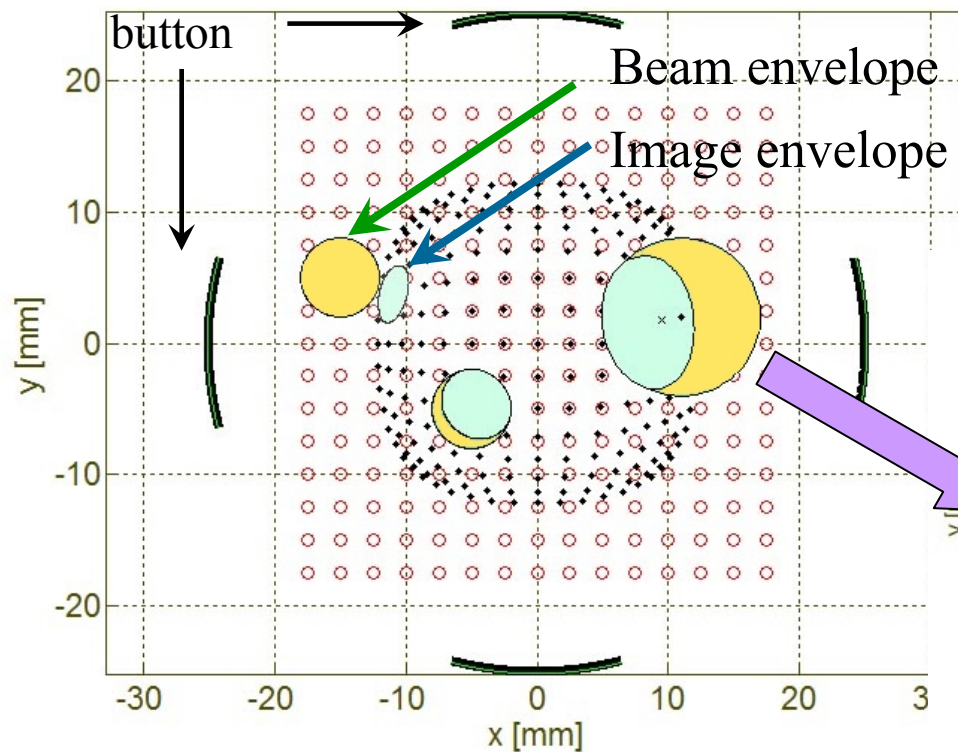
From C. Boccard, C. Palau-Montava et al.(CERN).

Estimation of finite Beam Size Effect for Button BPM



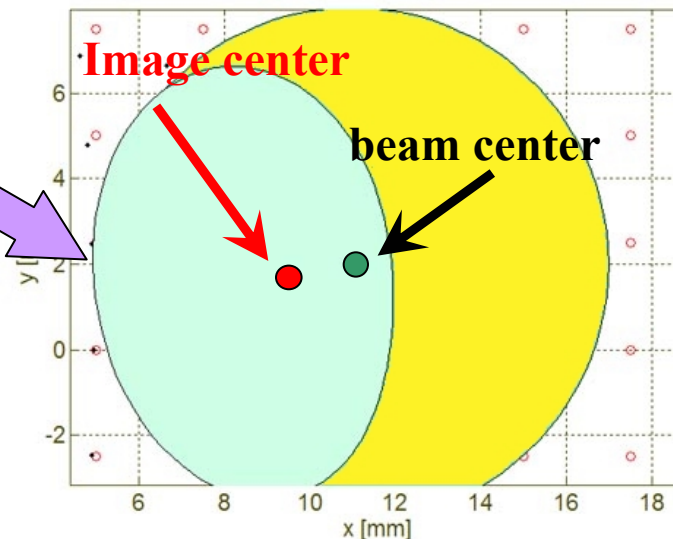
Ideal 2-dim model:

Due to the non-linearity, the beam size enters in the position reading.



Finite beam size:

- Calculation of signal response at different location
 - ‘Averaging’ of image position
- ⇒ Can not be corrected !



Remark: For most LINACs: Linearity is less important, because beam has to be centered
→ correction as feed-forward for next macro-pulse.

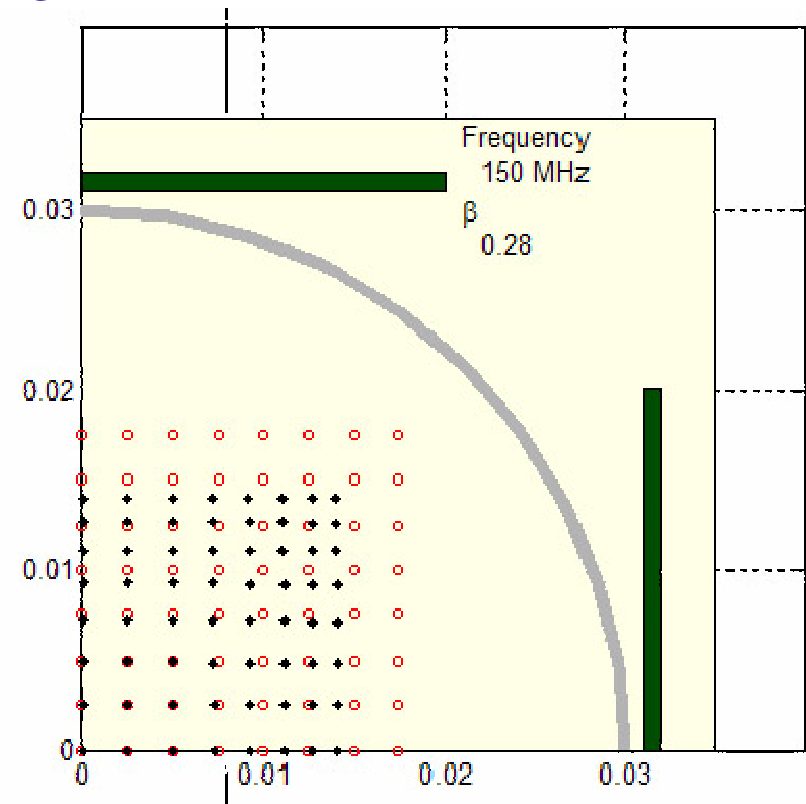
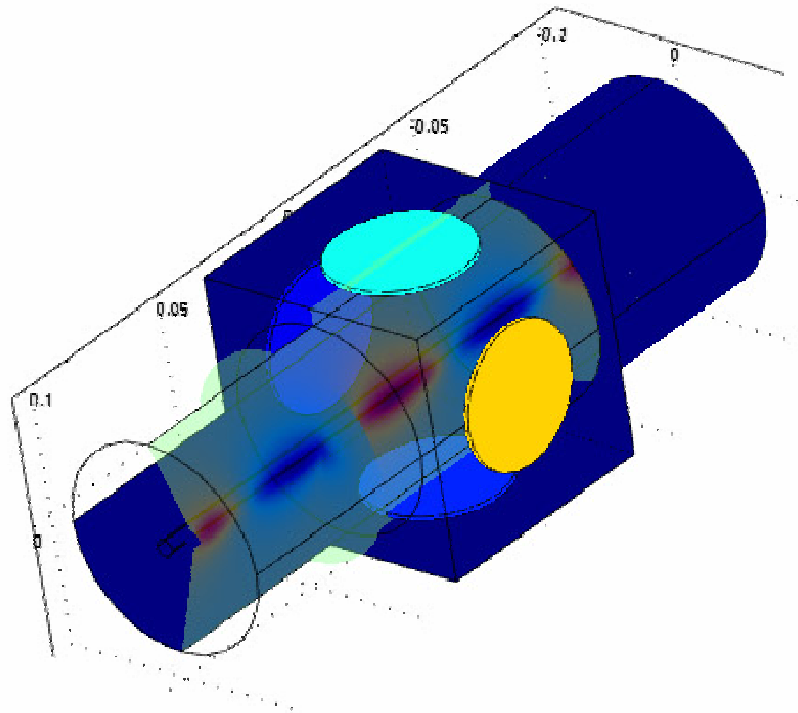


FEM Calculation for Button BPM simple Test Case



For realistic beam, 3-dim FEM calculations are required.

Example: Button BPM at $r=3$ cm beam-pipe, flat, round \varnothing 4cm
frequency $f_{rf}=150$ MHz, effect for higher harmonics calculated



Nearly same result as ideal case!

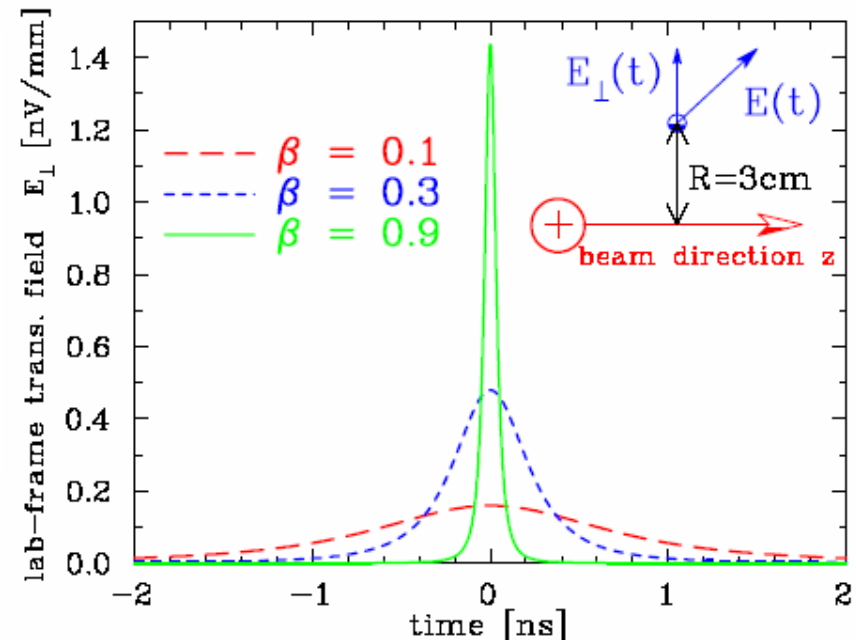
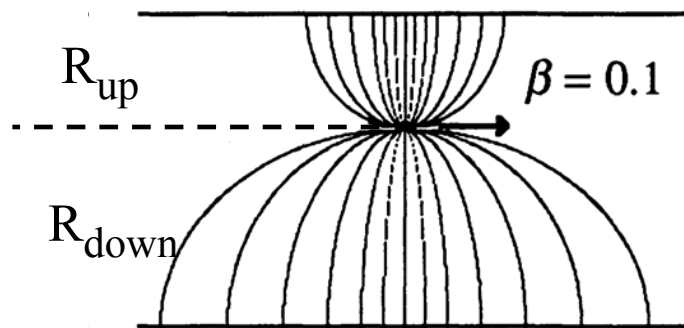


Low Velocity Effect: General Consideration

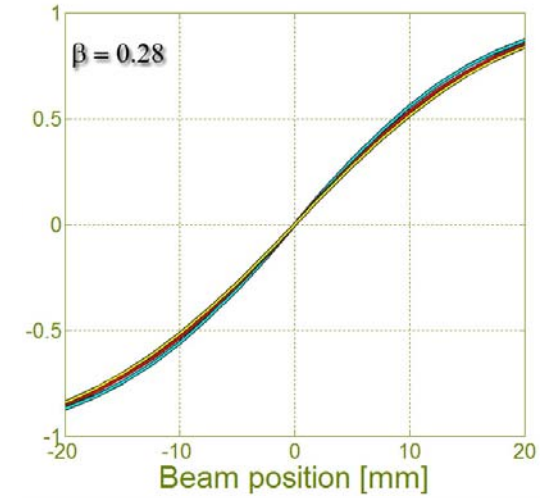
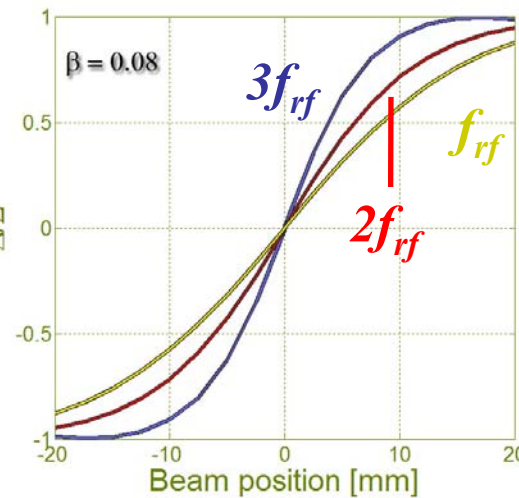
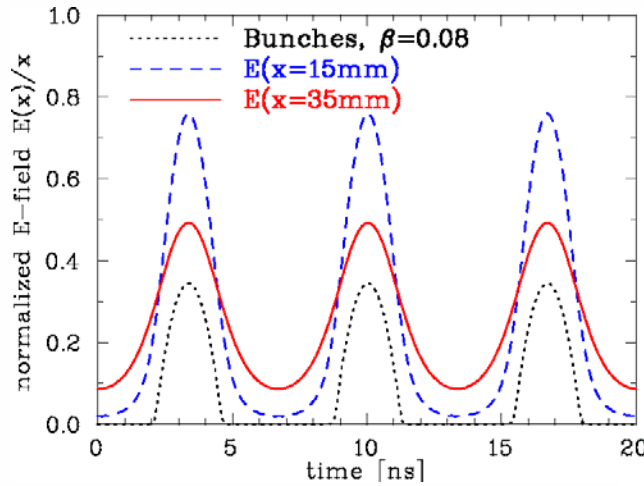
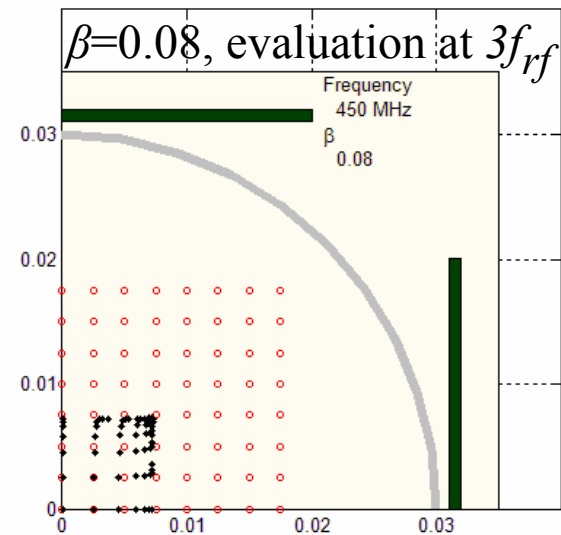
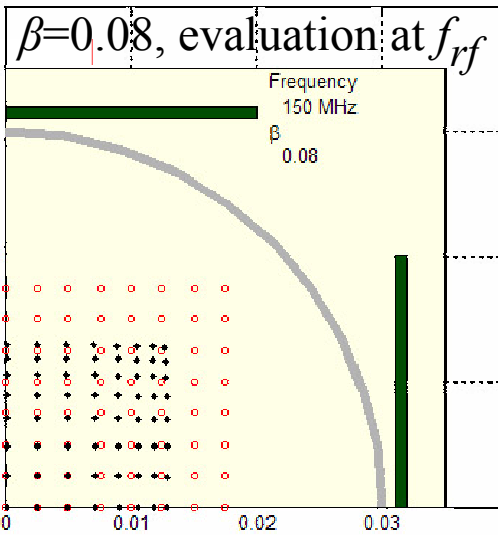
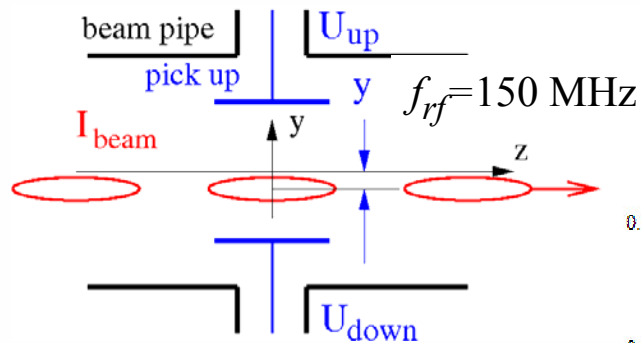
Simple Lorentz transformation of single point-like charge:

Lorentz boost and transformation of time: $E_{\perp}(t) = \gamma E'(t')$ and $t \rightarrow t'$

E-field of a point-like charge:
$$E_{\perp}(t) = \frac{e}{4\pi\epsilon_0} \cdot \frac{\gamma R}{\left[R^2 + (\gamma\beta ct)^2\right]^{3/2}}$$



FEM Calculation of low β Effect for p-LINAC

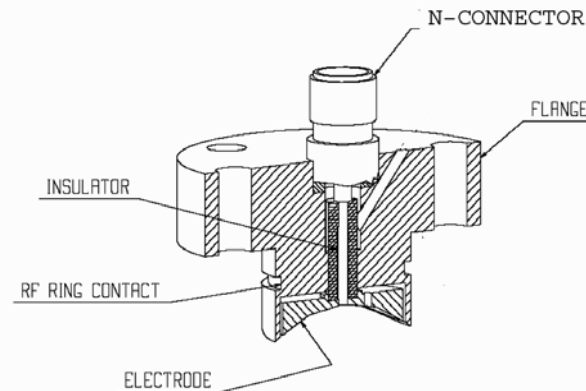
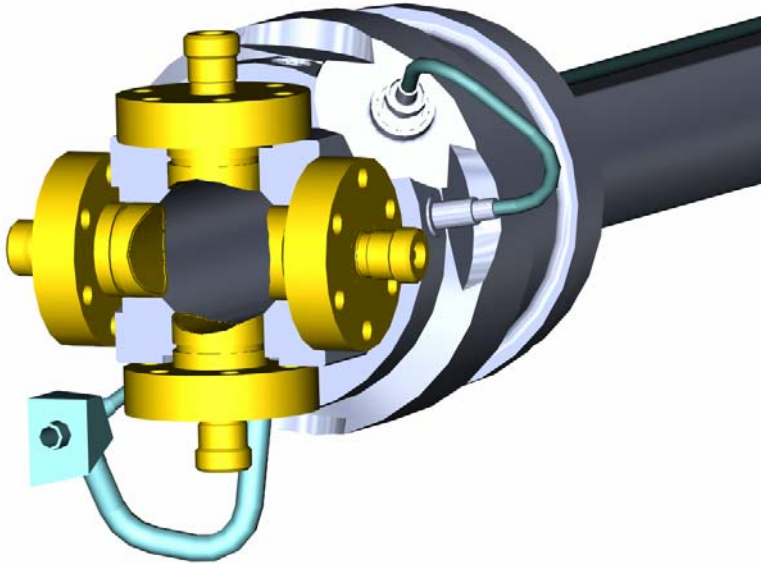


- Effect increases with f_{rf}
- Can also be calculated by Fourier-components.

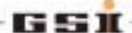


Realization of Button BPM at LHC

Example LHC: \varnothing 24 mm, half aperture $a=25$ mm, installed inside cryostat
Critically: 50Ω matching of button to standard feed-through.



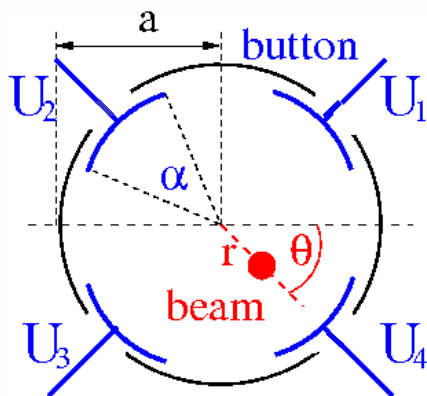
From C. Boccard,
C. Palau-Montava et al.(CERN).



Button BPM at Synchrotron Light Sources



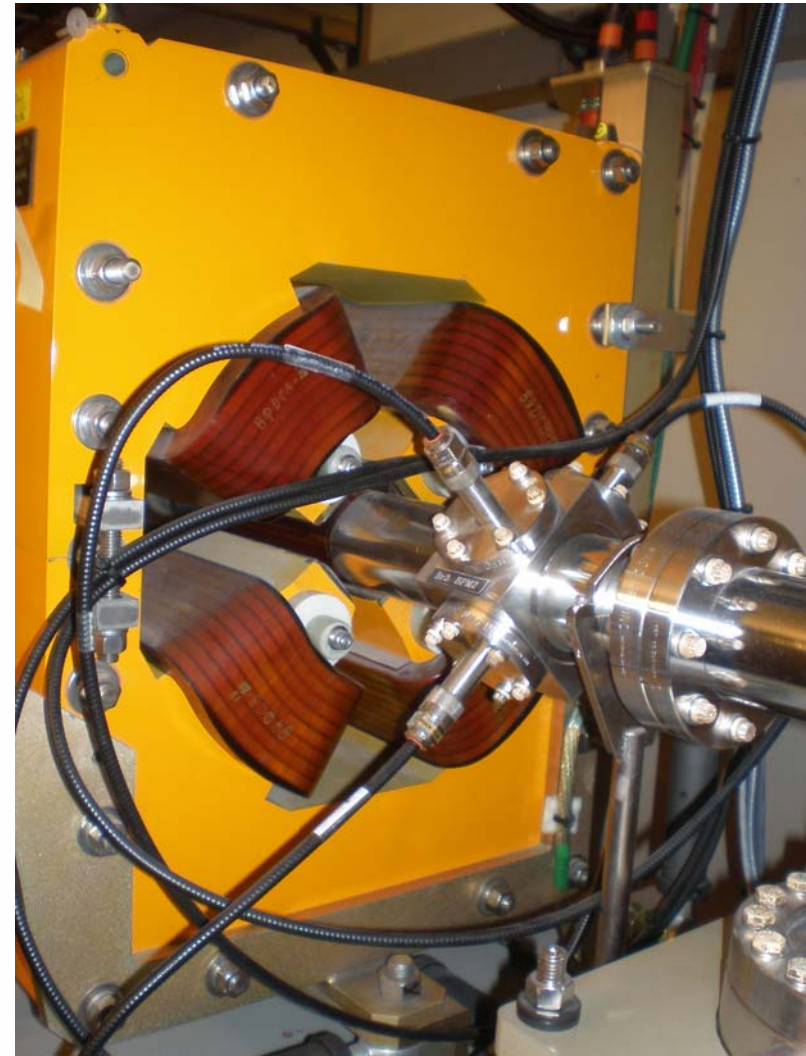
The button BPM can be rotated by 45° to avoid exposure by synchrotron light:
Frequently used at boosters for light sources



$$\text{horizontal: } x = \frac{1}{S} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

$$\text{vertical: } y = \frac{1}{S} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

Example: Booster of ALS, Berkeley



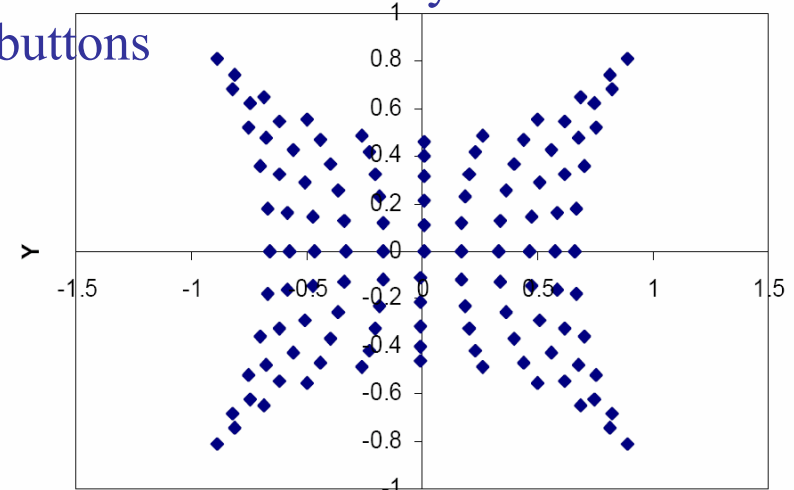
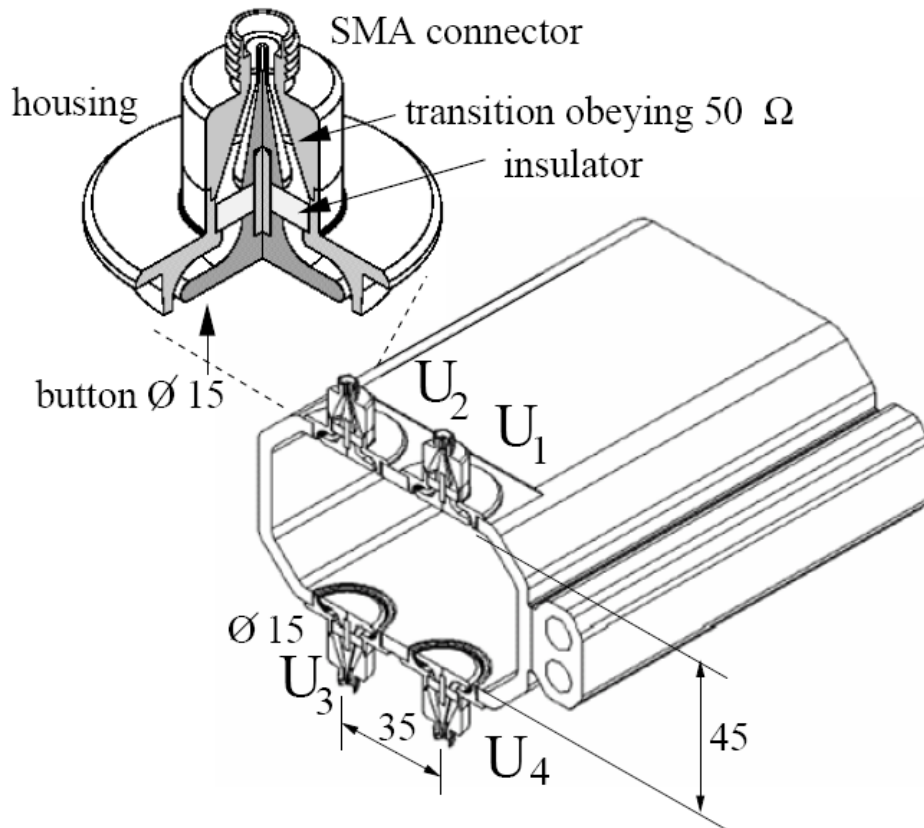
GSI

Button BPM at Synchrotron Light Sources



Due to synchrotron radiation, the button insulation might be destroyed
 ⇒ buttons only in vertical plane possible ⇒ increased non-linearity

Optimization: horizontal distance and size of buttons

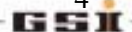


- Beam position swept with 2 mm steps
- Non-linear sensitivity and hor.-vert. coupling
- At center $S_x = 8.5\%/mm$ in this case

$$\text{horizontal : } x = \frac{1}{S_x} \cdot \frac{(U_2 + U_4) - (U_1 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

$$\text{vertical : } y = \frac{1}{S_y} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

From S. Varnasseri, SESAME, DIPAC 2005

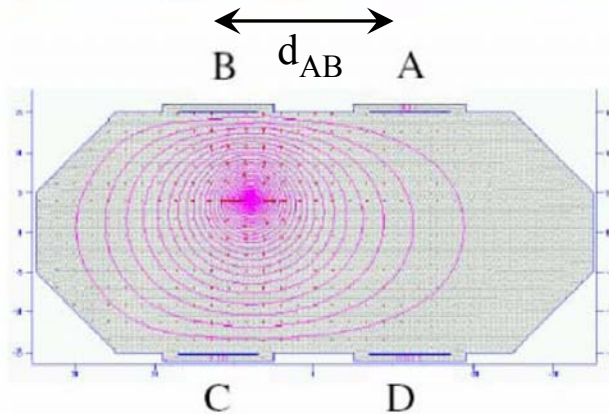
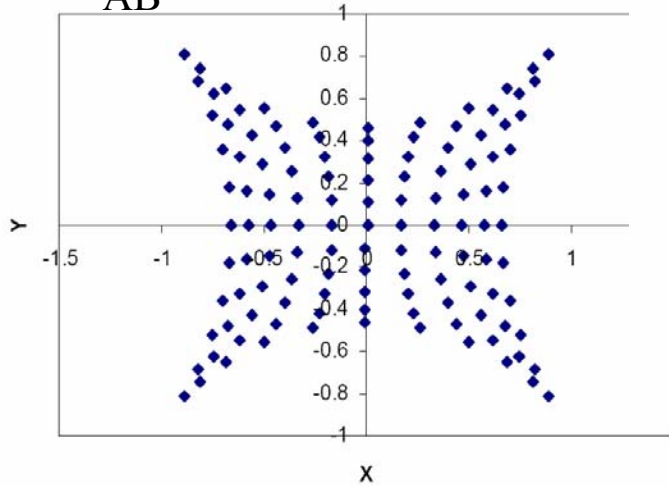


Button BPM at Synchrotron Light Sources



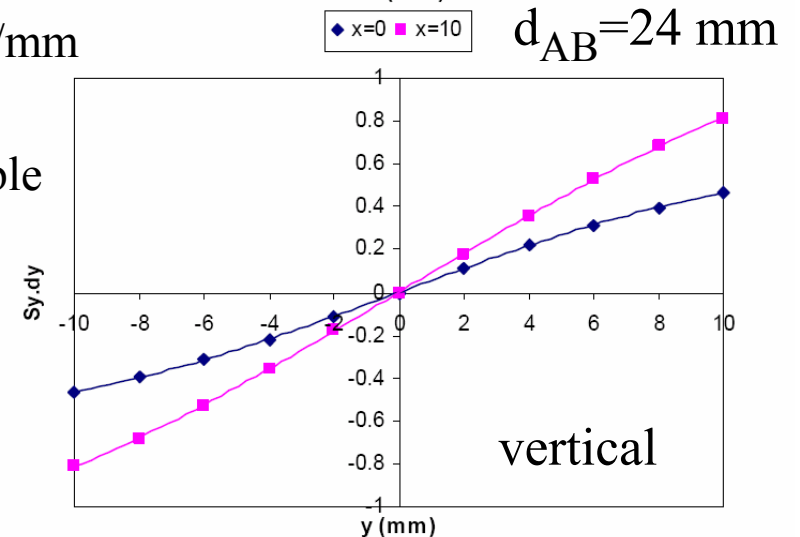
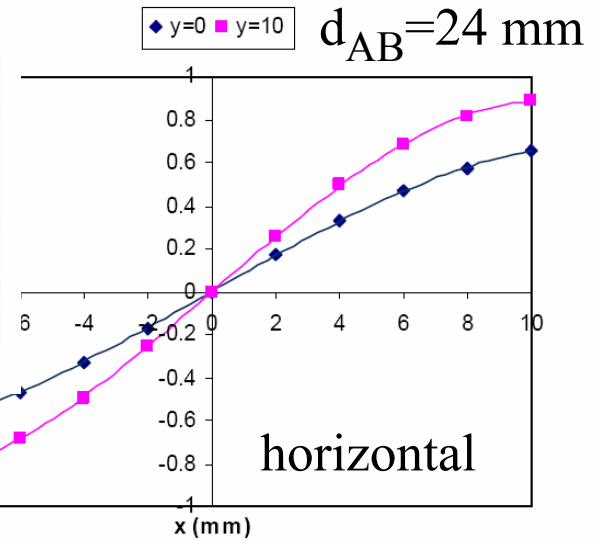
2-dim electro-static simulation:

$d_{AB}=24\text{ mm}$



Result:

- Hori. $S_x=8.5\%/mm$
- Vertical $S_y=5.6\%/mm$
- x&y dependent polynomial fit possible



— Beam position swept with 2 mm steps

P. Forck et al., GSI, February, 2009

From S. Varnasseri, SESAME, DIPAC 2005

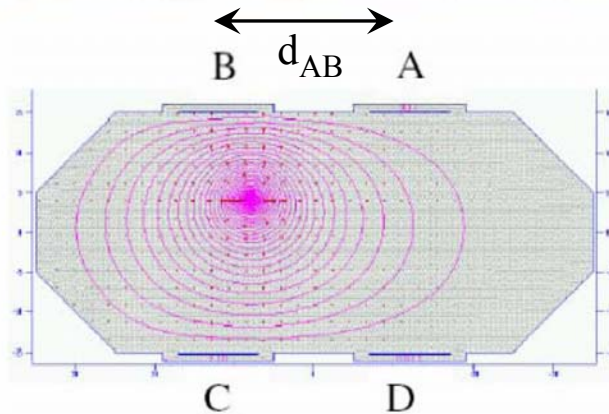
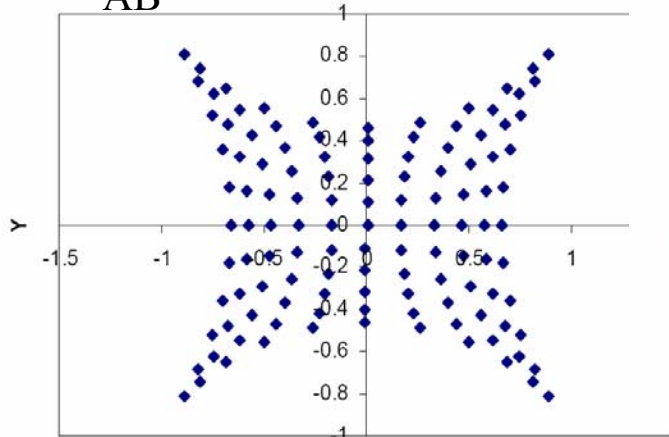
Beam Position Monitors: Principle and Realization

Button BPM at Synchrotron Light Sources



2-dim electro-static simulation:

$d_{AB}=24 \text{ mm}$



Result:

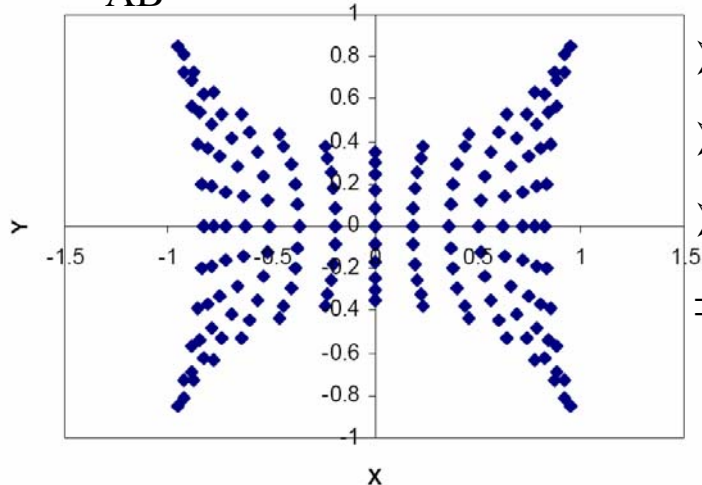
Distance d_{AB} influences the sensitivity

Larger d_{AB} has the effect:

- higher sensitivity in x-direction
- lower sensitivity in y-direction
- linearity in influenced

⇒ Numerical optimization required

$d_{AB}=30 \text{ mm}$



— Beam position swept with 2 mm steps

P. Forck et al., GSI, February, 2009

— From S. Varnasseri, SESAME, DIPAC 2005 —

Beam Position Monitors: Principle and Realization

Comparison Shoe-Box and Button BPM



	Shoe-Box BPM	Button BPM
Precaution	Bunches longer than BPM	Bunch length comparable to BPM
BPM length (typical)	10 to 20 cm length per plane	∅1 to 5 cm per button
Shape	Rectangular or cut cylinder	Orthogonal or planar orientation
Bandwidth (typical)	0.1 to 100 MHz	100 MHz to 5 GHz
Coupling	1 MΩ or ≈1 kΩ (transformer)	50 Ω
Cutoff frequency (typical)	0.01... 10 MHz ($C=30...100\text{pF}$)	0.3... 1 GHz ($C=2...10\text{pF}$)
Linearity	Very good, no x-y coupling	Non-linear, x-y coupling
Sensitivity	Good, care: plate cross talk	Good, care: signal matching
Usage	At proton synchrotrons, $f_{rf} < 10$ MHz	All electron acc., proton Linacs, $f_{rf} > 100$ MHz

