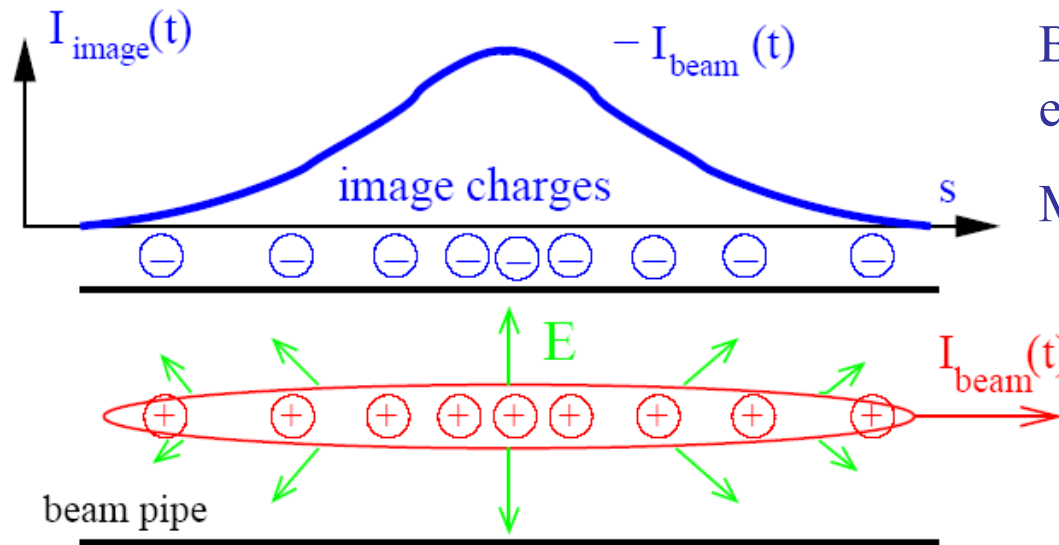


Pick-Ups for bunched Beams



The image current at the beam pipe is monitored on a high frequency basis
i.e. the ac-part given by the bunched beam.



Beam Position Monitor **BPM**
equals Pick-Up **PU**

Most frequent used instrument!

For relativistic velocities,
the electric field is transversal:

$$E_{\perp,lab}(t) = \gamma \cdot E_{\perp,rest}(t')$$

➤ Signal treatment for capacitive pick-ups:

- Longitudinal bunch shape
- Overview of processing electronics for Beam Position Monitor (BPM)

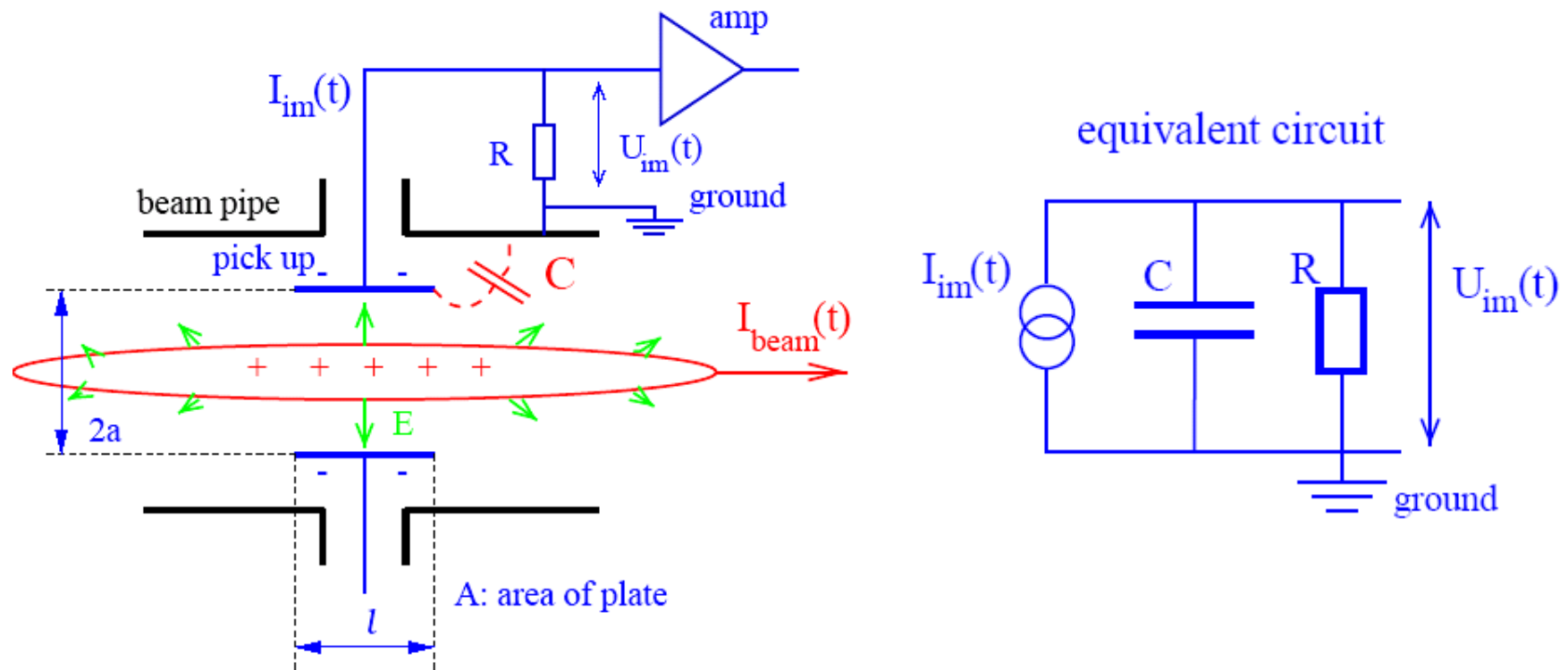
➤ Measurements:

- Closed orbit determination
- Tune and lattice function measurements (synchrotron only).

Model for Signal Treatment of capacitive BPMs



The wall current is monitored by a plate or ring inserted in the beam pipe:



The image current I_{im} at the plate is given by the beam current and geometry:

$$I_{im}(t) = -\frac{dQ_{im}(t)}{dt} = \frac{-A}{2\pi al} \cdot \frac{dQ_{beam}(t)}{dt} = \frac{-A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{dI_{beam}(t)}{dt} = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot i\omega I_{beam}(\omega)$$

Using a relation for Fourier transformation: $I_{beam} = I_0 e^{-i\omega t} \Rightarrow dI_{beam}/dt = -i\omega I_{beam}$

Transfer Impedance for a capacitive BPM



At a resistor R the voltage U_{im} from the image current is measured.

The transfer impedance Z_t is the ratio between voltage U_{im} and beam current I_{beam}

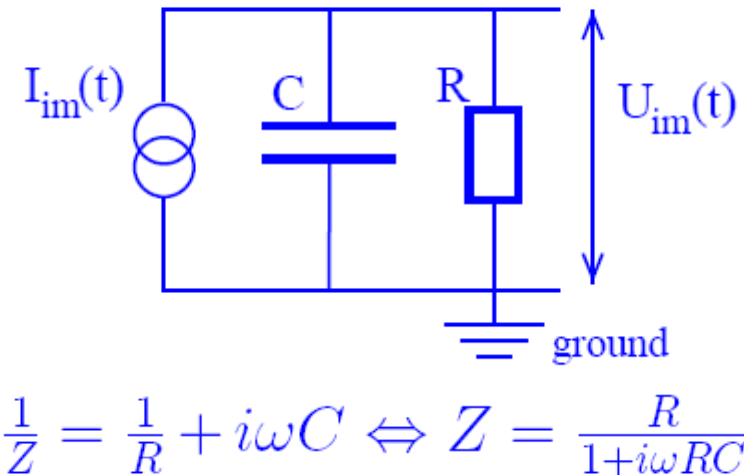
in *frequency domain*: $U_{im}(\omega) = R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega)$.

Capacitive BPM:

- The pick-up capacitance C :
plate \leftrightarrow vacuum-pipe and cable.
- The amplifier with input resistor R .
- The beam is a high-impedance current source:

$$\begin{aligned} U_{im} &= \frac{R}{1+i\omega RC} \cdot I_{im} \\ &= \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{i\omega RC}{1+i\omega RC} \cdot I_{beam} \\ &\equiv Z_t(\omega, \beta) \cdot I_{beam} \end{aligned}$$

equivalent circuit



$$\frac{1}{Z} = \frac{1}{R} + i\omega C \Leftrightarrow Z = \frac{R}{1+i\omega RC}$$

This is a high-pass characteristic with $\omega_{cut} = 1/RC$:

Amplitude: $|Z_t(\omega)| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$ **Phase:** $\varphi(\omega) = \arctan(\omega_{cut} / \omega)$

Example of Transfer Impedance for Proton Synchrotron



The high-pass characteristic for typical synchrotron BPM:

$$U_{im}(\omega) = Z_t(\omega) \cdot I_{beam}(\omega)$$

$$|Z_t| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$$

$$\varphi = \arctan(\omega_{cut} / \omega)$$

Parameter for shoe-box BPM:

$$C = 100 \text{ pF}, l = 10 \text{ cm}, \beta = 50\%$$

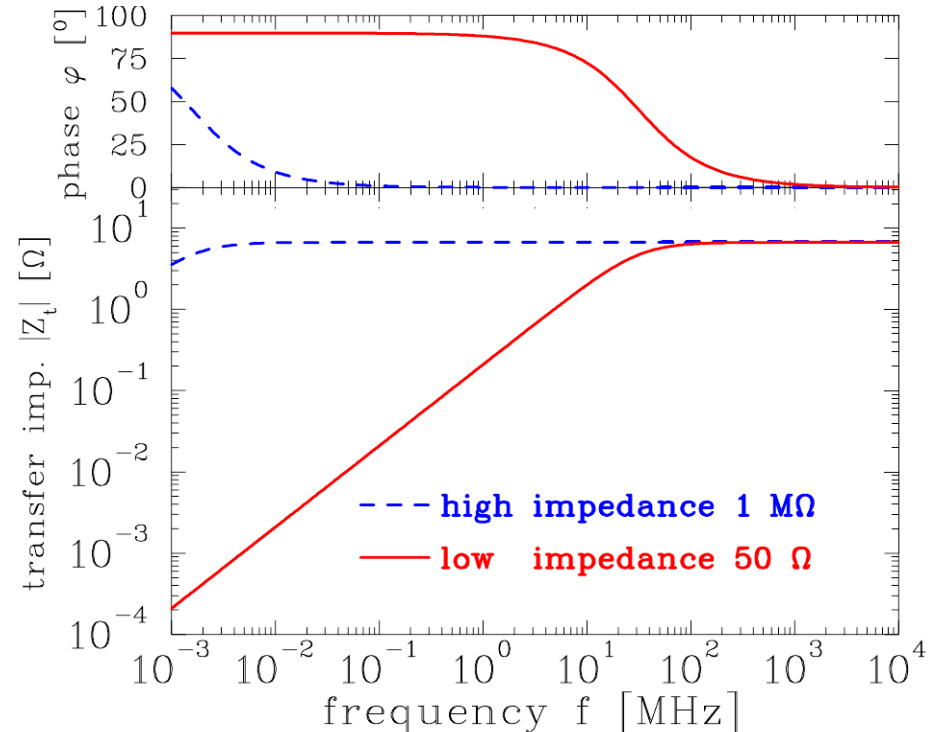
$$f_{cut} = \omega / 2\pi = (2\pi RC)^{-1}$$

$$\text{for } R = 50 \Omega \Rightarrow f_{cut} = 32 \text{ MHz}$$

$$\text{for } R = 1 \text{ M}\Omega \Rightarrow f_{cut} = 1.6 \text{ kHz}$$

Large signal strength → **high impedance**

Smooth signal transmission → **50 Ω**



Signal Shape for capacitive BPMs: differentiated \leftrightarrow proportional



Depending on the frequency range *and* termination the signal looks different:

➤ *High frequency range* $\omega \gg \omega_{cut}$:

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow 1 \Rightarrow U_{im}(t) = \frac{1}{C} \cdot \frac{1}{\beta c} \cdot \frac{A}{2\pi a} \cdot I_{beam}(t)$$

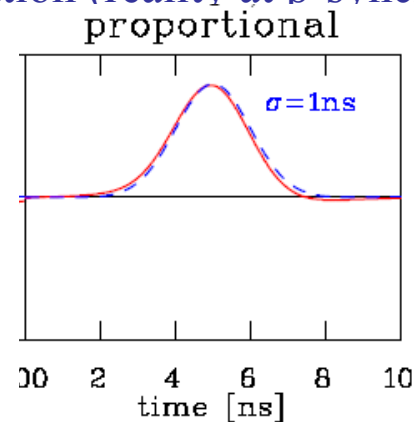
\Rightarrow **direct image** of the bunch. Signal strength $Z_t \propto A/C$ i.e. nearly independent on length

➤ *Low frequency range* $\omega \ll \omega_{cut}$:

$$Z_t \propto \frac{i\omega / \omega_{cut}}{1 + i\omega / \omega_{cut}} \rightarrow i \frac{\omega}{\omega_{cut}} \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot i\omega I_{beam}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$$

\Rightarrow **derivative** of bunch, single strength $Z_t \propto A$, i.e. (nearly) independent on C

Example from synchrotron BPM with 50Ω termination (reality at p-synchrotron : $\sigma \gg 1$ ns):

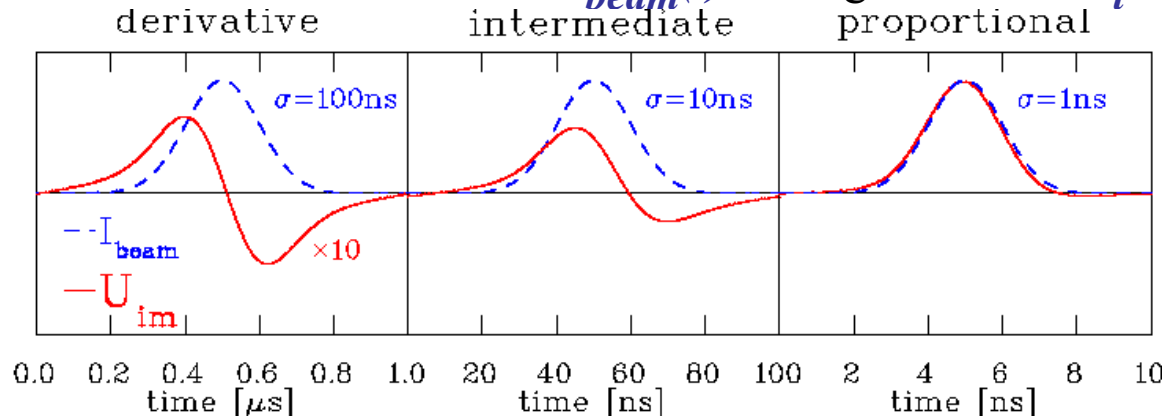


Calculation of Signal Shape (here single bunch)

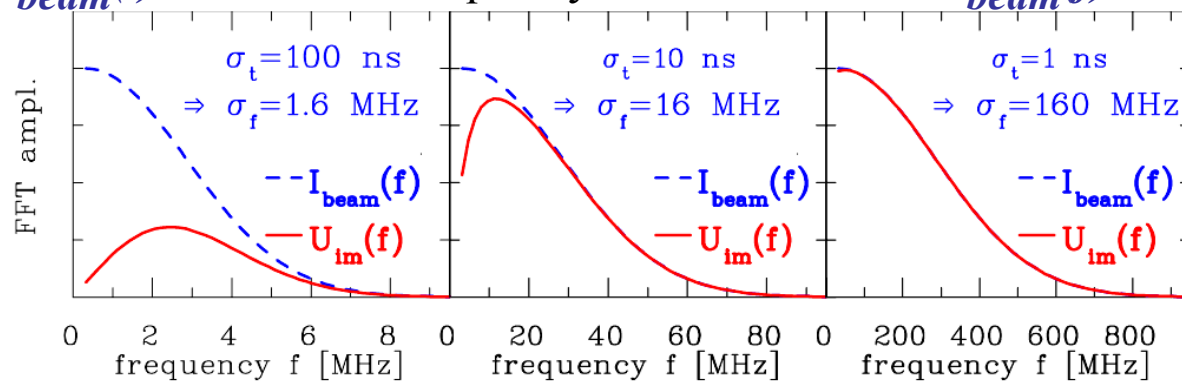


The transfer impedance is used in frequency domain! The following is performed:

- Start:** Time domain Gaussian function $I_{beam}(t)$ having a width of σ_t



- FFT of $I_{beam}(t)$ leads to the frequency domain Gaussian $I_{beam}(f)$ with $\sigma_f=(2\pi\sigma_t)^{-1}$**



- Multiplication with $Z_t(f)$ with $f_{cut}=32\text{ MHz}$ leads to $U_{im}(f) = Z_t(f) \cdot I_{beam}(f)$**

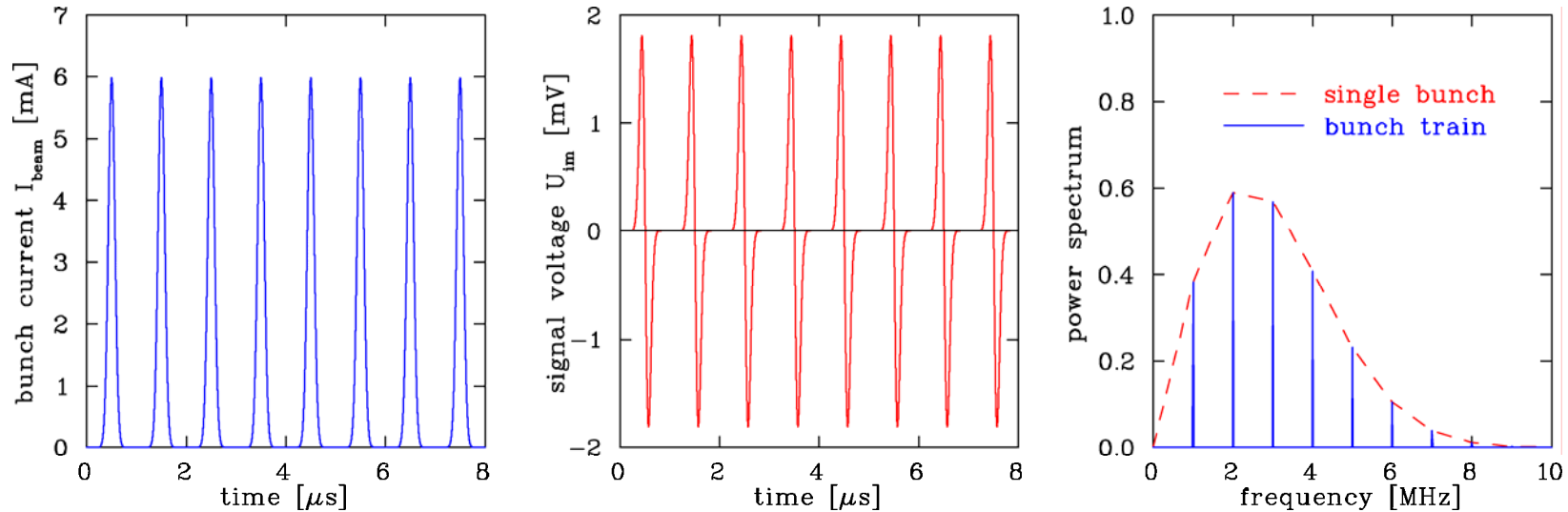
- Inverse FFT leads to $U_{im}(t)$**

Calculation of Signal Shape: repetitive Bunch in a Synchrotron



Synchrotron filled with 8 bunches accelerated with $f_{acc}=1$ MHz

BPM terminated with $R=50 \Omega \Rightarrow f_{acc} \ll f_{cut}$:



Parameter: $R=50 \Omega \Rightarrow f_{cut}=32$ MHz, all buckets filled

$C=100$ pF, $l=10$ cm, $\beta=50\%$, $\sigma_t=100$ ns

- Fourier spectrum is concentrated at acceleration harmonics with single bunch spectrum as an envelope.
- Bandwidth up to typically $10 \cdot f_{acc}$

Examples for differentiated & proportional Shape



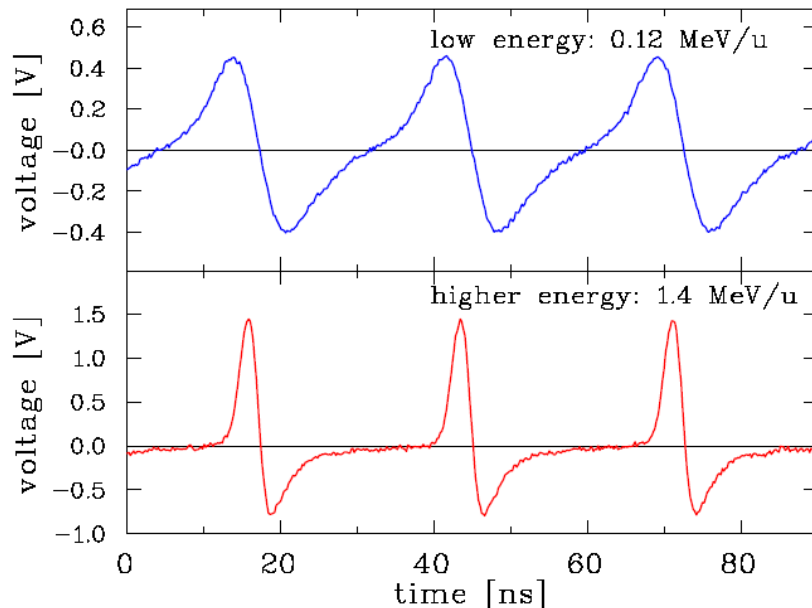
Proton LINAC, e⁻-LINAC & synchrotron:

100 MHz < f_{rf} < 1 GHz typically

$R=50 \Omega$ processing to reach bandwidth

$C \approx 5 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 700 \text{ MHz}$

Example: 36 MHz GSI ion LINAC



Proton synchrotron:

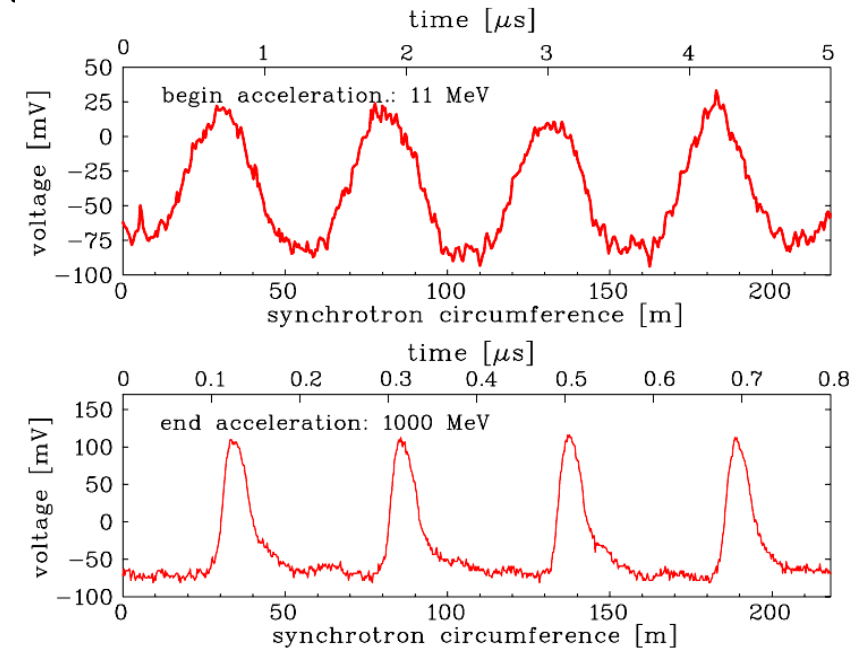
1 MHz < f_{rf} < 30 MHz typically

$R=1 \text{ M}\Omega$ for large signal i.e. large Z_t

$C \approx 100 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 10 \text{ kHz}$

Example: non-relativistic GSI synchrotron

f_{rf} : 0.8 MHz \rightarrow 5 MHz



Remark: During acceleration the bunching-factor is increased: ‘adiabatic damping’.

Pick-Ups at a LINAC for longitudinal Observation

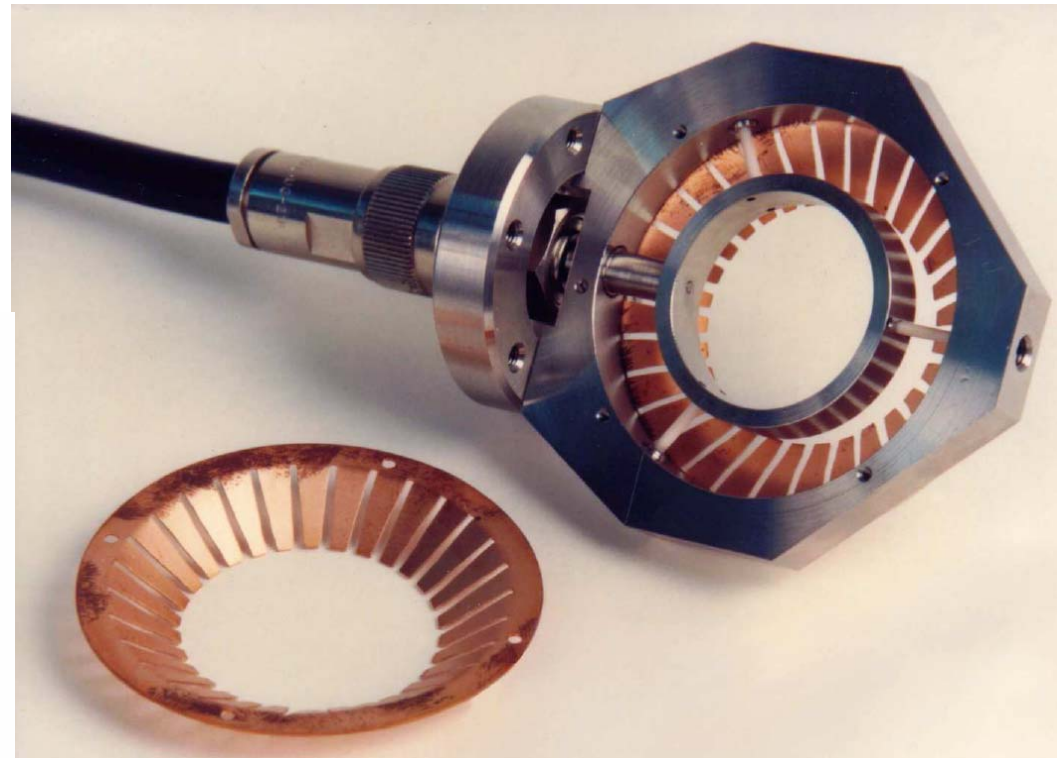
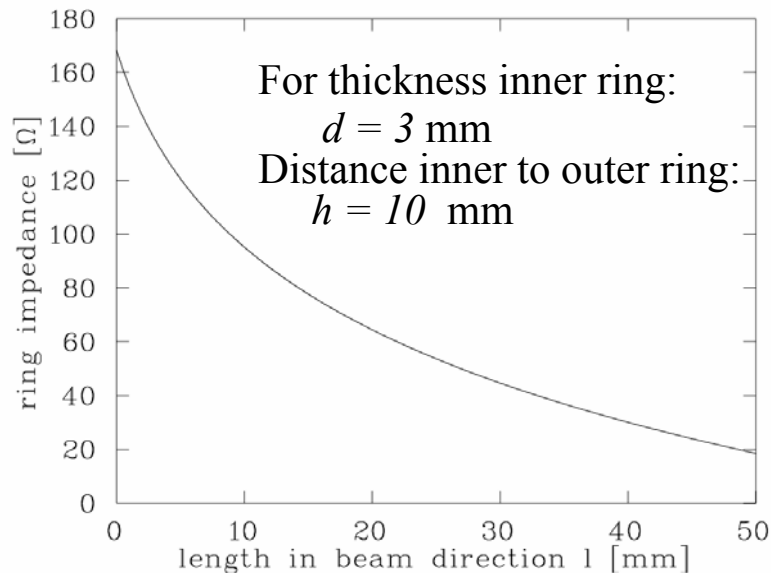


One ring in 50 Ω geometry to reach ≈ 1 GHz bandwidth.

The impedance is like a strip-line with 100 Ω due to the two passes of the signal:

$$Z_0(l) = \frac{87 [\Omega]}{\sqrt{\epsilon_r + 1.4}} \ln\left(\frac{5.98h}{0.8 \cdot l + d}\right)$$

\Rightarrow Impedance depends strongly on geometry



Principle of Position Determination by a BPM



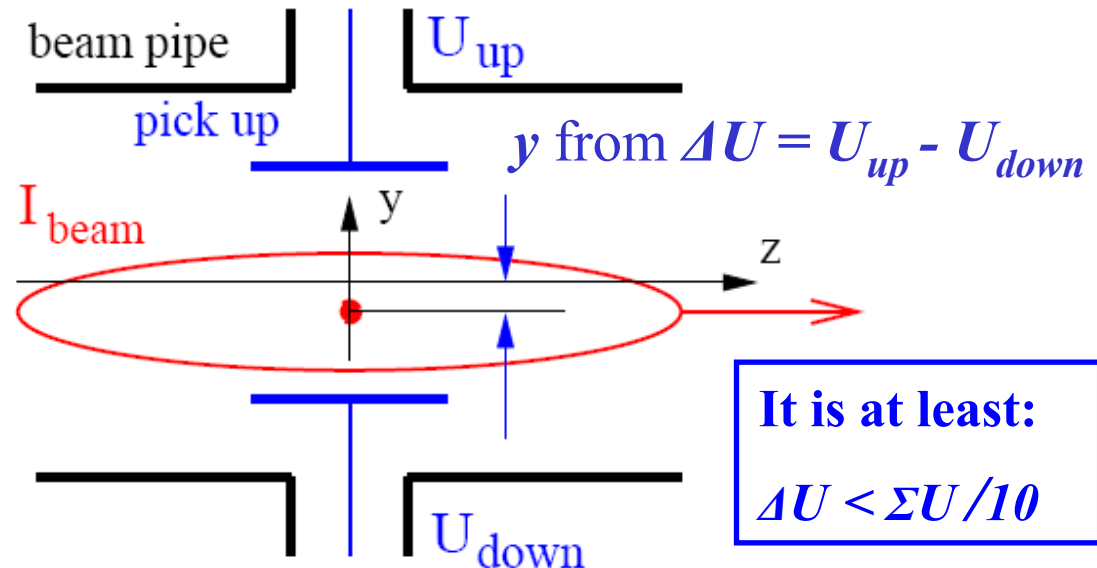
The difference voltage between plates gives the beam's center-of-mass
 → **most frequent application**

'Proximity' effect leads to different voltages at the plates:

$$y = \frac{1}{S_y(\omega)} \cdot \frac{U_{up} - U_{down}}{U_{up} + U_{down}} + \delta_y(\omega)$$

$$\equiv \frac{1}{S_y} \cdot \frac{\Delta U_y}{\Sigma U_y} + \delta_y$$

$$x = \frac{1}{S_x(\omega)} \cdot \frac{U_{right} - U_{left}}{U_{right} + U_{left}} + \delta_x(\omega)$$

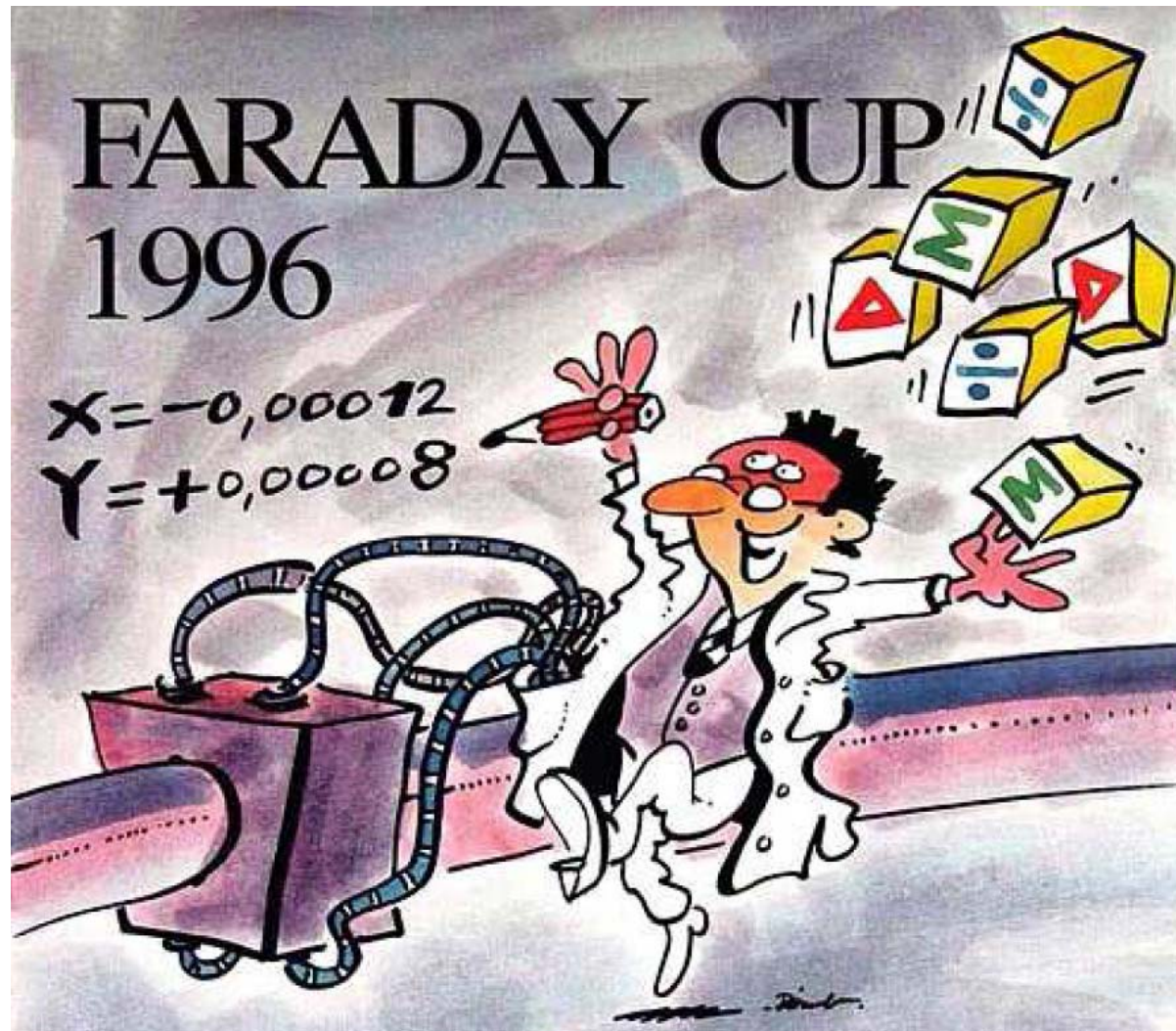


$S(\omega, \mathbf{x})$ is called **position sensitivity**, sometimes the inverse is used $k(\omega, \mathbf{x}) = 1/S(\omega, \mathbf{x})$

S is a geometry dependent, non-linear function, which have to be optimized

Units: $S = [\%/mm]$ and sometimes $S = [dB/mm]$ or $k = [mm]$.

The Artist View of a BPM



2-dim Model for a Button BPM



‘Proximity effect’: larger signal for closer plate

Ideal 2-dim model: Cylindrical pipe → image current density via ‘image charge method’ for ‘pensile’ beam:

$$j_{im}(\phi) = \frac{I_{beam}}{2\pi a} \cdot \left(\frac{a^2 - r^2}{a^2 + r^2 - 2ar \cdot \cos(\phi - \theta)} \right)$$

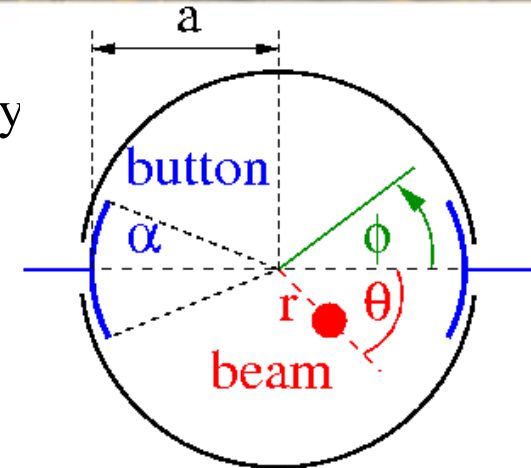
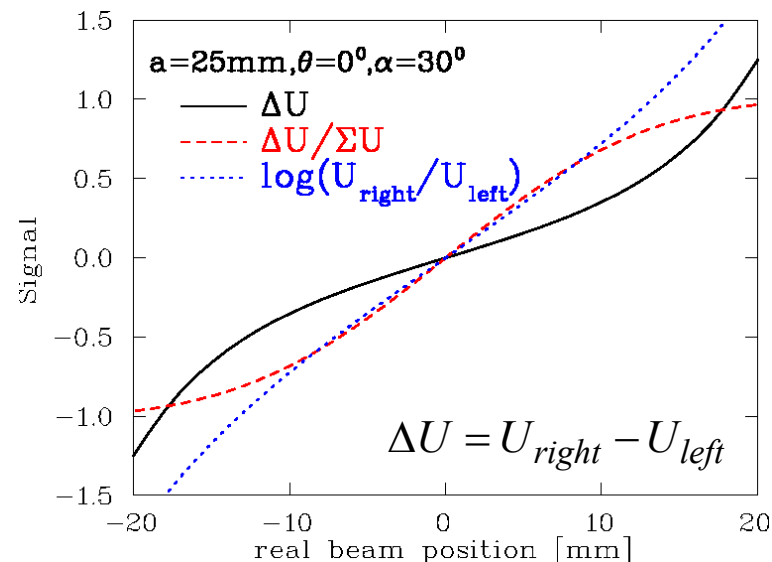
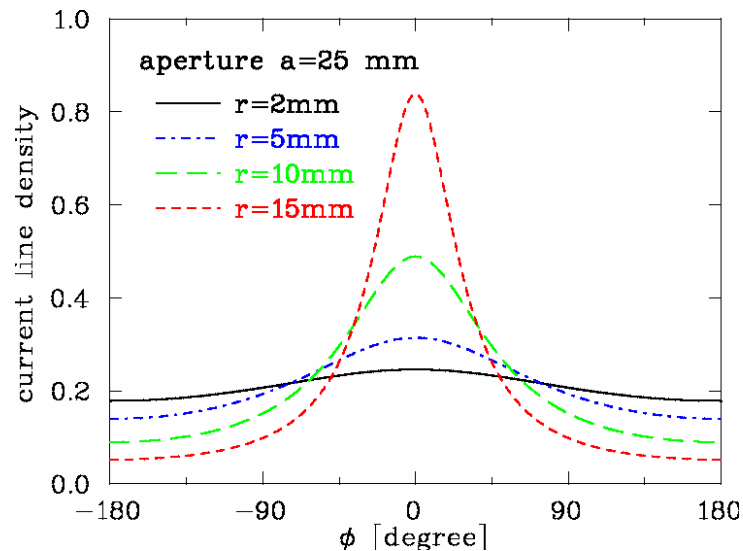


Image current: Integration of finite BPM size: $I_{im} = a \cdot \int_{-\alpha/2}^{\alpha/2} j_{im}(\phi) d\phi$



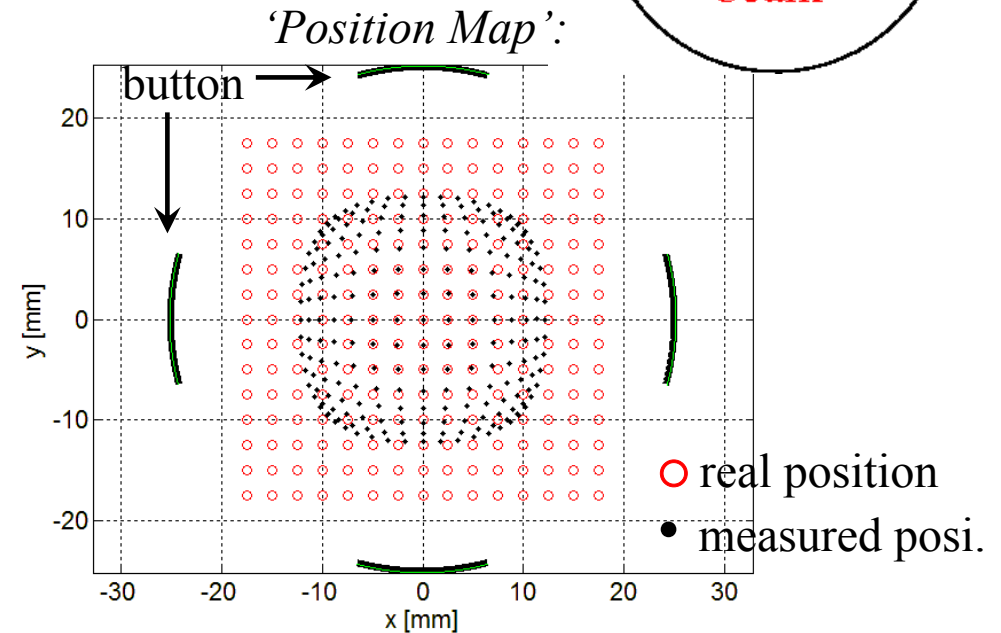
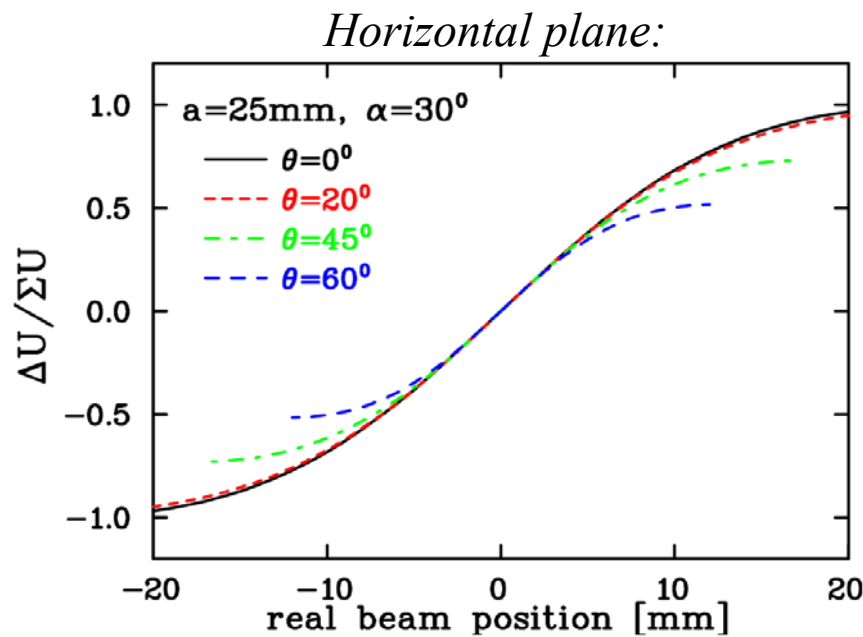
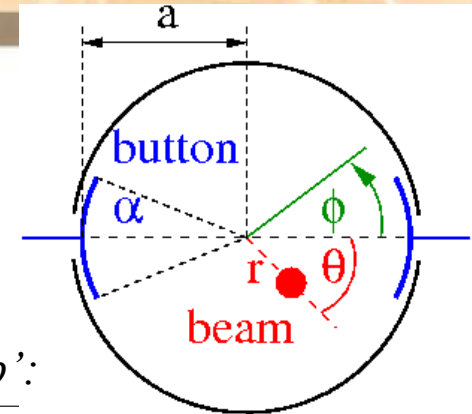
2-dim Model for a Button BPM



Ideal 2-dim model: Non-linear behavior and hor-vert coupling:

Sensitivity: $x = 1/S \cdot \Delta U / \Sigma U$ with S [%/mm] or [dB/mm]

For this example: center part $S = 7.4\%/mm \Leftrightarrow k = 1/S = 14mm$



The measurement of U delivers: $x = \frac{1}{S_x} \cdot \frac{\Delta U}{\Sigma U} \rightarrow$ here $S_x = S_x(x, y)$ i.e. non-linear.

Button BPM Realization

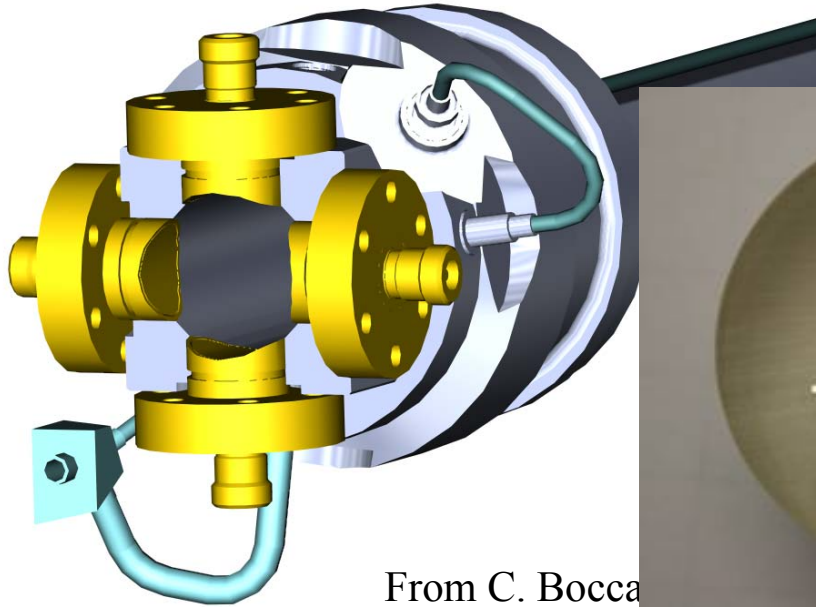
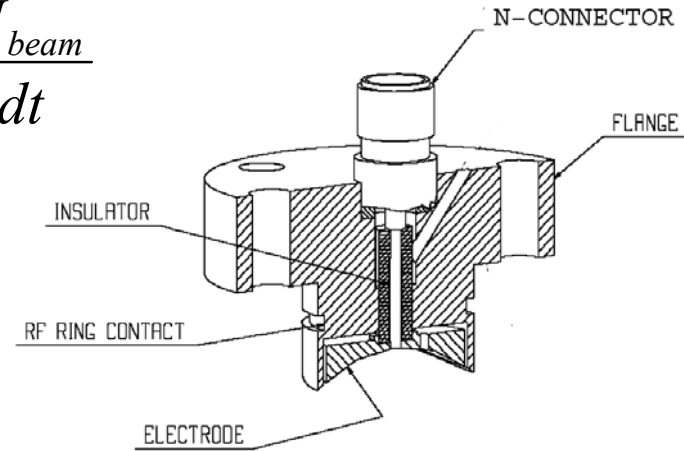
LINACs, e-synchrotrons: $100 \text{ MHz} < f_{rf} < 3 \text{ GHz} \rightarrow$ bunch length \approx BPM length
 $\rightarrow 50 \Omega$ signal path to prevent reflections

Button BPM with $50 \Omega \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$

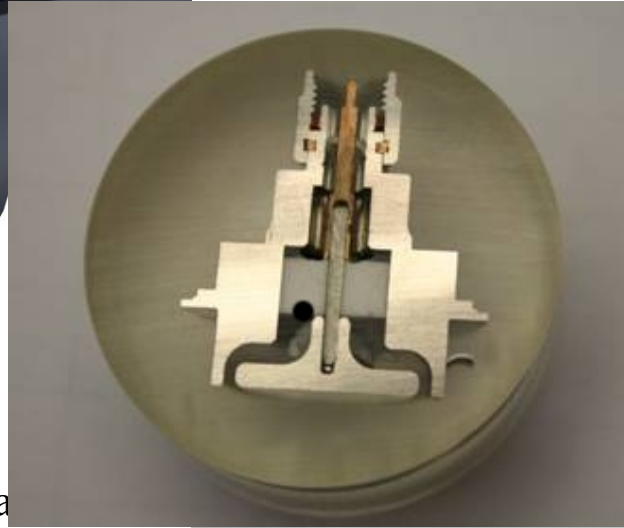
Example: LHC-type inside cryostat:

$\varnothing 24 \text{ mm}$, half aperture $a=25 \text{ mm}$, $C=8 \text{ pF}$

$\Rightarrow f_{cut}=400 \text{ MHz}$, $Z_t = 1.3 \Omega$ above f_{cut}



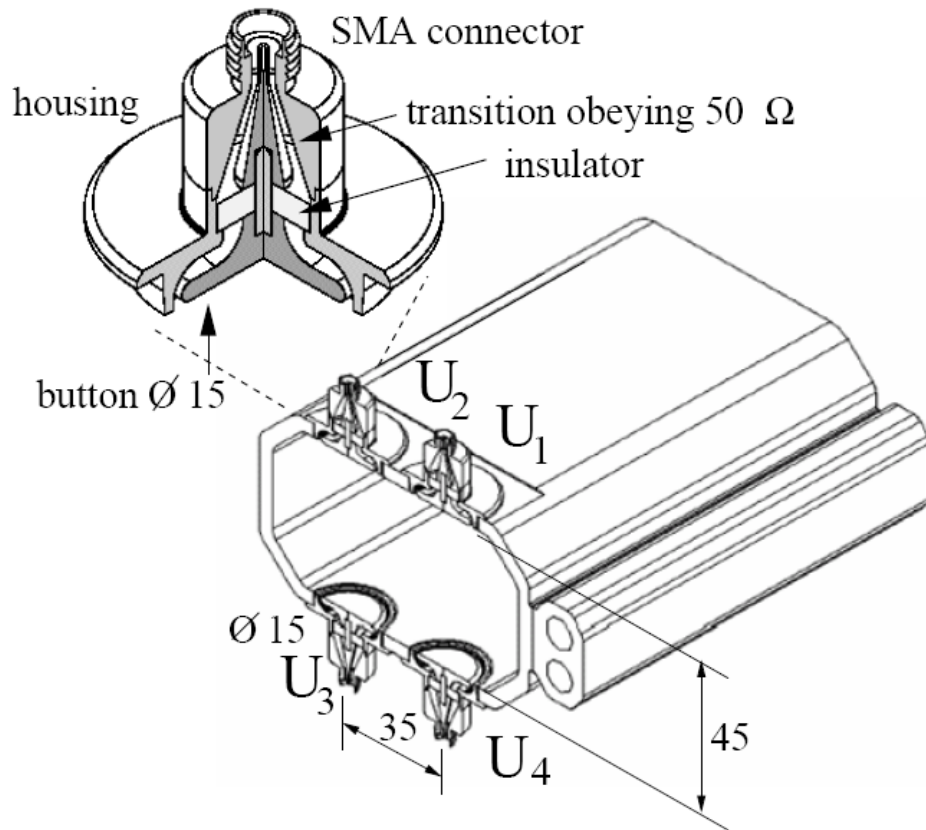
From C. Bocca



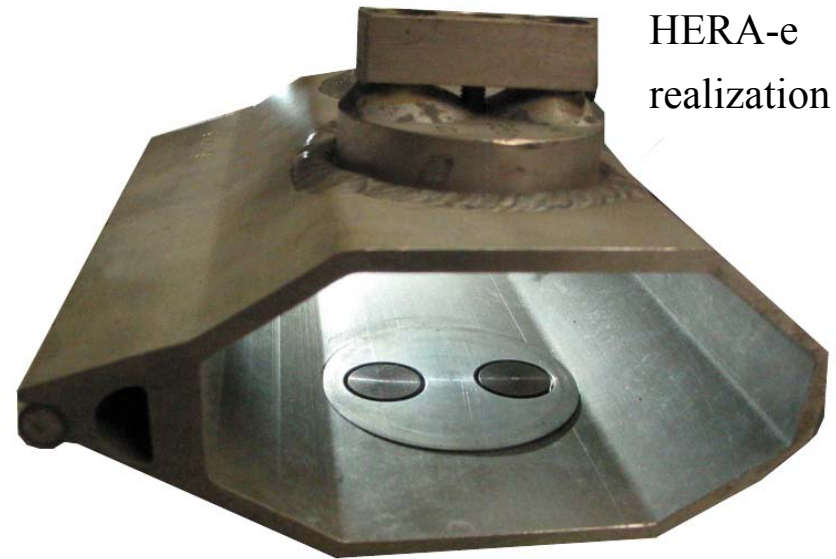
Button BPM at Synchrotron Light Sources



Due to synchrotron radiation, the button insulation might be destroyed
 ⇒ buttons only in vertical plane possible ⇒ increased non-linearity



PEP-realization



HERA-e realization

$$\text{horizontal : } x = \frac{1}{S_x} \cdot \frac{(U_2 + U_4) - (U_1 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

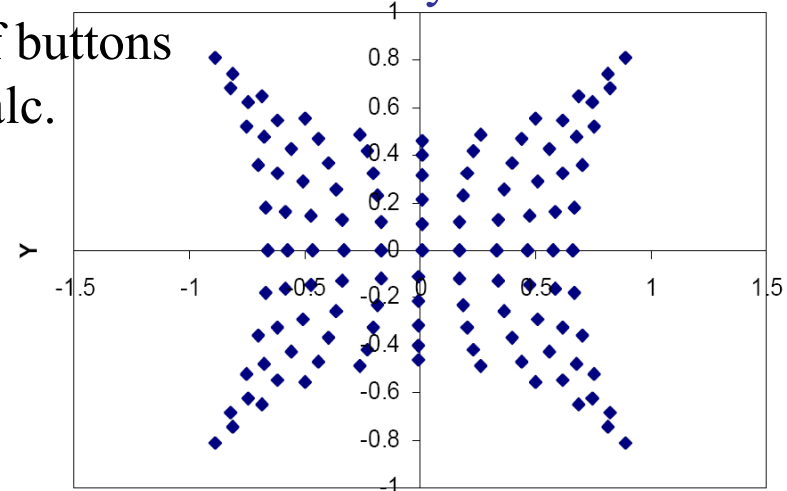
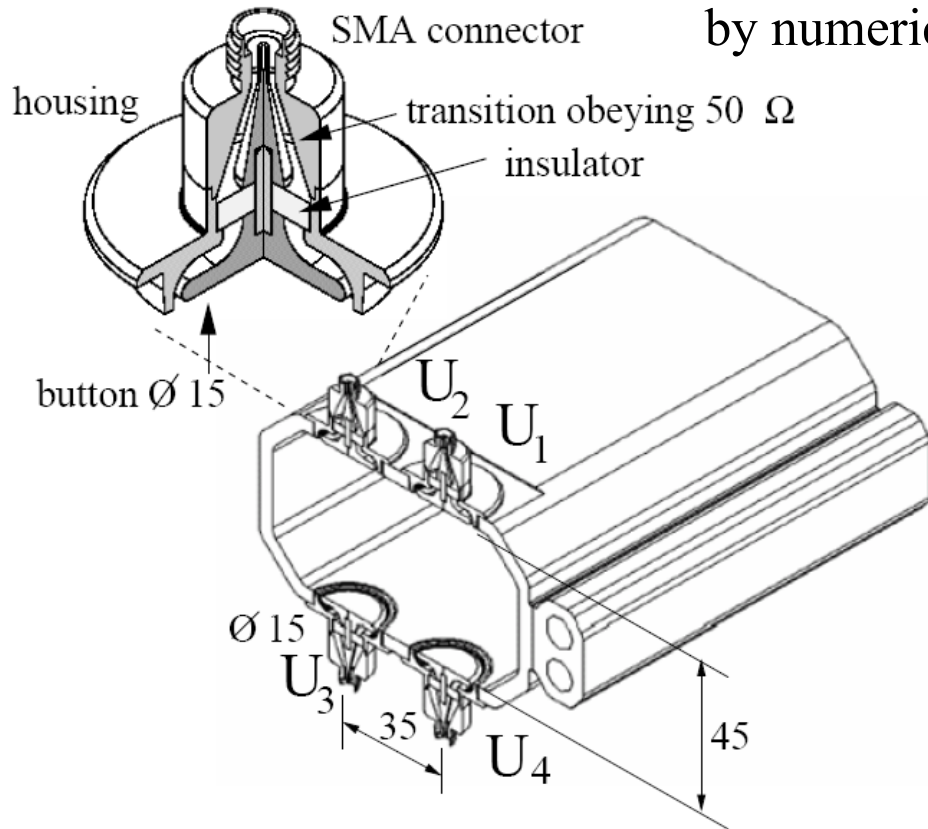
$$\text{vertical : } y = \frac{1}{S_y} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

Button BPM at Synchrotron Light Sources



Due to synchrotron radiation, the button insulation might be destroyed
 ⇒ buttons only in vertical plane possible ⇒ increased non-linearity

Optimization: horizontal distance and size of buttons
 by numerical calc.



- Beam position swept with 2 mm steps
- Non-linear sensitivity and hor.-vert. coupling
- At center $S_x = 8.5\%/mm$ in this example

$$\text{horizontal : } x = \frac{1}{S_x} \cdot \frac{(U_2 + U_4) - (U_1 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

$$\text{vertical : } y = \frac{1}{S_y} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$$

PEP-realization

From S. Varnasseri, SESAME, DIPAC 2005

Shoe-box BPM for Proton Synchrotrons

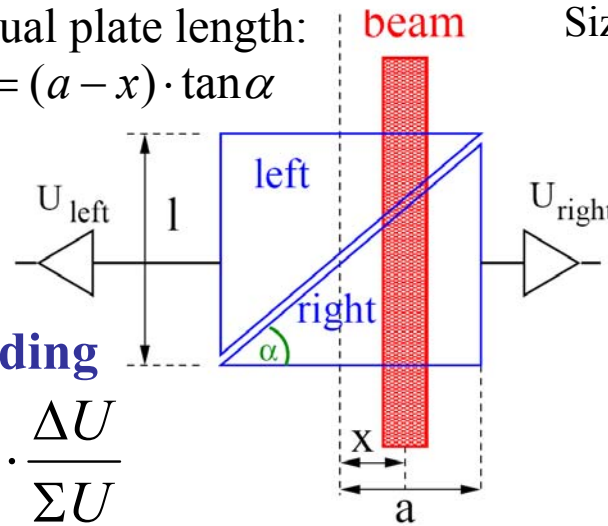


Frequency range: $1 \text{ MHz} < f_{rf} < 10 \text{ MHz} \Rightarrow \text{bunch-length} \gg \text{BPM length}$.

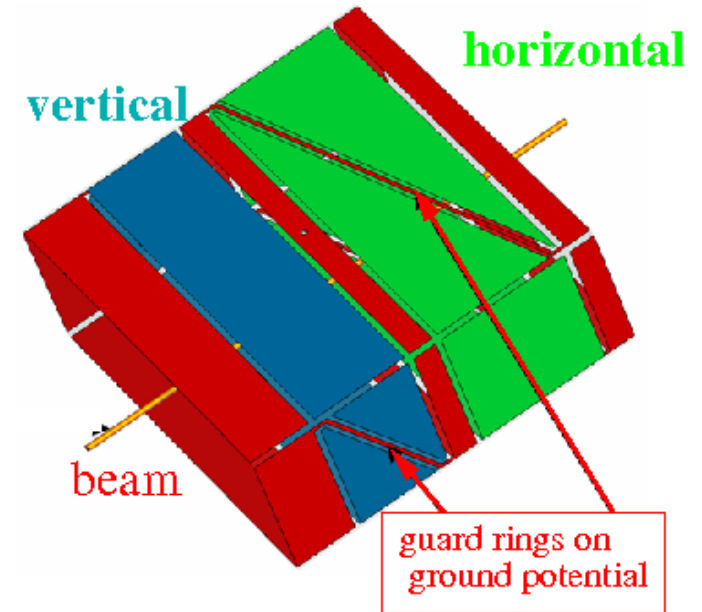
Signal is proportional to actual plate length:

$$l_{\text{right}} = (a + x) \cdot \tan \alpha, \quad l_{\text{left}} = (a - x) \cdot \tan \alpha$$

$$\Rightarrow x = a \cdot \frac{l_{\text{right}} - l_{\text{left}}}{l_{\text{right}} + l_{\text{left}}}$$

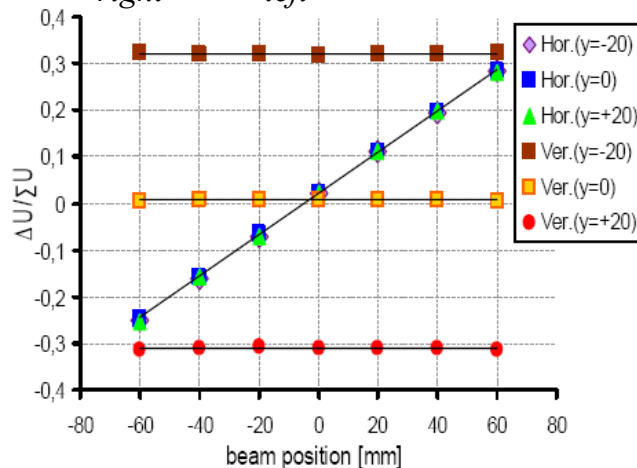


Size: $200 \times 70 \text{ mm}^2$



In ideal case: linear reading

$$x = a \cdot \frac{U_{\text{right}} - U_{\text{left}}}{U_{\text{right}} + U_{\text{left}}} \equiv a \cdot \frac{\Delta U}{\Sigma U}$$



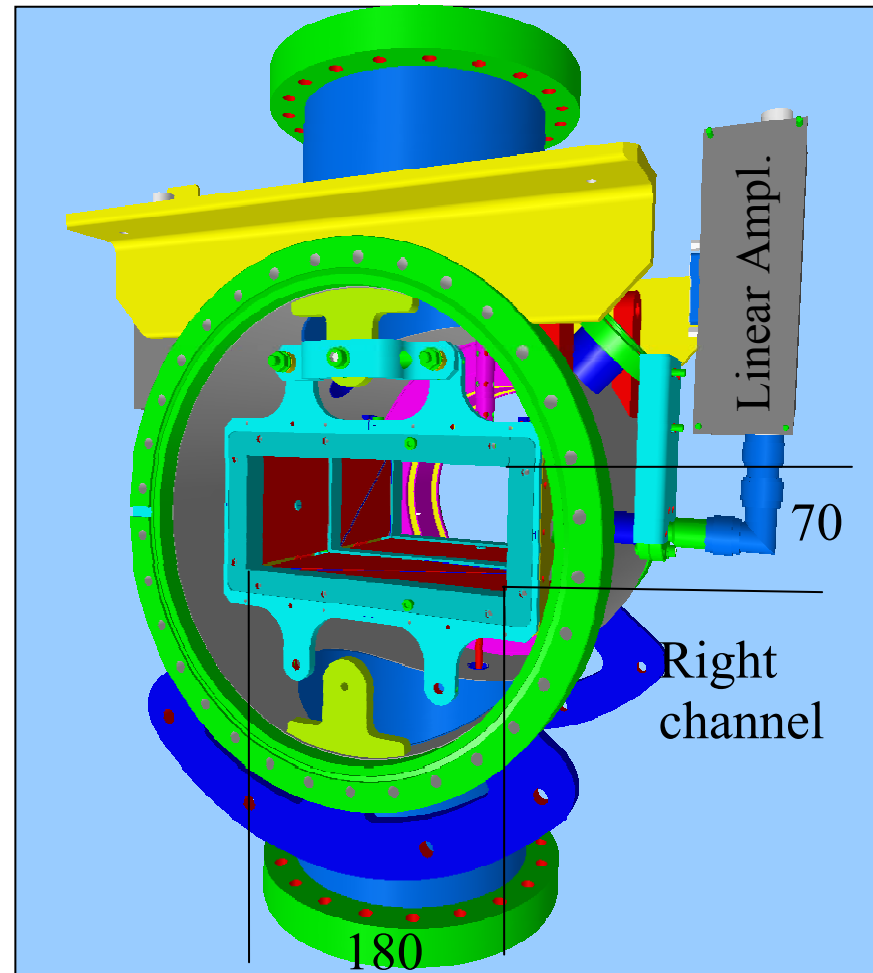
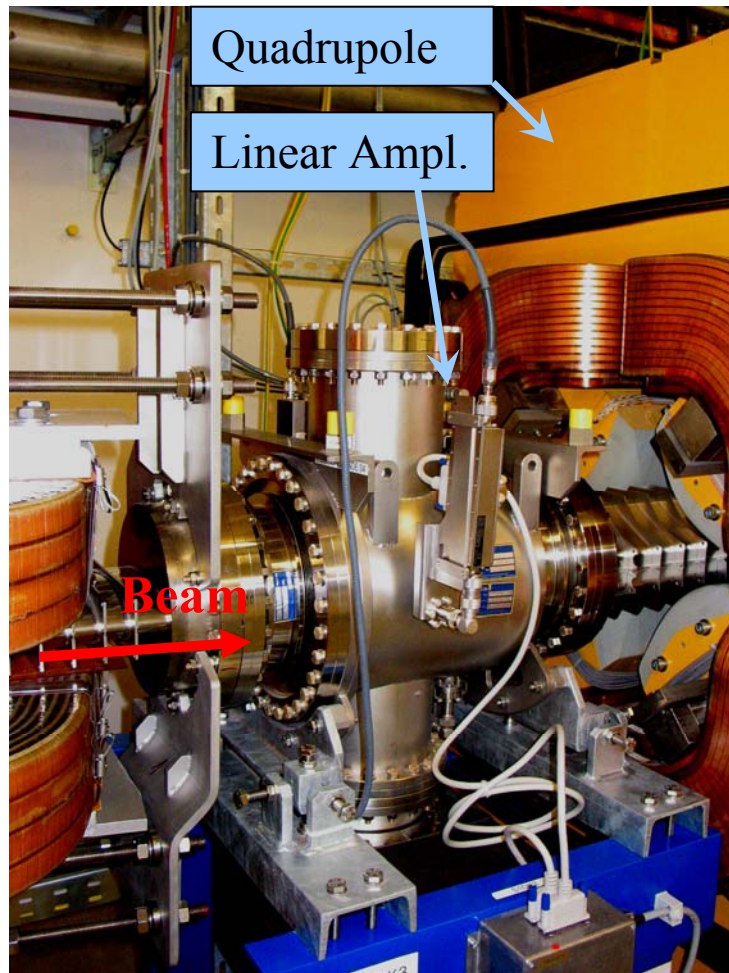
Shoe-box BPM:

Advantage: Very linear, low frequency dependence
i.e. position sensitivity \mathcal{S} is constant

Disadvantage: Large size, complex mechanics
high capacitance

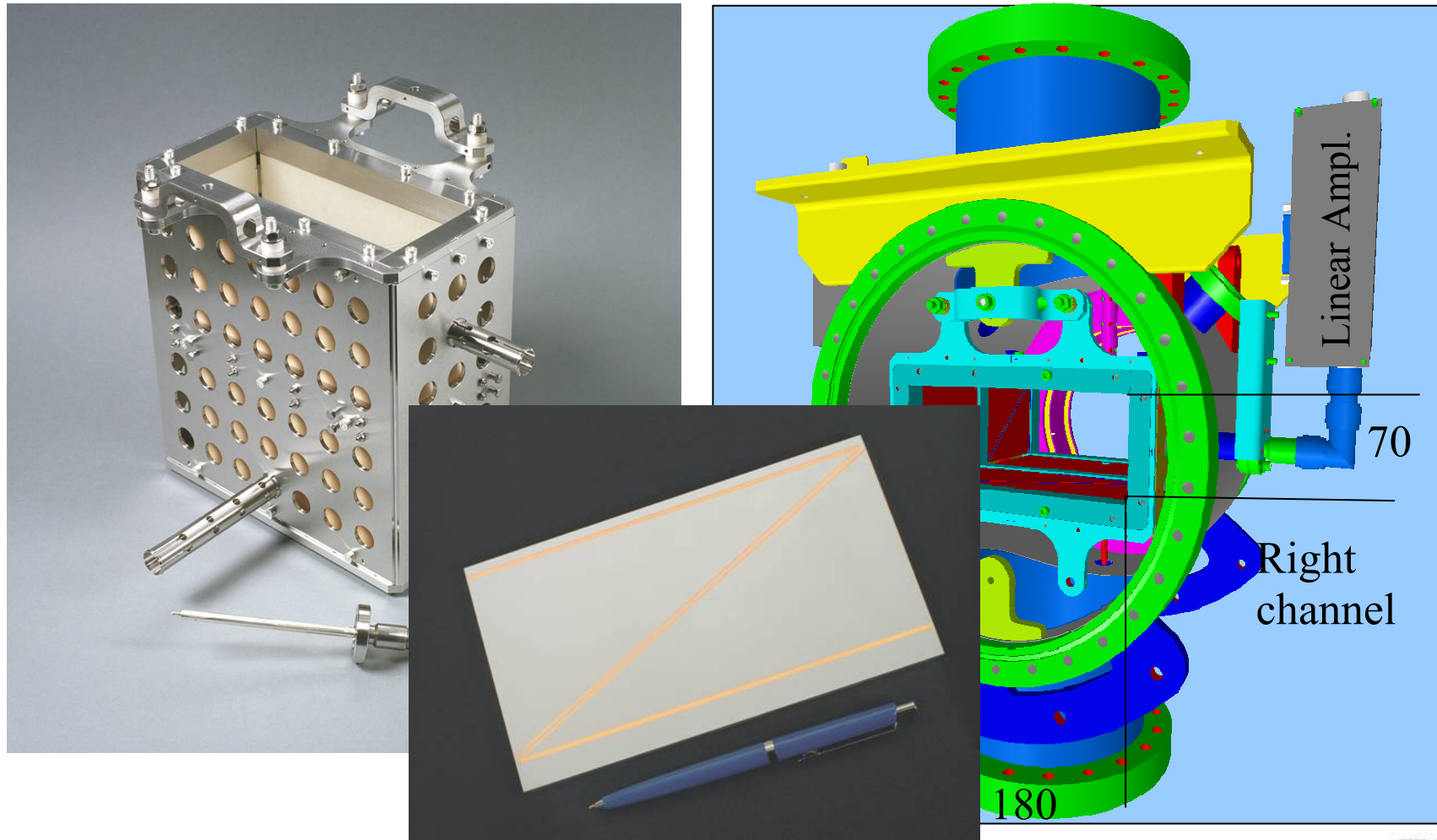
Technical Realization of a Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u \rightarrow 440 MeV/u
BPM clearance: 180x70 mm², standard beam pipe diameter: 200 mm.



Technical Realization of a Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u \rightarrow 440 MeV/u
BPM clearance: 180x70 mm², standard beam pipe diameter: 200 mm.



General: Noise Consideration

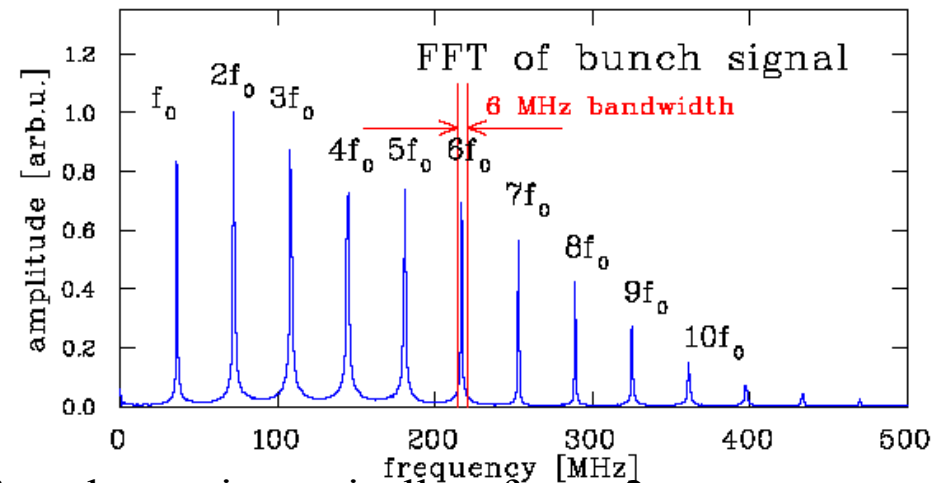
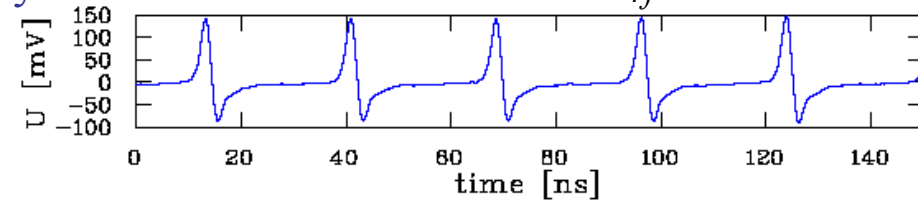


1. Signal voltage given by: $U_{im}(f) = Z_t(f) \cdot I_{beam}(f)$
2. Position information from voltage difference: $x = 1/S \cdot \Delta U / \Sigma U$
3. Thermal noise voltage given by: $U_{eff}(R, \Delta f) = \sqrt{4k_B \cdot T \cdot R \cdot \Delta f}$

⇒ Signal-to-noise $\Delta U_{im}/U_{eff}$ is influenced by:

- Input signal amplitude
→ large or matched Z_t
- Thermal noise at $R=50\Omega$ for $T=300K$
(for shoe box $R=1k\Omega \dots 1M\Omega$)
- Bandwidth Δf
⇒ Restriction of frequency width
because the power is concentrated
on the harmonics of f_{rf}

Example: GSI-LINAC with $f_{rf}=36$ MHz



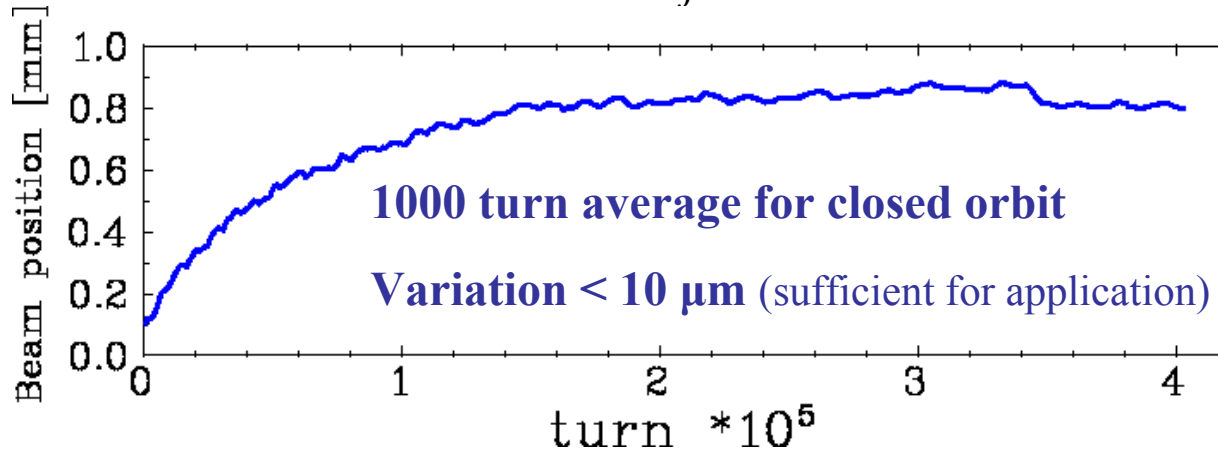
Remark: Additional contribution by non-perfect electronics typically a factor 2

Moreover, pick-up by electro-magnetic interference can contribute ⇒ good shielding required

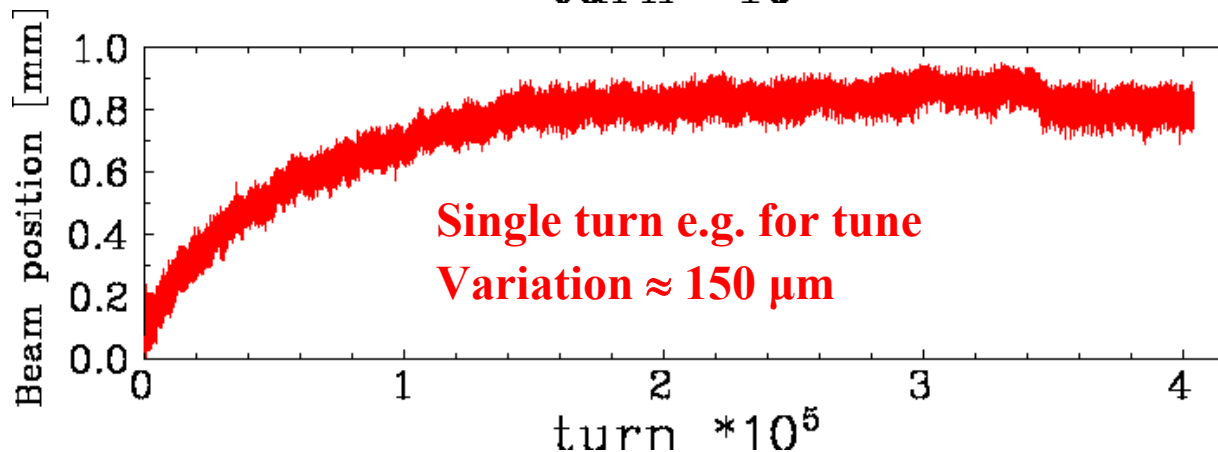
Comparison: Filtered Signal ↔ Single Turn



Example: GSI Synchr.: U^{73+} , $E_{inj}=11.5$ MeV/u \rightarrow 250 MeV/u within 0.5 s, 10^9 ions



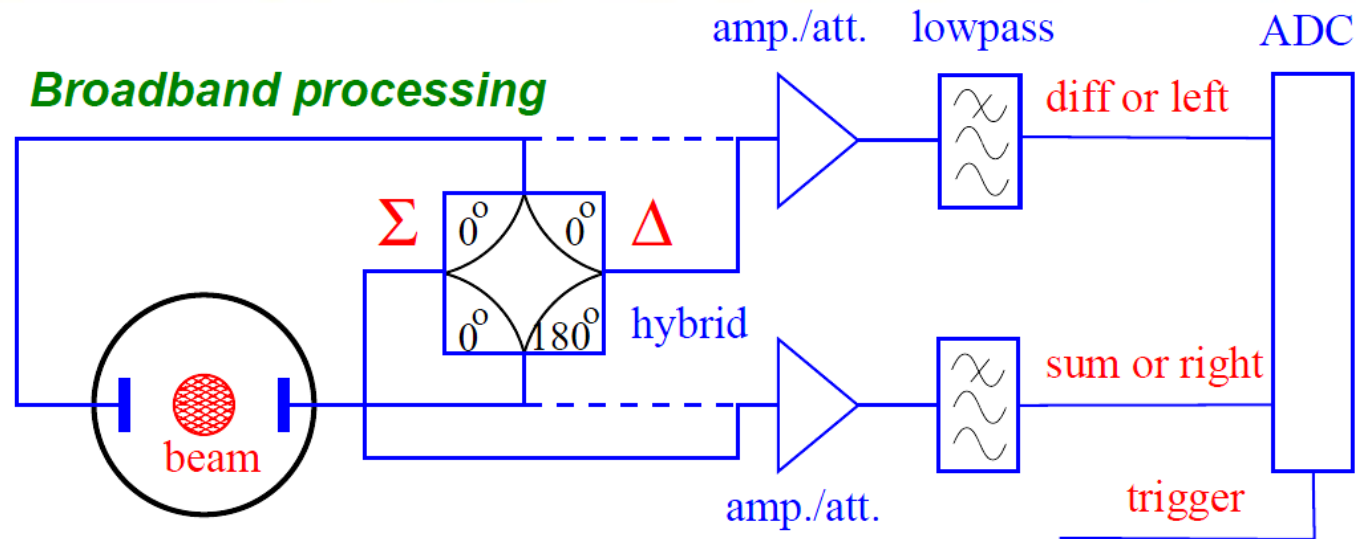
- Position resolution $< 30 \mu\text{m}$ (BPM half aperture $a=90$ mm)
- average over 1000 turns corresponding to ≈ 1 ms or ≈ 1 kHz bandwidth



- Turn-by-turn data have much larger variation

However: not only noise contributes but additionally **beam movement** by betatron oscillation \Rightarrow broadband processing i.e. turn-by-turn readout for tune determination.

Broadband Signal Processing

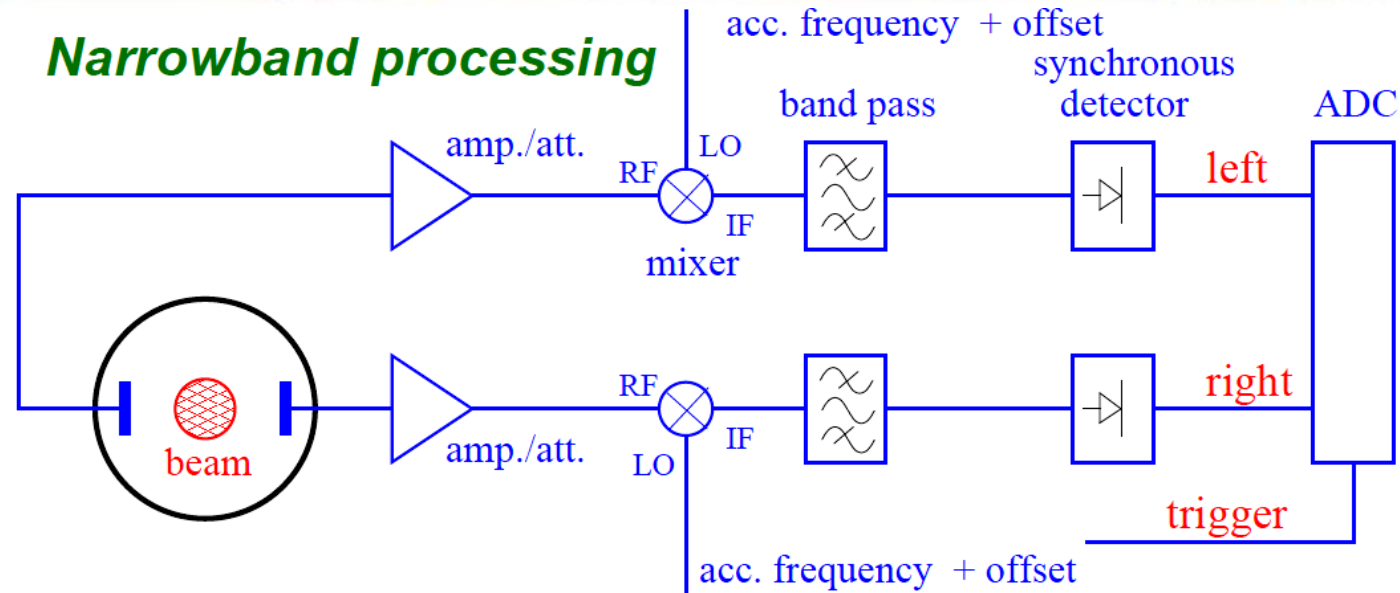


- Hybrid or transformer close to beam pipe for analog ΔU & ΣU generation or U_{left} & U_{right}
- Attenuator/amplifier
- Filter to get the wanted harmonics and to suppress stray signals
- ADC: digitalization → followed by calculation of $\Delta U / \Sigma U$

Advantage: Bunch-by-bunch possible, versatile post-processing possible

Disadvantage: Resolution down to $\approx 100 \mu\text{m}$ for shoe box type, i.e. $\approx 0.1\%$ of aperture, resolution is worse than narrowband processing

Narrowband Processing for improved Signal-to-Noise



Narrowband processing equals heterodyne receiver (e.g. AM-radio or spectrum analyzer)

- Attenuator/amplifier
- Mixing with accelerating frequency $f_{rf} \Rightarrow$ signal with sum and difference frequency
- Bandpass filter of the mixed signal (e.g at 10.7 MHz)
- Rectifier: synchronous detector
- ADC: digitalization \rightarrow followed calculation of $\Delta U/\Sigma U$

Advantage: spatial resolution about 100 time better than broadband processing

Disadvantage: No turn-by-turn diagnosis, due to mixing = 'long averaging time'

For non-relativistic p-synchrotron: \rightarrow variable f_{rf} leads via mixing to constant intermediate freq.

Mixer and Synchronous Detector



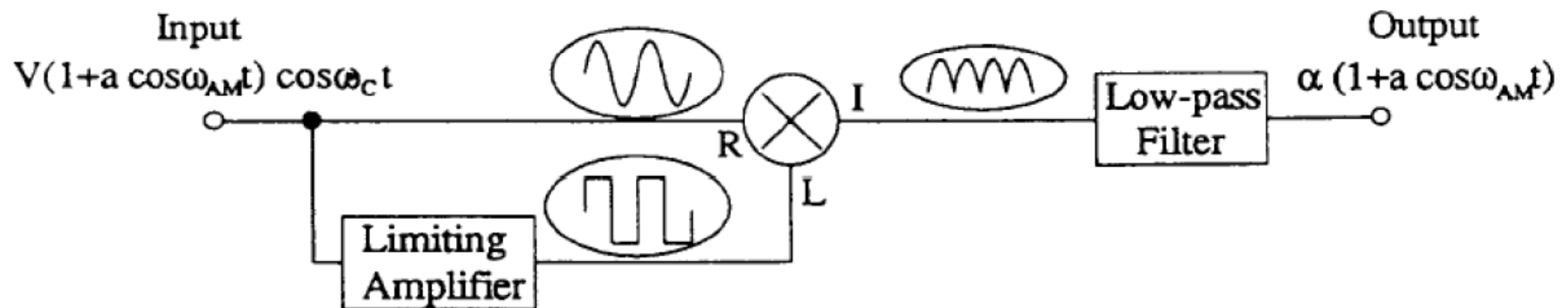
Mixer: A passive rf device with

- Input RF (radio frequency): Signal of investigation $A_{RF}(t) = A_{RF} \cos \omega_{RF} t$
- Input LO (local oscillator): Fixed frequency $A_{LO}(t) = A_{LO} \cos \omega_{LO} t$
- Output IF (intermediate frequency)

$$\begin{aligned} A_{IF}(t) &= A_{RF} \cdot A_{LO} \cos \omega_{RF} t \cdot \cos \omega_{LO} t \\ &= A_{RF} \cdot A_{LO} [\cos(\omega_{RF} - \omega_{LO})t + \cos(\omega_{RF} + \omega_{LO})t] \end{aligned}$$

⇒ Multiplication of both input signals, containing the sum and difference frequency.

Synchronous detector: A phase sensitive rectifier



Close Orbit Measurement with BPMs

Detected position on an analog narrowband basis → closed orbit with ms time steps.
It differs from ideal orbit by misalignments of the beam or components.

Example from GSI-Synchrotron:



Closed orbit:
Beam position
averaged over many
betatron oscillations.

Tune Measurement: General Considerations



The tune Q is the number of betatron oscillations per turn.

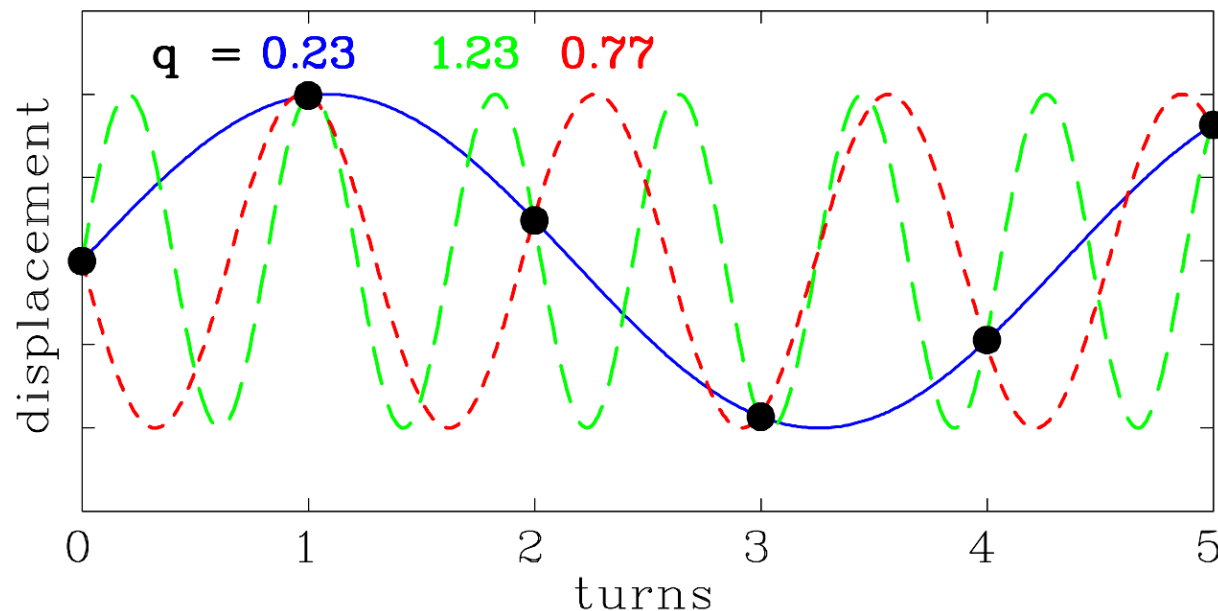
The betatron frequency is $f_\beta = Qf_0$.

Measurement: excitation of *coherent* betatron oscillations + position from one BPM.

From a measurement one gets only the non-integer part q of Q with $Q = n \pm q$.

Moreover, only $0 < q < 0.5$ is the unique result.

Example: Tune measurement for six turns with the three lowest frequency fits:



To distinguish

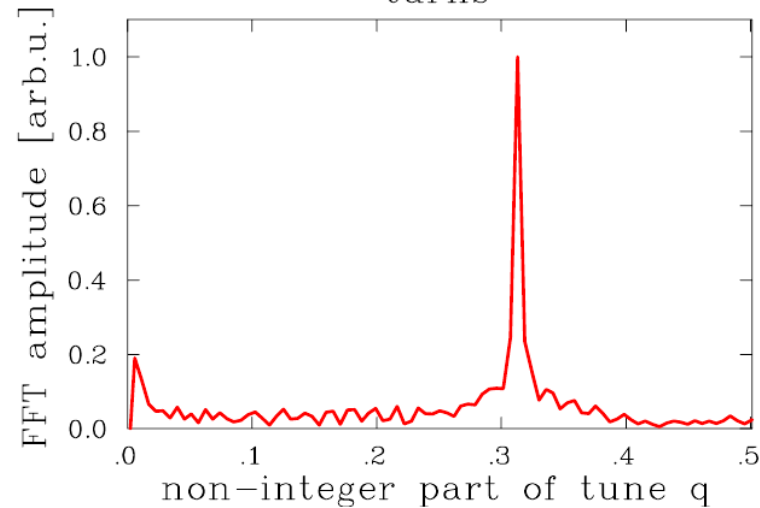
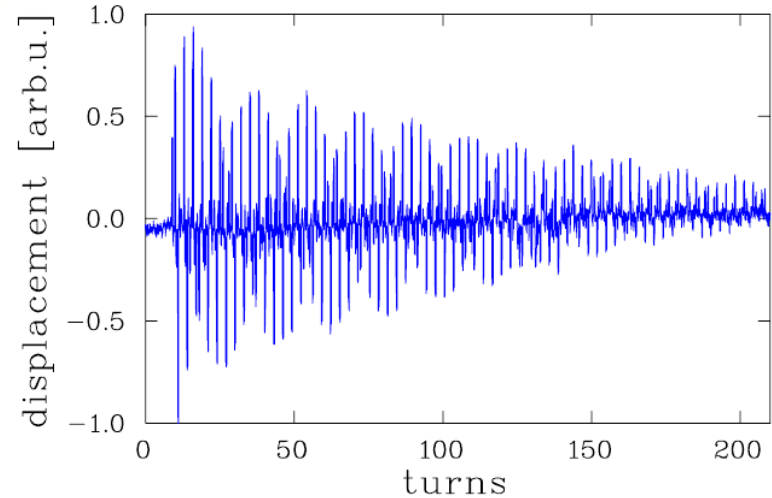
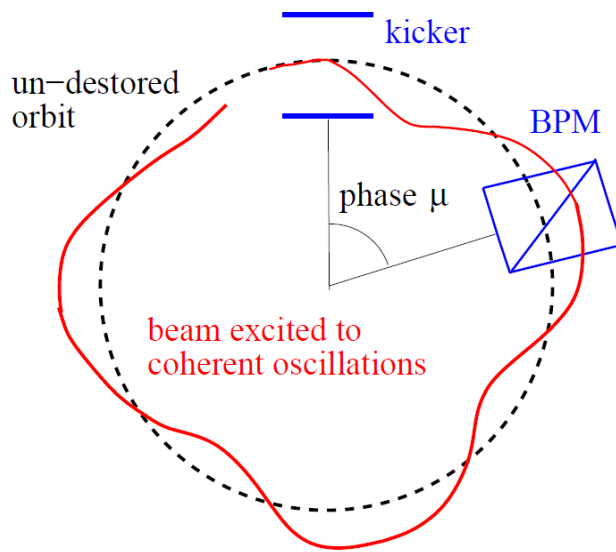
for $q < 0.5$ or $q > 0.5$:

Changing the tune slightly,
the direction of q shift differs.

Tune Measurement: The Kick-Method in Time Domain



The beam is excited to coherent betatron oscillation
 → the beam position measured each revolution ('turn-by-turn')
 → Fourier Trans. give the non-integer tune q .
 Short kick compared to revolution.



The de-coherence time limits the **resolution**:

N non-zero samples

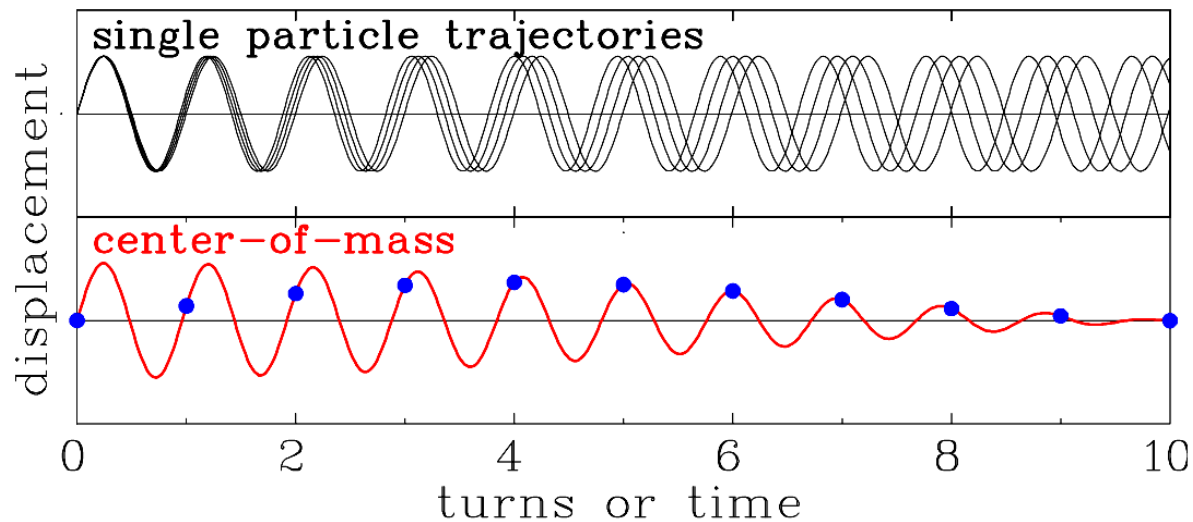
⇒ General limit of discrete FFT: $\Delta q > \frac{1}{2N}$

$N = 200$ turn ⇒ $\Delta q > 0.003$ as resolution
 (tune spreads are typically $\Delta q \approx 0.001!$)

Tune Measurement: De-Coherence Time



The particles are excited to betatron oscillations, but due to the spread in the betatron frequency, they get out of phase ('Landau damping'):



Scheme of the individual trajectories of four particles after a kick (top) and the resulting *coherent* signal as measured by a pick-up (bottom).

⇒ Kick excitation leads to limited resolution

Remark: The tune spread is much lower for a real machine.

Tune Measurement: Beam Transfer Function in Frequency Domain



Instead of one kick, the beam can be excited by a sweep of a sine wave, called ‘chirp’

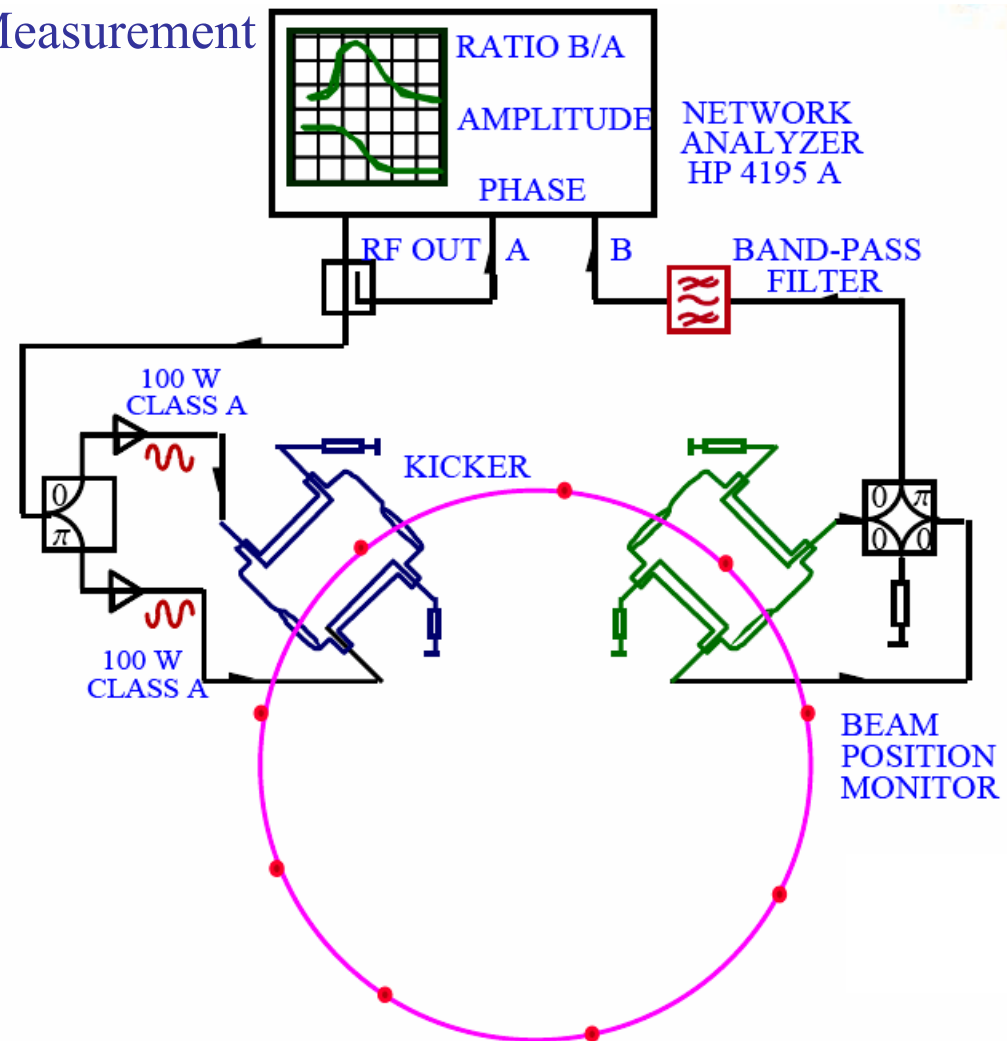
→ **Beam Transfer Function (BTF) Measurement**
as the velocity response to a kick

Prinziple:

Beam acts like a driven oscillator!

Using a network analyzer:

- RF OUT is feed to the beam by a kicker (reversed powered as a BPM)
- The position is measured at one BPM
- Network analyzer: amplitude and phase of the response
- Sweep time up to seconds due to de-coherence time per band
- resolution in tune: up to 10^{-4}



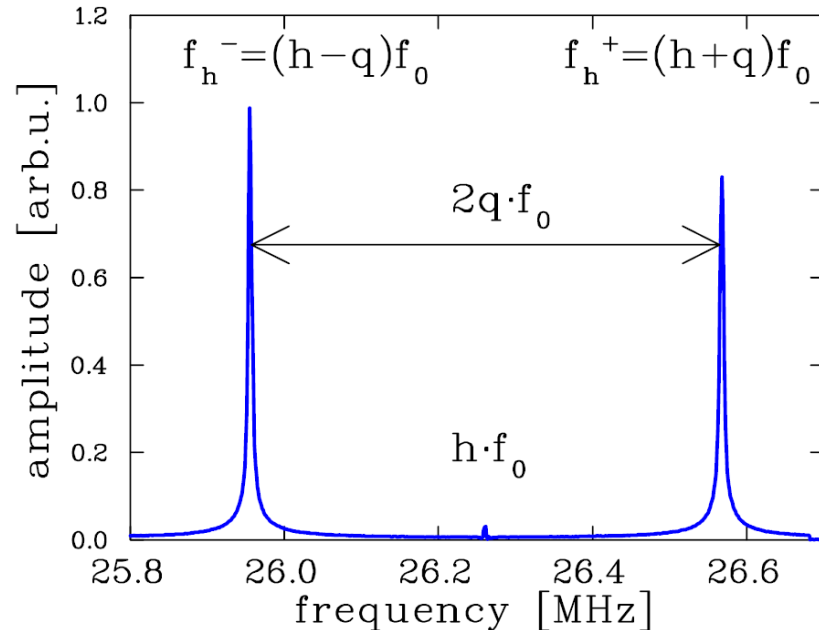
Tune Measurement: Result for BTF Measurement



BTF measurement at the GSI synchrotron, recorded at the 25th harmonics.

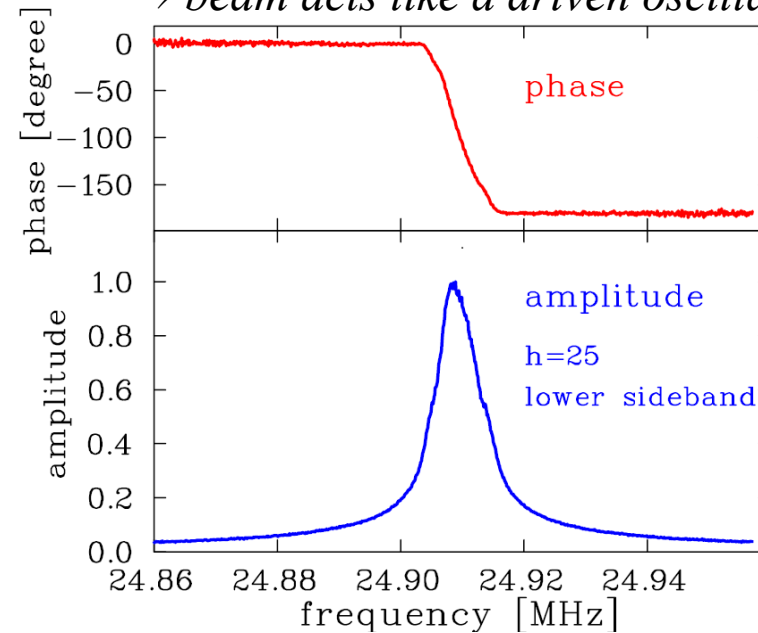
A wide scan with both sidebands at

$h=25^{\text{th}}$ -harmonics:



A detailed scan for the lower sideband

\Rightarrow beam acts like a driven oscillator:



From the position of the sidebands $q = 0.306$ is determined. From the width $\Delta f/f \approx 5 \cdot 10^{-4}$ the tune spread can be calculated via $\Delta f_h^- = \eta \frac{\Delta p}{p} \cdot h f_0 \left(h - q + \frac{\xi}{\eta} Q \right)$

Advantage: High resolution for tune and tune spread (also for de-bunched beams)

Disadvantage: Long sweep time (up to several seconds).

Tune Measurement: *Gentle* Excitation with Wideband Noise



Instead of a sine wave, noise with adequate bandwidth can be applied

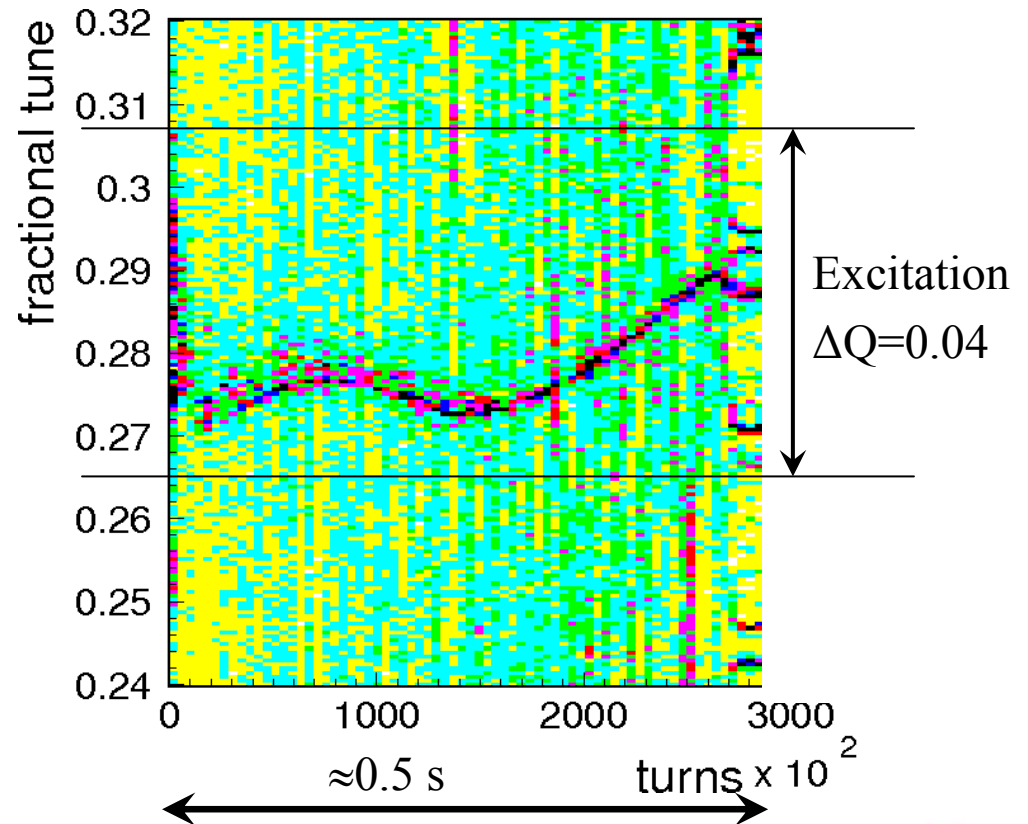
→ beam picks out its resonance frequency: *Example: Vertical tune within 2048 turn at GSI synchrotron 11 → 250 MeV/u
2048 turn FFT equals ≈ 5 ms.*

- broadband excitation with white noise of ≈ 10 kHz bandwidth
 - turn-by-turn position measurement by fast ADC
 - Fourier transformation of the recorded data
- ⇒ Continues monitoring with low disturbance

Advantage:

Fast scan with good time resolution

Disadvantage: Lower precision



β -Function Measurement from Bunch-by-Bunch BPM Data



Excitation of coherent betatron oscillations: From the position deviation x_{ik} at the BPM i and turn k the β -function $\beta(s_i)$ can be evaluated.

The position reading is: (\hat{x}_i amplitude, μ_i phase at i , Q tune, s_0 reference location)

$$x_{ik} = \hat{x}_i \cdot \cos(2\pi Qk + \mu_i) = \hat{x}_0 \cdot \sqrt{\beta(s_i) / \beta(s_0)} \cdot \cos(2\pi Qk + \mu_i)$$

→ a turn-by-turn position reading at many location (4 per unit of tune) is required.

The ratio of β -functions at different location:

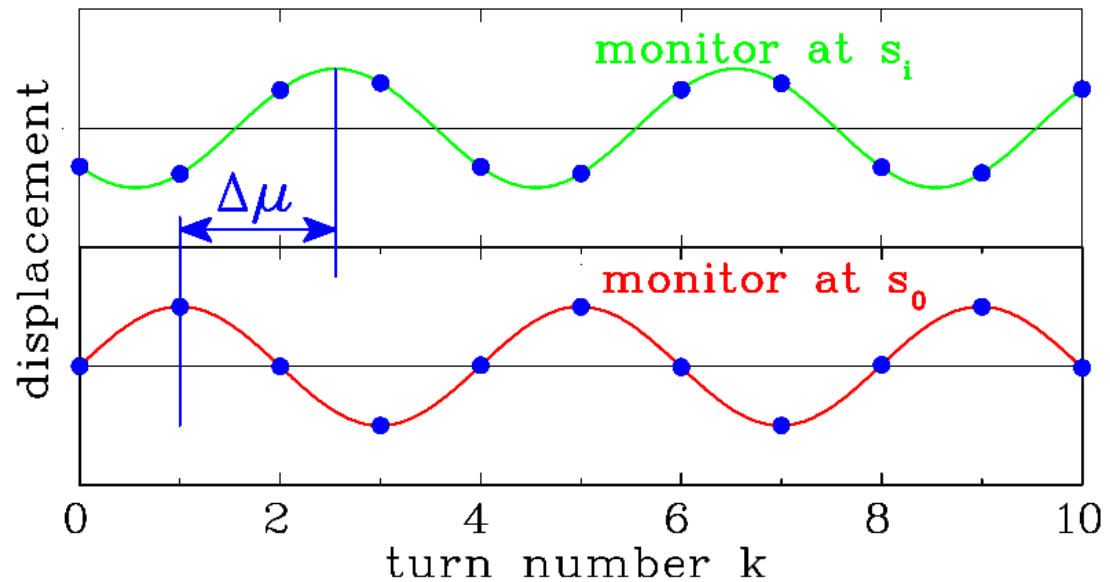
$$\frac{\beta(s_i)}{\beta(s_0)} = \left(\frac{\hat{x}_i}{\hat{x}_0} \right)^2$$

The phase advance is:

$$\Delta\mu = \mu_i - \mu_0$$

Without absolute calibration, β -function is more precise:

$$\Delta\mu = \int_{s_0}^{s_i} \frac{ds}{\beta(s)}$$



Dispersion and Chromaticity Measurement



Dispersion $D(s_i)$: Excitation of coherent betatron oscillations and change of momentum p by detuned rf-cavity:

→ Position reading at one location: $x_i = D(s_i) \cdot \frac{\Delta p}{p}$

→ Result from plot of x_i as a function of $\Delta p/p \Rightarrow$ slope is local dispersion $D(s_i)$.

Chromaticity ξ : Excitation of coherent betatron oscillations and change of momentum p by detuned rf-cavity:

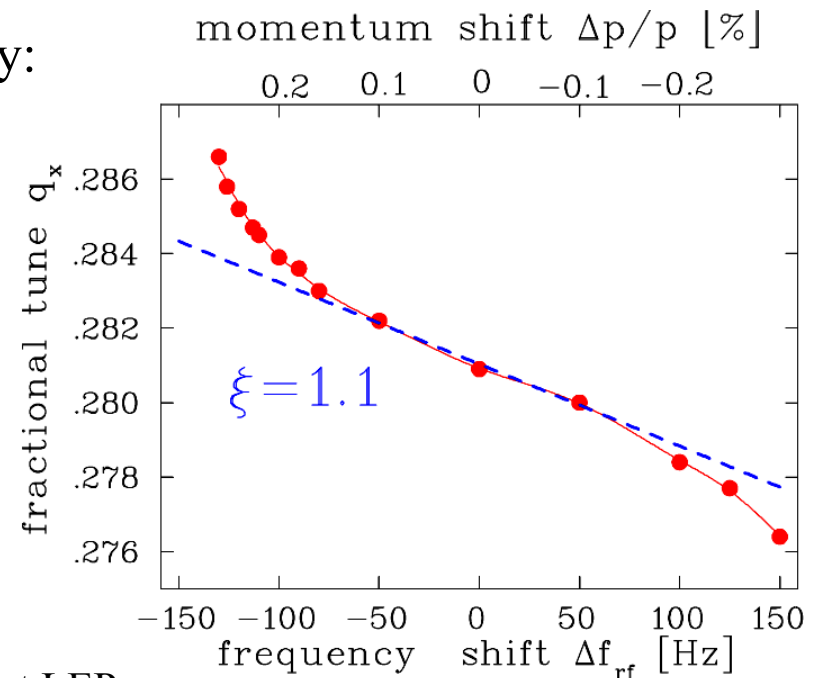
→ Tune measurement

(kick-method, BTF, noise excitation):

$$\frac{\Delta Q}{Q} = \xi \cdot \frac{\Delta p}{p}$$

Plot of $\Delta Q/Q$ as a function of $\Delta p/p$

\Rightarrow slope is dispersion ξ .



Measurement at LEP

Summary Pick-Ups for bunched Beams



The electric field is monitored for bunched beams using rf-technologies ('frequency domain'). Beside transformers they are the most often used instruments!

Differentiated or proportional signal: rf-bandwidth \leftrightarrow beam parameters

Proton synchrotron: 1 to 100 MHz, mostly 1 M Ω \Rightarrow proportional shape

LINAC, e⁻-synchrotron: 0.1 to 3 GHz, 50 Ω \Rightarrow differentiated shape

Important quantity: transfer impedance $Z_t(\omega, \beta)$.

Types of capacitive pick-ups:

Shoe-box (p-synch.), button (p-LINAC, e⁻-LINAC and synch.)

Remark: Stripline BPM as traveling wave devices are frequently used

Position reading: difference signal of four pick-up plates (BPM):

- **Non-intercepting** reading of center-of-mass \rightarrow online measurement and control
 - slow reading* \rightarrow closed orbit, *fast bunch-by-bunch* \rightarrow trajectory
- Excitation of *coherent betatron oscillations* and response measurement
 - excitation by short kick, white noise or sine-wave (BTF)
 - \rightarrow tune q , chromaticity ξ , dispersion D etc.